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# Lessons In Electric Circuits, Volume V - Reference 

By Tony R. Kuphaldt
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## Chapter 1

## USEFUL EQUATIONS AND CONVERSION FACTORS

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### 1.1 DC circuit equations and laws

### 1.1.1 Ohm's and Joule's Laws

## Ohm's Law

$\mathrm{E}=\mathrm{IR} \quad \mathrm{I}=\frac{\mathrm{E}}{\mathrm{R}} \quad \mathrm{R}=\frac{\mathrm{E}}{\mathrm{I}}$

## Joule's Law

$\mathrm{P}=\mathrm{IE} \quad \mathrm{P}=\frac{\mathrm{E}^{2}}{\mathrm{R}} \quad \mathrm{P}=\mathrm{I}^{2} \mathrm{R}$
Where,
$\mathrm{E}=$ Voltage in volts
$\mathrm{I}=$ Current in amperes (amps)
$\mathrm{R}=$ Resistance in ohms
$\mathrm{P}=$ Power in watts
NOTE: the symbol "V" ("U" in Europe) is sometimes used to represent voltage instead of "E". In some cases, an author or circuit designer may choose to exclusively use " V " for voltage, never using the symbol "E." Other times the two symbols are used interchangeably, or "E" is used to represent voltage from a power source while " V " is used to represent voltage across a load (voltage "drop").

### 1.1.2 Kirchhoff's Laws

"The algebraic sum of all voltages in a loop must equal zero." Kirchhoff's Voltage Law (KVL)
"The algebraic sum of all currents entering and exiting a node must equal zero." Kirchhoff's Current Law (KCL)

### 1.2 Series circuit rules

- Components in a series circuit share the same current. $\mathrm{I}_{\text {total }}=\mathrm{I}_{1}=\mathrm{I}_{2}=\ldots \mathrm{I}_{n}$
- Total resistance in a series circuit is equal to the sum of the individual resistances, making it greater than any of the individual resistances. $\mathrm{R}_{\text {total }}=\mathrm{R}_{1}+\mathrm{R}_{2}+\ldots \mathrm{R}_{n}$
- Total voltage in a series circuit is equal to the sum of the individual voltage drops. $\mathrm{E}_{\text {total }}=$ $\mathrm{E}_{1}+\mathrm{E}_{2}+\ldots \mathrm{E}_{n}$


### 1.3 Parallel circuit rules

- Components in a parallel circuit share the same voltage. $\mathrm{E}_{\text {total }}=\mathrm{E}_{1}=\mathrm{E}_{2}=\ldots \mathrm{E}_{n}$
- Total resistance in a parallel circuit is less than any of the individual resistances. $\mathrm{R}_{\text {total }}=1$ $/\left(1 / \mathrm{R}_{1}+1 / \mathrm{R}_{2}+\ldots 1 / \mathrm{R}_{n}\right)$
- Total current in a parallel circuit is equal to the sum of the individual branch currents. $\mathrm{I}_{\text {total }}$ $=\mathrm{I}_{1}+\mathrm{I}_{2}+\ldots \mathrm{I}_{n}$


### 1.4 Series and parallel component equivalent values

### 1.4.1 Series and parallel resistances

## Resistances

$\mathrm{R}_{\text {series }}=\mathrm{R}_{1}+\mathrm{R}_{2}+\ldots \mathrm{R}_{n}$
$\mathrm{R}_{\text {parallel }}=\frac{1}{\frac{1}{\mathrm{R}_{1}}+\frac{1}{\mathrm{R}_{2}}+\ldots \frac{1}{\mathrm{R}_{n}}}$

### 1.4.2 Series and parallel inductances

## Inductances

$\mathrm{L}_{\text {series }}=\mathrm{L}_{1}+\mathrm{L}_{2}+\ldots \mathrm{L}_{n}$
$\mathrm{L}_{\text {parallel }}=\frac{1}{\frac{1}{\mathrm{~L}_{1}}+\frac{1}{\mathrm{~L}_{2}}+\ldots \frac{1}{\mathrm{~L}_{n}}}$

Where,
$\mathrm{L}=$ Inductance in henrys

### 1.4.3 Series and Parallel Capacitances

## Capacitances

$$
\begin{aligned}
& \mathrm{C}_{\text {series }}=\frac{1}{\frac{1}{\mathrm{C}_{1}}+\frac{1}{\mathrm{C}_{2}}+\ldots \frac{1}{\mathrm{C}_{n}}} \\
& \mathrm{C}_{\text {parallel }}=\mathrm{C}_{1}+\mathrm{C}_{2}+\ldots \mathrm{C}_{n} \\
& \text { Where, } \\
& \quad \mathrm{C}=\text { Capacitance in farads }
\end{aligned}
$$

### 1.5 Capacitor sizing equation

$$
\begin{aligned}
& \mathrm{C}=\frac{\varepsilon \mathrm{A}}{\mathrm{~d}} \\
& \text { Where }, \\
& \mathrm{C}
\end{aligned}=\text { Capacitance in Farads } \quad \begin{aligned}
& \varepsilon=\begin{array}{l}
\text { Permittivity of dielectric (absolute, not } \\
\text { relative) }
\end{array} \\
& \mathrm{A}=\text { Area of plate overlap in square meters } \\
& \mathrm{d}=\text { Distance between plates in meters } \\
& \varepsilon=\varepsilon_{0} \mathrm{~K}
\end{aligned}
$$

| Dielectric constants |  |  |  |
| :---: | :---: | :---: | :---: |
| Dielectric | K | Dielectric K |  |
| Vacuum | 1.0000 | Quartz, fused | 3.8 |
| Air | 1.0006 | Wood, maple | 4.4 |
| PTFE, Teflon | 2.0 | Glass | 4.9-7.5 |
| Mineral oil | 2.0 | Castor oil |  |
| Polypropylene | 2.20-2.28 | Wood, birch | 5.2 |
| ABS resin | $2.45-3.2$ | Mica, muscovite | 5.0-8.7 |
| Polystyrene | 2.45-4 | Glass-bonded mica | ca 6.3-9.3 |
| Waxed paper | 2.5 | Poreclain, steatie | 6.5 |
| Transformer oil | 2.5-4 | Alumina $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 8-10.0 |
| Wood, oak | 3.3 | Water, distilled | 80 |
| Hard Rubber | 2.5-4.8 |  | 27.6 |
| Silicones | 3.4-4.3 | ${ }_{\text {Ba }} \mathrm{Ba}_{2} \mathrm{TiO}_{3}$ | 1200-1500 |
| Bakelite | 3.5-6.0 | $\mathrm{BaSrTiO}_{3}$ | 17500 |

A formula for capacitance in picofards using practical dimensions:

$$
\begin{aligned}
& \mathrm{C}=\frac{0.0885 \mathrm{~K}(\mathrm{n}-1) \mathrm{A}}{\mathrm{~d}}=\frac{0.225 \mathrm{~K}(\mathrm{n}-1) \mathrm{A}^{\prime}}{\mathrm{d}^{\prime}} \\
& \text { Where, } \\
& \mathrm{C}=\text { Capacitance in picofarads } \\
& \mathrm{K}=\text { Dielectric constant } \\
& \mathrm{A}=\text { Area of one plate in square centimeters } \\
& \mathrm{A}^{\prime}=\text { Area of one plate in square inches } \\
& \mathrm{d}=\text { Thickness in centimeters } \\
& \mathrm{d}^{\prime}=\text { Thickness in inches } \\
& \mathrm{n}=\text { Number of plates }
\end{aligned}
$$

### 1.6 Inductor sizing equation

$\mathrm{L}=\frac{\mathrm{N}^{2} \mu \mathrm{~A}}{1}$
$\mu=\mu_{\mathrm{r}} \mu_{0}$

Where,

$$
\begin{aligned}
\mathrm{L} & =\text { Inductance of coil in Henrys } \\
\mathrm{N} & =\text { Number of turns in wire coil (straight wire }=1 \text { ) } \\
\mu & =\text { Permeability of core material (absolute, not relative) } \\
\mu_{\mathrm{r}} & =\text { Relative permeability, dimensionless ( } \mu_{0}=1 \text { for air) } \\
\mu_{0} & =1.26 \times 10^{-6} \mathrm{~T}-\mathrm{m} / \mathrm{At} \text { permeability of free space } \\
\mathrm{A} & =\text { Area of coil in square meters } \\
\mathrm{l} & =\text { Average length of coil in meters }
\end{aligned}
$$

Wheeler's formulas for inductance of air core coils which follow are usefull for radio frequency inductors. The following formula for the inductance of a single layer air core solenoid coil is accurate to approximately $1 \%$ for $2 \mathrm{r} / \mathrm{l}<3$. The thick coil formula is $1 \%$ accurate when the denominator terms are approximately equal. Wheeler's spiral formula is $1 \%$ accurate for $\mathrm{c}>0.2 \mathrm{r}$. While this is a "round wire" formula, it may still be applicable to printed circuit spiral inductors at reduced accuracy.

$L=\frac{N^{2} r^{2}}{9 r+10 \cdot 1}$

Where,

$$
\mathrm{L}=\text { Inductance of coil in microhenrys }
$$

$\mathrm{N}=$ Number of turns of wire
$r=$ Mean radius of coil in inches
I = Length of coil in inches
$c=$ Thickness of coil in inches

The wire table provides "turns per inch" for enamel magnet wire for use with the inductance formulas for coils.

| AWG <br> gauge <br> turns <br> inch | AWG <br> gauge | turns <br> inch | AWG <br> gauge <br> tnch | turn <br> gauge | turns <br> inch |  |  |
| :--- | :---: | :--- | :---: | :--- | :--- | :--- | :--- |
| 10 | 9.6 | 20 | 29.4 | 30 | 90.5 | 40 | 282 |
| 11 | 10.7 | 21 | 33.1 | 31 | 101 | 41 | 327 |
| 12 | 12.0 | 22 | 37.0 | 32 | 113 | 42 | 378 |
| 13 | 13.5 | 23 | 41.3 | 33 | 127 | 43 | 421 |
| 14 | 15.0 | 24 | 46.3 | 34 | 143 | 44 | 471 |
| 15 | 16.8 | 25 | 51.7 | 35 | 158 | 45 | 523 |
| 16 | 18.9 | 26 | 58.0 | 36 | 175 | 46 | 581 |
| 17 | 21.2 | 27 | 64.9 | 37 | 198 |  |  |
| 18 | 23.6 | 28 | 72.7 | 38 | 224 |  |  |
| 19 | 26.4 | 29 | 81.6 | 39 | 248 |  |  |

### 1.7 Time constant equations

### 1.7.1 Value of time constant in series RC and RL circuits

Time constant in seconds $=\mathrm{RC}$
Time constant in seconds $=\mathrm{L} / \mathrm{R}$

### 1.7.2 Calculating voltage or current at specified time

## Universal Time Constant Formula

Change $=($ Final-Start $)\left(1-\frac{1}{e^{\mathrm{t} / \tau}}\right)$
Where,

$$
\left.\begin{array}{rl}
\text { Final } & =\text { Value of calculated variable after infinite time } \\
& \text { (its ultimate value) }
\end{array}\right\} \begin{aligned}
\text { Start } & =\text { Initial value of calculated variable } \\
e & =\text { Euler's number }(\approx 2.7182818) \\
\mathrm{t} & =\text { Time in seconds } \\
\tau & =\text { Time constant for circuit in seconds }
\end{aligned}
$$

1.7.3 Calculating time at specified voltage or current

$$
\mathrm{t}=\tau\left(\ln \frac{1}{1-\frac{\text { Change }}{\text { Final }- \text { Start }}}\right)
$$

### 1.8 AC circuit equations

### 1.8.1 Inductive reactance

$\mathrm{X}_{\mathrm{L}}=2 \pi \mathrm{fL}$
Where,
$\mathrm{X}_{\mathrm{L}}=$ Inductive reactance in ohms
$\mathrm{f}=$ Frequency in hertz
$\mathrm{L}=$ Inductance in henrys

### 1.8.2 Capacitive reactance

$\mathrm{X}_{\mathrm{C}}=\frac{1}{2 \pi \mathrm{fC}}$
Where,
$\mathrm{X}_{\mathrm{C}}=$ Inductive reactance in ohms
$\mathrm{f}=$ Frequency in hertz
C = Capacitance in farads

### 1.8.3 Impedance in relation to R and X

$$
\begin{aligned}
& \mathrm{Z}_{L}=\mathrm{R}+\mathrm{j} \mathrm{X}_{L} \\
& \mathrm{Z}_{C}=\mathrm{R}-\mathrm{j} \mathrm{X}_{C}
\end{aligned}
$$

### 1.8.4 Ohm's Law for AC

$$
\begin{aligned}
& \mathrm{E}=\mathrm{IZ} \quad \mathrm{I}=\frac{\mathrm{E}}{\mathrm{Z}} \quad \mathrm{Z}=\frac{\mathrm{E}}{\mathrm{I}} \\
& \text { Where, } \\
& \mathrm{E}=\text { Voltage in volts } \\
& \mathrm{I}=\text { Current in amperes (amps) } \\
& \mathrm{Z}=\text { Impedance in ohms }
\end{aligned}
$$

### 1.8.5 Series and Parallel Impedances

$$
\begin{aligned}
& \mathrm{Z}_{\text {series }}=\mathrm{Z}_{1}+\mathrm{Z}_{2}+\ldots \mathrm{Z}_{n} \\
& \mathrm{Z}_{\text {parallel }}=\frac{1}{\frac{1}{\mathrm{Z}_{1}}+\frac{1}{\mathrm{Z}_{2}}+\ldots \frac{1}{\mathrm{Z}_{n}}}
\end{aligned}
$$

NOTE: All impedances must be calculated in complex number form for these equations to work.

### 1.8.6 Resonance

$$
\mathrm{f}_{\text {resonant }}=\frac{1}{2 \pi \sqrt{\mathrm{LC}}}
$$

NOTE: This equation applies to a non-resistive LC circuit. In circuits containing resistance as well as inductance and capacitance, this equation applies only to series configurations and to parallel configurations where R is very small.

### 1.8.7 AC power

$$
\begin{gathered}
\mathbf{P}=\text { true power } \quad \mathrm{P}=\mathrm{I}^{2} \mathrm{R} \quad \mathrm{P}=\frac{\mathrm{E}^{2}}{\mathrm{R}} \\
\text { Measured in units of Watts }
\end{gathered}
$$

$$
\mathrm{Q}=\text { reactive power } \quad \mathrm{Q}=\mathrm{I}^{2} \mathrm{X} \quad \mathrm{Q}=\frac{\mathrm{E}^{2}}{\mathrm{X}}
$$

Measured in units of Volt-Amps-Reactive (VAR)

$$
\begin{gathered}
\mathbf{S}=\text { apparent power } \quad \mathrm{S}=\mathrm{I}^{2} \mathrm{Z} \quad \mathrm{~S}=\frac{\mathrm{E}^{2}}{\mathrm{Z}} \quad \mathrm{~S}=\mathrm{IE} \\
\text { Measured in units of Volt-Amps }
\end{gathered}
$$

$\mathrm{P}=(\mathrm{IE})($ power factor $)$

$$
\mathrm{S}=\sqrt{\mathrm{P}^{2}+\mathrm{Q}^{2}}
$$

Power factor $=\cos (\mathrm{Z}$ phase angle $)$

### 1.9 Decibels

$\mathrm{A}_{\mathrm{V}(\mathrm{dB})}=20 \log \mathrm{~A}_{\mathrm{V} \text { (ratio) }}$
$\mathrm{A}_{\mathrm{I}(\mathrm{dB})}=20 \log \mathrm{~A}_{\mathrm{I} \text { (ratio) }}$
$\mathrm{A}_{\mathrm{P}(\mathrm{dB})}=10 \log \mathrm{~A}_{\mathrm{P}(\text { ratio })}$

$$
A_{V(\text { ratio })}=10^{\frac{\mathrm{A}_{\mathrm{V}(\mathrm{BB})}}{20}}
$$

$$
\mathrm{A}_{\mathrm{I}(\text { ratio })}=10^{\frac{\mathrm{A}_{\mathrm{I}(\mathrm{BB})}}{20}}
$$

$$
A_{P(\text { ratio })}=10^{\frac{\mathrm{A}_{\mathrm{P}(\mathrm{~dB})}}{10}}
$$

### 1.10 Metric prefixes and unit conversions

- Metric prefixes
- Yotta $=10^{24}$ Symbol: Y
- Zetta $=10^{21}$ Symbol: Z
- $\mathrm{Exa}=10^{18}$ Symbol: E
- Peta $=10^{15}$ Symbol: P
- Tera $=10^{12}$ Symbol: T
- Giga $=10^{9}$ Symbol: G
- $\mathrm{Mega}=10^{6}$ Symbol: M
- Kilo $=10^{3}$ Symbol: k
- Hecto $=10^{2}$ Symbol: h
- Deca $=10^{1}$ Symbol: da
- Deci $=10^{-1}$ Symbol: d
- Centi $=10^{-2}$ Symbol: c
- Milli $=10^{-3}$ Symbol: m
- Micro $=10^{-6}$ Symbol: $\mu$
- Nano $=10^{-9}$ Symbol: n
- Pico $=10^{-12}$ Symbol: p
- Femto $=10^{-15}$ Symbol: f
- Atto $=10^{-18}$ Symbol: a
- Zepto $=10^{-21}$ Symbol: z
- Yocto $=10^{-24}$ Symbol: y

METRIC PREFIX SCALE


- Conversion factors for temperature
- ${ }^{\circ} \mathrm{F}=\left({ }^{\circ} \mathrm{C}\right)(9 / 5)+32$
- ${ }^{\circ} \mathrm{C}=\left({ }^{\circ} \mathrm{F}-32\right)(5 / 9)$
- ${ }^{\circ} \mathrm{R}={ }^{\circ} \mathrm{F}+459.67$
- ${ }^{\circ} \mathrm{K}={ }^{\circ} \mathrm{C}+273.15$


## Conversion equivalencies for volume

1 US gallon $($ gal $)=231.0$ cubic inches $\left(\mathrm{in}^{3}\right)=4$ quarts $(\mathrm{qt})=8$ pints $(\mathrm{pt})=128$ fluid ounces (fl. oz.) $=3.7854$ liters ( 1 )

1 Imperial gallon (gal) $=160$ fluid ounces (fl. oz.) $=4.546$ liters ( 1 )

## Conversion equivalencies for distance

1 inch (in) $=2.540000$ centimeter $(\mathrm{cm})$

## Conversion equivalencies for velocity

1 mile per hour $(\mathrm{mi} / \mathrm{h})=88$ feet per minute $(\mathrm{ft} / \mathrm{m})=1.46667$ feet per second $(\mathrm{ft} / \mathrm{s})$ $=1.60934$ kilometer per hour $(\mathrm{km} / \mathrm{h})=0.44704$ meter per second $(\mathrm{m} / \mathrm{s})=0.868976$ knot (knot - international)

## Conversion equivalencies for weight

1 pound $(\mathrm{lb})=16$ ounces $(\mathrm{oz})=0.45359$ kilogram ( kg )

## Conversion equivalencies for force

1 pound-force $(\mathrm{lbf})=4.44822$ newton $(\mathrm{N})$

## Acceleration of gravity (free fall), Earth standard

9.806650 meters per second per second $\left(\mathrm{m} / \mathrm{s}^{2}\right)=32.1740$ feet per second per second (ft/s ${ }^{2}$ )

## Conversion equivalencies for area

1 acre $=43560$ square feet $\left(\mathrm{ft}^{2}\right)=4840$ square yards $\left(\mathrm{yd}^{2}\right)=4046.86$ square meters ( $\mathrm{m}^{2}$ )

## Conversion equivalencies for pressure

1 pound per square inch $(\mathrm{psi})=2.03603$ inches of mercury $(\mathrm{in} . \mathrm{Hg})=27.6807$ inches of water (in. W.C.) $=6894.757$ pascals $(\mathrm{Pa})=0.0680460$ atmospheres $($ Atm $)=$ 0.0689476 bar (bar)

## Conversion equivalencies for energy or work

1 british thermal unit (BTU - "International Table") $=251.996$ calories (cal - "International Table" $)=1055.06$ joules $(\mathrm{J})=1055.06$ watt-seconds $(\mathrm{W}-\mathrm{s})=0.293071$ watthour $(\mathrm{W}-\mathrm{hr})=1.05506 \times 10^{10} \operatorname{ergs}(\mathrm{erg})=778.169$ foot-pound-force $(\mathrm{ft}-\mathrm{lbf})$

## Conversion equivalencies for power

1 horsepower ( $\mathrm{hp}-550 \mathrm{ft}-\mathrm{lbf} / \mathrm{s})=745.7$ watts $(\mathrm{W})=2544.43$ british thermal units per hour $(\mathrm{BTU} / \mathrm{hr})=0.0760181$ boiler horsepower (hp - boiler)

## Conversion equivalencies for motor torque

|  | Newton-meter <br> $(\mathrm{n}-\mathrm{m})$ | Gram-centimeter <br> $(\mathrm{g}-\mathrm{cm})$ | Pound-inch <br> $(\mathrm{lb}-\mathrm{in})$ | Pound-foot <br> $(\mathrm{lb}-\mathrm{ft})$ | Ounce-inch <br> $(\mathrm{oz}-\mathrm{in})$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{n}-\mathrm{m}$ | 1 | 1020 | 8.85 | 0.738 | 141.6 |
| $\mathrm{~g}-\mathrm{cm}$ | $981 \times 10^{-6}$ | 1 | $8.68 \times 10^{-3}$ | $723 \times 10^{-6}$ | 0.139 |
| $\mathrm{lb}-\mathrm{in}$ | 0.113 | 115 | 1 | 0.0833 | 16 |
| $\mathrm{lb}-\mathrm{ft}$ | 1.36 | 1383 | 12 | 1 | 192 |
| $\mathrm{oz}-\mathrm{in}$ | $7.062 \times 10^{-3}$ | 7.20 | 0.0625 | $5.21 \times 10^{-3}$ | 1 |

Locate the row corresponding to known unit of torque along the left of the table. Multiply by the factor under the column for the desired units. For example, to convert 2 oz-in torque to $n-m$, locate oz-in row at table left. Locate $7.062 \times 10^{-3}$ at intersection of desired n-m units column. Multiply 2 oz-in $\times\left(7.062 \times 10^{-3}\right)=14.12 \times 10^{-3} \mathrm{n}-\mathrm{m}$.

Converting between units is easy if you have a set of equivalencies to work with. Suppose we wanted to convert an energy quantity of 2500 calories into watt-hours. What we would need to do is find a set of equivalent figures for those units. In our reference here, we see that 251.996 calories is physically equal to 0.293071 watt hour. To convert from calories into watt-hours, we must form a "unity fraction" with these physically equal figures (a fraction composed of different figures and different units, the numerator and denominator being physically equal to one another), placing the desired unit in the numerator and the initial unit in the denominator, and then multiply our initial value of calories by that fraction.

Since both terms of the "unity fraction" are physically equal to one another, the fraction as a whole has a physical value of 1 , and so does not change the true value of any figure when multiplied
by it. When units are canceled, however, there will be a change in units. For example, 2500 calories multiplied by the unity fraction of $(0.293071 \mathrm{w}-\mathrm{hr} / 251.996 \mathrm{cal})=2.9075$ watt-hours.

$$
\text { Original figure } \quad 2500 \text { calories }
$$

"Unity fraction" $\frac{0.293071 \text { watt-hour }}{251.996 \text { calories }}$
. . . cancelling units . . .


Converted figure 2.9075 watt-hours

The "unity fraction" approach to unit conversion may be extended beyond single steps. Suppose we wanted to convert a fluid flow measurement of 175 gallons per hour into liters per day. We have two units to convert here: gallons into liters, and hours into days. Remember that the word "per" in mathematics means "divided by," so our initial figure of 175 gallons per hour means 175 gallons divided by hours. Expressing our original figure as such a fraction, we multiply it by the necessary unity fractions to convert gallons to liters ( 3.7854 liters $=1$ gallon), and hours to days ( 1 day $=24$ hours). The units must be arranged in the unity fraction in such a way that undesired units cancel each other out above and below fraction bars. For this problem it means using a gallons-to-liters unity fraction of (3.7854 liters / 1 gallon) and a hours-to-days unity fraction of ( 24 hours / 1 day):

"Unity fraction" $\frac{3.7854 \text { liters }}{1 \text { gallon }}$
"Unity fraction" $\frac{24 \text { hours }}{1 \text { day }}$
. . . cancelling units . . .
$\frac{175 \text { gallons }}{1 \text { hour }} \frac{3.7854 \text { liters }}{1 \text { gałłon }} \quad \frac{24 \text { hours }}{1 \text { day }}$

Converted figure $15,898.68$ liters/day
Our final (converted) answer is 15898.68 liters per day.

### 1.11 Data

Conversion factors were found in the $78^{\text {th }}$ edition of the CRC Handbook of Chemistry and Physics, and the $3^{\text {rd }}$ edition of Bela Liptak's Instrument Engineers' Handbook - Process Measurement and Analysis.

### 1.12 Contributors

Contributors to this chapter are listed in chronological order of their contributions, from most recent to first. See Appendix 2 (Contributor List) for dates and contact information.

Gerald Gardner (January 2003): Addition of Imperial gallons conversion.

## Chapter 2

## RESISTOR COLOR CODES

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| Color | Digit | Multiplier | Tolerance (\%) |
| :--- | :---: | :---: | :---: |
| Black | 0 | $10^{0}(1)$ |  |
| Brown | 1 | $10^{1}$ | 1 |
| Red | 2 | $10^{2}$ | 2 |
| Orange | 3 | $10^{3}$ |  |
| Yellow | 4 | $10^{4}$ |  |
| Green | 5 | $10^{5}$ | 0.5 |
| Blue | 6 | $10^{6}$ | 0.25 |
| Violet | 7 | $10^{7}$ | 0.1 |
| Grey | 8 | $10^{8}$ |  |
| White | 9 | $10^{9}$ |  |
| Gold |  | $10^{-1}$ | 5 |
| Silver |  | $10^{-2}$ | 10 |
| (none) |  |  | 20 |

The colors brown, red, green, blue, and violet are used as tolerance codes on 5 -band resistors only. All 5 -band resistors use a colored tolerance band. The blank ( $20 \%$ ) "band" is only used with the "4-band" code ( 3 colored bands + a blank "band").


### 2.1 Example \#1



A resistor colored Yellow-Violet-Orange-Gold would be $47 \mathrm{k} \Omega$ with a tolerance of $+/-5 \%$.

### 2.2 Example \#2



A resistor colored Green-Red-Gold-Silver would be $5.2 \Omega$ with a tolerance of $+/-10 \%$.

### 2.3 Example \#3



A resistor colored White-Violet-Black would be $97 \Omega$ with a tolerance of $+/-20 \%$. When you see only three color bands on a resistor, you know that it is actually a 4 -band code with a blank (20\%) tolerance band.

### 2.4 Example \#4



A resistor colored Orange-Orange-Black-Brown-Violet would be $3.3 \mathrm{k} \Omega$ with a tolerance of $+/-$ $0.1 \%$.

### 2.5 Example \#5



A resistor colored Brown-Green-Grey-Silver-Red would be $1.58 \Omega$ with a tolerance of $+/-2 \%$.

### 2.6 Example \#6



A resistor colored Blue-Brown-Green-Silver-Blue would be $6.15 \Omega$ with a tolerance of $+/-0.25 \%$.

## Chapter 3

## CONDUCTOR AND INSULATOR TABLES

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### 3.1 Copper wire gage table

Soild copper wire table:

| Size <br> AWG | Diameter <br> inches | Cross-sectional area <br> cir. mils <br> sq. <br> s. | Weight <br> inches |
| :--- | :---: | :---: | :---: | :---: | :---: |
| lb/1000 ft |  |  |  |



### 3.2 Copper wire ampacity table

Ampacities of copper wire, in free air at $30^{\circ} \mathrm{C}$ :

| INSULATION TYPE: |  |  |
| :---: | :---: | :---: |
| RUW, T | THW, THWN | FEP, FEPB |
| TW | RUH | THHN, XHHW |


| $\begin{aligned} & \text { Size } \\ & \text { AWG } \end{aligned}$ | Current Rating <br> @ 60 degrees C | Current Ratin © 75 degrees | Current Rating |
| :---: | :---: | :---: | :---: |
| 20 -------- *9 ------------------------------ *12.5 |  |  |  |
|  |  |  |  |
| 18 -------- *13 --------------------------------18 18 |  |  |  |
| 16 -------- *18 |  |  |  |
| 14 --------- 25 -------------- 30 -------------- 35 |  |  |  |
| 12 --------- 30 -------------- 35 -------------- 40 |  |  |  |
| 10 --------- 40 -------------- 50 -------------- 55 |  |  |  |
| 8 ---------- 60 -------------- 70 ---------------80 |  |  |  |
| 6 ---------- 80 -------------- 95 -------------105 |  |  |  |
| 4 --------- 105 ------------- 125 ------------- 140 |  |  |  |
| 2 --------- 140 ------------- 170 ------------- 190 |  |  |  |
| 1 --------- 165 ------------- 195 ------------- 220 |  |  |  |
| 1/0 ------- 195 ------------- 230 ------------ 260 |  |  |  |
| 2/0 ------- 225 ------------- 265 ------------ 300 |  |  |  |
| 3/0 ------- 260 ------------- 310 ------------- 350 |  |  |  |
| 4/0 ------- 300 ------------- 360 ------------- 405 |  |  |  |

* $=$ estimated values; normally, wire gages this small are not manufactured with these insulation types.


### 3.3 Coefficients of specific resistance

Specific resistance at $20^{\circ} \mathrm{C}$ :

| Material Element/Alloy | (ohm-cmil/ft) | (ohm-cm) |
| :---: | :---: | :---: |
| Nichrome ------- Alloy | - 675 | $112.2^{-6}$ |
| Nichrome V ----- Alloy | 650 | $108.1^{-6}$ |
| Manganin ------- Alloy | 290 | $48.21{ }^{-6}$ |
| Constantan ----- Alloy | 272.97 | $45.38^{-6}$ |
| Steel* --------- Alloy | 100 | $16.62^{-6}$ |
| Platinum ------ Element | - 63.16 | $10.5^{-6}$ |
| Iron ---------- Element | - 57.81 | $9.61{ }^{-6}$ |
| Nickel -------- Element | - 41.69 | $6.93{ }^{-6}$ |
| Zinc ---------- Element | - 35.49 | $5.90{ }^{-6}$ |
| Molybdenum ---- Element | - 32.12 | $5.34{ }^{-6}$ |
| Tungsten ------ Element | - 31.76 | $5.28{ }^{-6}$ |
| Aluminum ------ Element | - 15.94 | $2.650^{-6}$ |
| Gold ---------- Element | - 13.32 | $2.214^{-6}$ |
| Copper -------- Element | - 10.09 | $1.678^{-6}$ |
| Silver -------- Element | - 9.546 - | $1.587^{-6}$ |

$*=$ Steel alloy at 99.5 percent iron, 0.5 percent carbon.

### 3.4 Temperature coefficients of resistance

Temperature coefficient ( $\alpha$ ) per degree C:

| Material | Element/Alloy | Temp. coefficient |
| :---: | :---: | :---: |
| Nickel -------- Element --------------- 0.005866 |  |  |
| Iron | - Element | --- 0.005671 |
| Molybdenum | -- Element | 0.004579 |
| Tungsten | Element | 0.004403 |
| Aluminum | Element | 0.004308 |
| Copper | - Element | - 0.004041 |
| Silver | -- Element | - 0.003819 |
| Platinum | -- Element | -- 0.003729 |
| old | Element | 0.003715 |
| Zinc | Element | 0.003847 |
| Steel* | - Alloy | 0.003 |
| Nichrome | --- Alloy | 0.00017 |
| Nichrome V | --- Alloy | 0.00013 |
|  |  |  |
|  |  |  |

* $=$ Steel alloy at 99.5 percent iron, 0.5 percent carbon


### 3.5 Critical temperatures for superconductors



Note: all critical temperatures given at zero magnetic field strength.

### 3.6 Dielectric strengths for insulators

```
Dielectric strength in kilovolts per inch (kV/in):
Material* Dielectric strength
==========================================
Vacuum ---------------------- }2
Air ------------------------- }20\mathrm{ to }7
Porcelain ------------------- }40\mathrm{ to 200
Paraffin Wax --------------- 200 to 300
Transformer Oil ------------- }40
Bakelite --------------------- }300\mathrm{ to }55
Rubber ----------------------- }450\mathrm{ to }70
Shellac ---------------------}90
Paper ------------------------}125
Teflon ----------------------}150
Glass ---------------------- }2000\mathrm{ to }300
Mica -------------------------}500
```

* = Materials listed are specially prepared for electrical use


### 3.7 Data

Tables of specific resistance and temperature coefficient of resistance for elemental materials (not alloys) were derived from figures found in the 78th edition of the CRC Handbook of Chemistry and Physics. Superconductivity data from Collier's Encyclopedia (volume 21, 1968, page 640).

## Chapter 4

## ALGEBRA REFERENCE

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### 4.1 Basic identities

$$
\begin{array}{ccc}
\mathrm{a}+0=\mathrm{a} & 1 \mathrm{a}=\mathrm{a} & 0 \mathrm{a}=0 \\
\frac{\mathrm{a}}{1}=\mathrm{a} & \frac{0}{\mathrm{a}}=0 & \frac{\mathrm{a}}{\mathrm{a}}=1 \\
& \frac{\mathrm{a}}{0}=\text { undefined } &
\end{array}
$$

Note: while division by zero is popularly thought to be equal to infinity, this is not technically true. In some practical applications it may be helpful to think the result of such a fraction approaching infinity as the denominator approaches zero (imagine calculating current $\mathrm{I}=\mathrm{E} / \mathrm{R}$ in a circuit with resistance approaching zero - current would approach infinity), but the actual fraction of anything divided by zero is undefined in the scope of "real" numbers.

### 4.2 Arithmetic properties

### 4.2.1 The associative property

In addition and multiplication, terms may be arbitrarily associated with each other through the use of parentheses:

$$
\mathrm{a}+(\mathrm{b}+\mathrm{c})=(\mathrm{a}+\mathrm{b})+\mathrm{c} \quad \mathrm{a}(\mathrm{bc})=(\mathrm{ab}) \mathrm{c}
$$

### 4.2.2 The commutative property

In addition and multiplication, terms may be arbitrarily interchanged, or commutated:

$$
a+b=b+a \quad a b=b a
$$

### 4.2.3 The distributive property

$a(b+c)=a b+a c$

### 4.3 Properties of exponents

$$
\begin{array}{ll}
a^{m} a^{n}=a^{m+n} & (a b)^{m}=a^{m} b^{m} \\
\left(a^{m}\right)^{n}=a^{m n} & \frac{a^{m}}{a^{n}}=a^{m-n}
\end{array}
$$

### 4.4 Radicals

### 4.4.1 Definition of a radical

When people talk of a "square root," they're referring to a radical with a root of 2 . This is mathematically equivalent to a number raised to the power of $1 / 2$. This equivalence is useful to know when using a calculator to determine a strange root. Suppose for example you needed to find the fourth root of a number, but your calculator lacks a " 4 th root" button or function. If it has a $\mathrm{y}^{x}$ function (which any scientific calculator should have), you can find the fourth root by raising that number to the $1 / 4$ power, or $\mathrm{x}^{0.25}$.

$$
\sqrt[x]{a}=a^{1 / x}
$$

It is important to remember that when solving for an even root (square root, fourth root, etc.) of any number, there are two valid answers. For example, most people know that the square root of nine is three, but negative three is also a valid answer, since $(-3)^{2}=9$ just as $3^{2}=9$.

### 4.4.2 Properties of radicals

$$
\sqrt[x]{a}^{x}=a \quad \sqrt[x]{a}_{a^{x}}^{x}=a
$$

$$
\sqrt[x]{a b}=\sqrt[x]{a} \sqrt[x]{b}
$$

$$
\sqrt[x]{\frac{a}{b}}=\frac{\sqrt[x]{a}}{\sqrt[x]{b}}
$$

### 4.5 Important constants

### 4.5.1 Euler's number

Euler's constant is an important value for exponential functions, especially scientific applications involving decay (such as the decay of a radioactive substance). It is especially important in calculus due to its uniquely self-similar properties of integration and differentiation.

```
e approximately equals:
2.71828 18284 59045 23536 02874 71352662497757247093 69996
```

$$
\begin{aligned}
& \mathrm{e}=\sum_{\mathrm{k}=0}^{\infty} \frac{1}{\mathrm{k}!} \\
& \frac{1}{0!}+\frac{1}{1!}+\frac{1}{2!}+\frac{1}{3!}+\cdots \frac{1}{n!}
\end{aligned}
$$

### 4.5.2 Pi

$\operatorname{Pi}(\pi)$ is defined as the ratio of a circle's circumference to its diameter.
Pi approximately equals:
3.14159265358979323846264338327950288419716939937511

Note: For both Euler's constant $(e)$ and pi $(\pi)$, the spaces shown between each set of five digits have no mathematical significance. They are placed there just to make it easier for your eyes to "piece" the number into five-digit groups when manually copying.

### 4.6 Logarithms

### 4.6.1 Definition of a logarithm

$$
\begin{aligned}
& \text { If: } \\
& \mathrm{b}^{\mathrm{y}}=\mathrm{x}
\end{aligned}
$$

Then:
$\log _{\mathrm{b}} \mathrm{x}=\mathrm{y}$

Where,
$\mathrm{b}=$ "Base" of the logarithm
"log" denotes a common logarithm (base $=10$ ), while "ln" denotes a natural logarithm (base $=$ e).

### 4.6.2 Properties of logarithms

$(\log a)+(\log b)=\log a b$
$(\log a)-(\log b)=\log \frac{a}{b}$
$\log a^{m}=(m)(\log a)$
$\mathrm{a}^{(\log \mathrm{m})}=\mathrm{m}$
These properties of logarithms come in handy for performing complex multiplication and division operations. They are an example of something called a transform function, whereby one type of mathematical operation is transformed into another type of mathematical operation that is simpler to solve. Using a table of logarithm figures, one can multiply or divide numbers by adding or subtracting their logarithms, respectively. then looking up that logarithm figure in the table and seeing what the final product or quotient is.

Slide rules work on this principle of logarithms by performing multiplication and division through addition and subtraction of distances on the slide.


Marks on a slide rule's scales are spaced in a logarithmic fashion, so that a linear positioning of the scale or cursor results in a nonlinear indication as read on the scale(s). Adding or subtracting lengths on these logarithmic scales results in an indication equivalent to the product or quotient, respectively, of those lengths.

Most slide rules were also equipped with special scales for trigonometric functions, powers, roots, and other useful arithmetic functions.

### 4.7 Factoring equivalencies

$$
x^{2}-y^{2}=(x+y)(x-y)
$$

$$
x^{3}-y^{3}=(x-y)\left(x^{2}+x y+y^{2}\right)
$$

### 4.8 The quadratic formula

For a polynomial expression in
the form of: $a^{2}+b x+c=0$

$$
\mathrm{x}=\frac{-\mathrm{b} \pm \sqrt{\mathrm{b}^{2}-4 \mathrm{ac}}}{2 \mathrm{a}}
$$

### 4.9 Sequences

### 4.9.1 Arithmetic sequences

An arithmetic sequence is a series of numbers obtained by adding (or subtracting) the same value with each step. A child's counting sequence ( $1,2,3,4, \ldots$ ) is a simple arithmetic sequence, where the common difference is 1 : that is, each adjacent number in the sequence differs by a value of one. An arithmetic sequence counting only even numbers ( $2,4,6,8, \ldots$ ) or only odd numbers ( $1,3,5$, $7,9, \ldots$.) would have a common difference of 2 .

In the standard notation of sequences, a lower-case letter "a" represents an element (a single number) in the sequence. The term " $\mathrm{a}_{n}$ " refers to the element at the $\mathrm{n}^{\text {th }}$ step in the sequence. For example, " $a_{3}$ " in an even-counting (common difference $=2$ ) arithmetic sequence starting at 2 would be the number 6 , "a" representing 4 and " $a_{1}$ " representing the starting point of the sequence (given in this example as 2 ).

A capital letter "A" represents the sum of an arithmetic sequence. For instance, in the same even-counting sequence starting at $2, \mathrm{~A}_{4}$ is equal to the sum of all elements from $\mathrm{a}_{1}$ through $\mathrm{a}_{4}$, which of course would be $2+4+6+8$, or 20 .

$$
\mathrm{a}_{\mathrm{n}}=\mathrm{a}_{\mathrm{n}-1}+\mathrm{d} \quad \mathrm{a}_{\mathrm{n}}=\mathrm{a}_{1}+\mathrm{d}(\mathrm{n}-1)
$$

## Where:

$$
\mathrm{d}=\text { The "common difference" }
$$

## Example of an arithmetic sequence:

$$
-7,-3,1,5,9,13,17,21,25 \ldots
$$

$\mathrm{A}_{\mathrm{n}}=\mathrm{a}_{1}+\mathrm{a}_{2}+\ldots \mathrm{a}_{n}$
$\mathrm{A}_{\mathrm{n}}=\frac{\mathrm{n}}{2}\left(\mathrm{a}_{1}+\mathrm{a}_{\mathrm{n}}\right)$

### 4.9.2 Geometric sequences

A geometric sequence, on the other hand, is a series of numbers obtained by multiplying (or dividing) by the same value with each step. A binary place-weight sequence ( $1,2,4,8,16,32,64, \ldots$. $)$ is a simple geometric sequence, where the common ratio is 2 : that is, each adjacent number in the sequence differs by a factor of two.

$$
\mathrm{a}_{\mathrm{n}}=\mathrm{r}\left(\mathrm{a}_{\mathrm{n}-1}\right) \quad \mathrm{a}_{\mathrm{n}}=\mathrm{a}_{1}\left(\mathrm{r}^{\mathrm{n}-1}\right)
$$

Where:
$r=$ The "common ratio"

## Example of a geometric sequence:

3, 12, 48, 192, 768, $3072 \ldots$
$\mathrm{A}_{\mathrm{n}}=\mathrm{a}_{1}+\mathrm{a}_{2}+\ldots \mathrm{a}_{n}$
$A_{n}=\frac{a_{1}\left(1-r^{n}\right)}{1-r}$

### 4.10 Factorials

### 4.10.1 Definition of a factorial

Denoted by the symbol "!" after an integer; the product of that integer and all integers in descent to 1.

Example of a factorial:
$5!=5 \times 4 \times 3 \times 2 \times 1$
$5!=120$

### 4.10.2 Strange factorials

$0!=1 \quad 1!=1$

### 4.11 Solving simultaneous equations

The terms simultaneous equations and systems of equations refer to conditions where two or more unknown variables are related to each other through an equal number of equations. Consider the following example:

$$
x+y=24
$$

$2 x-y=-6$
For this set of equations, there is but a single combination of values for x and y that will satisfy both. Either equation, considered separately, has an infinitude of valid ( $\mathrm{x}, \mathrm{y}$ ) solutions, but together there is only one. Plotted on a graph, this condition becomes obvious:


Each line is actually a continuum of points representing possible x and y solution pairs for each equation. Each equation, separately, has an infinite number of ordered pair ( $\mathrm{x}, \mathrm{y}$ ) solutions. There is only one point where the two linear functions $\mathrm{x}+\mathrm{y}=24$ and $2 \mathrm{x}-\mathrm{y}=-6$ intersect (where one of their many independent solutions happen to work for both equations), and that is where x is equal to a value of 6 and y is equal to a value of 18 .

Usually, though, graphing is not a very efficient way to determine the simultaneous solution set for two or more equations. It is especially impractical for systems of three or more variables. In a three-variable system, for example, the solution would be found by the point intersection of three planes in a three-dimensional coordinate space - not an easy scenario to visualize.

### 4.11.1 Substitution method

Several algebraic techniques exist to solve simultaneous equations. Perhaps the easiest to comprehend is the substitution method. Take, for instance, our two-variable example problem:

$$
x+y=24
$$

$$
2 x-y=-6
$$

In the substitution method, we manipulate one of the equations such that one variable is defined in terms of the other:


## Defining y in terms of x

Then, we take this new definition of one variable and substitute it for the same variable in the other equation. In this case, we take the definition of $y$, which is $24-\mathrm{x}$ and substitute this for the y term found in the other equation:

$$
\mathrm{y}=24-\mathrm{x}
$$

substitute

$$
2 x-y=-6
$$


$2 \mathrm{x}-(24-\mathrm{x})=-6$

Now that we have an equation with just a single variable (x), we can solve it using "normal" algebraic techniques:

$2 \mathrm{x}-24+\mathrm{x}=-6$

$3 x-24=-6$

$3 \mathrm{x}=18$


$$
x=6
$$

Now that x is known, we can plug this value into any of the original equations and obtain a value for $y$. Or, to save us some work, we can plug this value (6) into the equation we just generated to define y in terms of x , being that it is already in a form to solve for y :


Applying the substitution method to systems of three or more variables involves a similar pattern, only with more work involved. This is generally true for any method of solution: the number of steps required for obtaining solutions increases rapidly with each additional variable in the system.

To solve for three unknown variables, we need at least three equations. Consider this example:

$$
\begin{array}{r}
x-y+z=10 \\
3 x+y+2 z=34 \\
-5 x+2 y-z=-14
\end{array}
$$

Being that the first equation has the simplest coefficients (1, -1 , and 1 , for $\mathrm{x}, \mathrm{y}$, and z , respectively), it seems logical to use it to develop a definition of one variable in terms of the other two. In this example, I'll solve for x in terms of y and z :

$$
\begin{aligned}
& \mathrm{x}-\mathrm{y}+\mathrm{z}=10 \\
& \square \text { Adding } \mathrm{y} \text { and subtracting } \mathrm{z} \\
& \text { from both sides }
\end{aligned}
$$

$$
x=y-z+10
$$

Now, we can substitute this definition of x where x appears in the other two equations:


Reducing these two equations to their simplest forms:
$3(\mathrm{y}-\mathrm{z}+10)+\mathrm{y}+2 \mathrm{z}=34 \quad-5(\mathrm{y}-\mathrm{z}+10)+2 \mathrm{y}-\mathrm{z}=-14$

Distributive property

$3 y-3 z+30+y+2 z=34$

$$
-5 y+5 z-50+2 y-z=-14
$$

Combining like terms

$$
4 y-z+30=34 \quad-3 y+4 z-50=-14
$$


Moving constant values to right

$4 y-z=4$
$-3 y+4 z=36$

So far, our efforts have reduced the system from three variables in three equations to two variables in two equations. Now, we can apply the substitution technique again to the two equations $4 y-z$ $=4$ and $-3 y+4 z=36$ to solve for either $y$ or $z$. First, I'll manipulate the first equation to define $z$ in terms of $y$ :
$4 y-z=4$
Adding z to both sides;
$\checkmark$ subtracting 4 from both sides

$$
z=4 y-4
$$

Next, we'll substitute this definition of $z$ in terms of $y$ where we see $z$ in the other equation:

$$
\begin{aligned}
& \downarrow \text { substitute } \\
& -3 \mathrm{y}+4 \mathrm{z}=36 \\
& \square \\
& -3 \mathrm{y}+4(4 \mathrm{y}-4)=36 \\
& \square \text { Distributive property } \\
& -3 \mathrm{y}+16 \mathrm{y}-16=36
\end{aligned}
$$

$\sqrt{7}$ Combining like terms
$13 y-16=36$
$\sqrt{7}$ Adding 16 to both sides
$13 \mathrm{y}=52$
$\sqrt{ }$ Dividing both sides by 13
$y=4$

Now that y is a known value, we can plug it into the equation defining z in terms of y and obtain a figure for z :


Now, with values for $y$ and $z$ known, we can plug these into the equation where we defined $x$ in terms of y and z , to obtain a value for x :


In closing, we've found values for $\mathrm{x}, \mathrm{y}$, and z of 2,4 , and 12 , respectively, that satisfy all three equations.

### 4.11.2 Addition method

While the substitution method may be the easiest to grasp on a conceptual level, there are other methods of solution available to us. One such method is the so-called addition method, whereby equations are added to one another for the purpose of canceling variable terms.

Let's take our two-variable system used to demonstrate the substitution method:

$$
x+y=24
$$

$2 x-y=-6$
One of the most-used rules of algebra is that you may perform any arithmetic operation you wish to an equation so long as you do it equally to both sides. With reference to addition, this means we may add any quantity we wish to both sides of an equation - so long as it's the same quantity without altering the truth of the equation.

An option we have, then, is to add the corresponding sides of the equations together to form a new equation. Since each equation is an expression of equality (the same quantity on either side of the $=$ sign), adding the left-hand side of one equation to the left-hand side of the other equation is valid so long as we add the two equations' right-hand sides together as well. In our example equation set, for instance, we may add $x+y$ to $2 x-y$, and add 24 and -6 together as well to form a new equation. What benefit does this hold for us? Examine what happens when we do this to our example equation set:

$$
\begin{gathered}
x+y=24 \\
+2 x-y=-6 \\
\hline 3 x+0=18
\end{gathered}
$$

Because the top equation happened to contain a positive y term while the bottom equation happened to contain a negative y term, these two terms canceled each other in the process of addition, leaving no y term in the sum. What we have left is a new equation, but one with only a single unknown variable, x ! This allows us to easily solve for the value of x :

$$
\begin{aligned}
& 3 \mathrm{x}+0=18 \\
& \leftrightarrows \text { Dropping the } 0 \text { term } \\
& 3 \mathrm{x}=18 \\
& \zeta \text { Dividing both sides by } 3 \\
& x=6
\end{aligned}
$$

Once we have a known value for $x$, of course, determining y's value is a simply matter of substitution (replacing $x$ with the number 6) into one of the original equations. In this example, the technique of adding the equations together worked well to produce an equation with a single unknown variable. What about an example where things aren't so simple? Consider the following equation set:

$$
\begin{array}{r}
2 x+2 y=14 \\
3 x+y=13
\end{array}
$$

We could add these two equations together - this being a completely valid algebraic operation but it would not profit us in the goal of obtaining values for x and y :

$$
\begin{array}{r}
2 x+2 y=14 \\
+\quad 3 x+y=13 \\
\hline 5 x+3 y=27
\end{array}
$$

The resulting equation still contains two unknown variables, just like the original equations do, and so we're no further along in obtaining a solution. However, what if we could manipulate one of the equations so as to have a negative term that would cancel the respective term in the other equation when added? Then, the system would reduce to a single equation with a single unknown variable just as with the last (fortuitous) example.

If we could only turn the $y$ term in the lower equation into $a-2 y$ term, so that when the two equations were added together, both y terms in the equations would cancel, leaving us with only an x term, this would bring us closer to a solution. Fortunately, this is not difficult to do. If we multiply each and every term of the lower equation by a -2 , it will produce the result we seek:

$$
\begin{aligned}
-2(3 \mathrm{x}+\mathrm{y}) & =-2(13) \\
& \text { Distributive property } \\
-6 \mathrm{x}-2 \mathrm{y} & =-26
\end{aligned}
$$

Now, we may add this new equation to the original, upper equation:

$$
\begin{array}{r}
2 x+2 y=14 \\
+-6 x-2 y=-26 \\
\hline-4 x+0 y=-12
\end{array}
$$

Solving for x , we obtain a value of 3 :

$$
-4 x+0 y=-12
$$

Dropping the 0 term

$$
-4 x=-12
$$

$\zeta$ Dividing both sides by -4

$$
x=3
$$

Substituting this new-found value for x into one of the original equations, the value of y is easily determined:

$$
\begin{aligned}
& \mathrm{x}=3 \\
& 2 \mathrm{x}+2 \mathrm{y}=14 \\
& \text { substitute } \\
& 6+2 \mathrm{y}=14 \\
& 2 \mathrm{y}=8 \\
& \mathrm{y}=4
\end{aligned}
$$

Using this solution technique on a three-variable system is a bit more complex. As with substitution, you must use this technique to reduce the three-equation system of three variables down to
two equations with two variables, then apply it again to obtain a single equation with one unknown variable. To demonstrate, I'll use the three-variable equation system from the substitution section:

$$
\begin{array}{r}
x-y+z=10 \\
3 x+y+2 z=34 \\
-5 x+2 y-z=-14
\end{array}
$$

Being that the top equation has coefficient values of 1 for each variable, it will be an easy equation to manipulate and use as a cancellation tool. For instance, if we wish to cancel the $3 x$ term from the middle equation, all we need to do is take the top equation, multiply each of its terms by -3 , then add it to the middle equation like this:

$$
\begin{aligned}
\mathrm{x}-\mathrm{y}+\mathrm{z} & =10 \\
-3(\mathrm{x}-\mathrm{y}+\mathrm{z}) & =-3(10) \\
\square & \text { Dultiply both sides by }-3 \\
-3 \mathrm{x}+3 \mathrm{y}-3 \mathrm{z} & =-30
\end{aligned}
$$

(Adding)

$$
\begin{gathered}
-3 x+3 y-3 z=-30 \\
+3 x+y+2 z=34 \\
\hline 0 x+4 y-z=4 \\
\text { or } \\
4 y-z=4
\end{gathered}
$$

We can rid the bottom equation of its $-5 x$ term in the same manner: take the original top equation, multiply each of its terms by 5 , then add that modified equation to the bottom equation, leaving a new equation with only y and $z$ terms:

$$
\begin{aligned}
& x-y+z=10 \\
& \checkmark \text { Multiply both sides by } 5 \\
& 5(\mathrm{x}-\mathrm{y}+\mathrm{z})=5(10) \\
& \checkmark \text { Distributive property } \\
& 5 x-5 y+5 z=50 \\
& \text { (Adding) } \\
& 5 x-5 y+5 z=50 \\
& \begin{array}{r}
+-5 x+2 y-z=-14 \\
\hline 0 x-3 y+4 z=36
\end{array} \\
& \text { or } \\
& -3 y+4 z=36
\end{aligned}
$$

At this point, we have two equations with the same two unknown variables, y and z :

$$
\begin{aligned}
4 y-z & =4 \\
-3 y+4 z & =36
\end{aligned}
$$

By inspection, it should be evident that the -z term of the upper equation could be leveraged to cancel the $4 z$ term in the lower equation if only we multiply each term of the upper equation by 4 and add the two equations together:

$$
\begin{aligned}
& 4 \mathrm{y}-\mathrm{z}=4 \\
& \longleftarrow \text { Multiply both sides by } 4 \\
& 4(4 y-z)=4(4) \\
& \sqrt{ } \text { Distributive property } \\
& 16 y-4 z=16 \\
& 16 y-4 z=16 \\
& \text { (Adding) } \\
& +\begin{array}{r}
-3 y+4 z=36 \\
\hline 13 y+0 z=52
\end{array} \\
& \text { or } \\
& 13 y=52
\end{aligned}
$$

Taking the new equation $13 y=52$ and solving for $y$ (by dividing both sides by 13), we get a value of 4 for $y$. Substituting this value of 4 for $y$ in either of the two-variable equations allows us to
solve for $z$. Substituting both values of $y$ and $z$ into any one of the original, three-variable equations allows us to solve for x . The final result (I'll spare you the algebraic steps, since you should be familiar with them by now!) is that $\mathrm{x}=2, \mathrm{y}=4$, and $\mathrm{z}=12$.

### 4.12 Contributors

Contributors to this chapter are listed in chronological order of their contributions, from most recent to first. See Appendix 2 (Contributor List) for dates and contact information.

Chirvasuta Constantin (April 2, 2003): Pointed out error in quadratic equation formula.

## Chapter 5

## TRIGONOMETRY REFERENCE

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### 5.1 Right triangle trigonometry



A right triangle is defined as having one angle precisely equal to $90^{\circ}$ (a right angle).

### 5.1.1 Trigonometric identities

$$
\begin{array}{lll}
\sin x=\frac{O}{H} & \cos x=\frac{A}{H} & \tan x=\frac{O}{A}
\end{array}
$$

H is the Hypotenuse, always being opposite the right angle. Relative to angle $\mathrm{x}, \mathrm{O}$ is the Opposite and A is the Adjacent.
"Arc" functions such as "arcsin", "arccos", and "arctan" are the complements of normal trigonometric functions. These functions return an angle for a ratio input. For example, if the tangent of $45^{\circ}$ is equal to 1 , then the "arctangent" (arctan) of 1 is $45^{\circ}$. "Arc" functions are useful for finding angles in a right triangle if the side lengths are known.

### 5.1.2 The Pythagorean theorem

$\mathrm{H}^{2}=\mathrm{A}^{2}+\mathrm{O}^{2}$

### 5.2 Non-right triangle trigonometry



### 5.2.1 The Law of Sines (for any triangle)

$\frac{\sin a}{A}=\frac{\sin b}{B}=\frac{\sin c}{C}$

### 5.2.2 The Law of Cosines (for any triangle)

$A^{2}=B^{2}+C^{2}-(2 B C)(\cos a)$
$B^{2}=A^{2}+C^{2}-(2 A C)(\cos b)$
$C^{2}=A^{2}+B^{2}-(2 A B)(\cos c)$

### 5.3 Trigonometric equivalencies

$$
\begin{array}{ll}
\sin -x=-\sin x & \cos -x=\cos x \\
\csc -t=-\csc t & \sec -t=\sec t \\
\sin 2 x=2(\sin x)(\cos x) & \cos 2 x=-t \cos t \\
\tan 2 t=\frac{2(\tan x)}{1-\tan ^{2} x} & \\
\sin ^{2} x=\frac{1}{2}-\frac{\cos 2 x}{2} & \cos ^{2} x=\frac{1}{2}+\frac{\cos 2 x}{2}
\end{array}
$$

### 5.4 Hyperbolic functions

$\sinh x=\frac{e^{x}-e^{-x}}{2}$
$\cosh \mathrm{x}=\frac{\mathrm{e}^{\mathrm{x}}+\mathrm{e}^{-\mathrm{x}}}{2}$
$\tanh \mathrm{x}=\frac{\sinh \mathrm{x}}{\cosh \mathrm{x}}$
Note: all angles (x) must be expressed in units of radians for these hyperbolic functions. There are $2 \pi$ radians in a circle $\left(360^{\circ}\right)$.

### 5.5 Contributors

Contributors to this chapter are listed in chronological order of their contributions, from most recent to first. See Appendix 2 (Contributor List) for dates and contact information.

Harvey Lew (??? 2003): Corrected typographical error: "tangent" should have been "cotangent".

## Chapter 6

## CALCULUS REFERENCE

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### 6.1 Rules for limits

$\lim _{\mathrm{x} \rightarrow \mathrm{a}}[f(\mathrm{x})+g(\mathrm{x})]=\lim _{\mathrm{x} \rightarrow \mathrm{a}} f(\mathrm{x})+\lim _{\mathrm{x} \rightarrow \mathrm{a}} g(\mathrm{x})$
$\lim _{\mathrm{x} \rightarrow \mathrm{a}}[f(\mathrm{x})-g(\mathrm{x})]=\lim _{\mathrm{x} \rightarrow \mathrm{a}} f(\mathrm{x})-\lim _{\mathrm{x} \rightarrow \mathrm{a}} g(\mathrm{x})$
$\left.\lim _{\mathrm{x} \rightarrow \mathrm{a}}[f(\mathrm{x}) g(\mathrm{x})]=\left[\lim _{\mathrm{x} \rightarrow \mathrm{a}} f(\mathrm{x})\right] \underset{\mathrm{x} \rightarrow \mathrm{a}}{\left[\lim _{\mathrm{a}}\right.} g(\mathrm{x})\right]$

### 6.2 Derivative of a constant

> If:
> $f(\mathrm{x})=\mathrm{c}$

Then:

$$
\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})=0
$$

(" $c$ " being a constant)

### 6.3 Common derivatives

$\frac{d}{d x} x^{n}=n x^{n-1}$
$\frac{\mathrm{d}}{\mathrm{dx}} \ln \mathrm{x}=\frac{1}{\mathrm{x}}$
$\frac{d}{d x} a^{x}=\left(a^{n}\right)(\ln a)$

### 6.4 Derivatives of power functions of $e$

If:
If:

$$
f(x)=\mathrm{e}^{g(x)}
$$

$$
f(x)=\mathrm{e}^{\mathrm{x}}
$$

Then:

$$
\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})=\mathrm{e}^{\mathrm{x}}
$$

Then:
$\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})=\mathrm{e}^{g(\mathrm{x})} \frac{\mathrm{d}}{\mathrm{dx}} g(\mathrm{x})$

## Example:

$$
\begin{aligned}
& f(\mathrm{x})=\mathrm{e}^{\left(\mathrm{x}^{2}+2 \mathrm{x}\right)} \\
& \frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})=\mathrm{e}^{\left(\mathrm{x}^{2}+2 \mathrm{x}\right)} \frac{\mathrm{d}}{\mathrm{dx}}\left(\mathrm{x}^{2}+2 \mathrm{x}\right) \\
& \frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})=\left(\mathrm{e}^{\left(\mathrm{x}^{2}+2 \mathrm{x}\right)}\right)(2 \mathrm{x}+2)
\end{aligned}
$$

### 6.5 Trigonometric derivatives

$$
\begin{aligned}
\frac{d}{d x} \sin x=\cos x & \frac{d}{d x} \cos x=-\sin x \\
\frac{d}{d x} \tan x=\sec ^{2} x & \frac{d}{d x} \cot x=-\csc ^{2} x \\
\frac{d}{d x} \sec x=(\sec x)(\tan x) & \frac{d}{d x} \csc x=(-\csc x)(\cot x)
\end{aligned}
$$

### 6.6 Rules for derivatives

### 6.6.1 Constant rule

$\frac{\mathrm{d}}{\mathrm{dx}}[\mathrm{cf}(\mathrm{x})]=\mathrm{c} \frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})$

### 6.6.2 Rule of sums

$$
\frac{\mathrm{d}}{\mathrm{dx}}[f(\mathrm{x})+g(\mathrm{x})]=\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})+\frac{\mathrm{d}}{\mathrm{dx}} g(\mathrm{x})
$$

### 6.6.3 Rule of differences

$$
\frac{\mathrm{d}}{\mathrm{dx}}[f(\mathrm{x})-g(\mathrm{x})]=\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})-\frac{\mathrm{d}}{\mathrm{dx}} g(\mathrm{x})
$$

### 6.6.4 Product rule

$\frac{\mathrm{d}}{\mathrm{dx}}[f(\mathrm{x}) g(\mathrm{x})]=f(\mathrm{x})\left[\frac{\mathrm{d}}{\mathrm{dx}} g(\mathrm{x})\right]+g(\mathrm{x})\left[\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})\right]$

### 6.6.5 Quotient rule

$\frac{\mathrm{d}}{\mathrm{dx}} \frac{f(\mathrm{x})}{g(\mathrm{x})}=\frac{g(\mathrm{x})\left[\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})\right]-f(\mathrm{x})\left[\frac{\mathrm{d}}{\mathrm{dx}} g(\mathrm{x})\right]}{[g(\mathrm{x})]^{2}}$

### 6.6.6 Power rule

$\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})^{\mathrm{a}}=\mathrm{a}[f(\mathrm{x})]^{\mathrm{a}-1} \frac{\mathrm{~d}}{\mathrm{dx}} f(\mathrm{x})$

### 6.6.7 Functions of other functions

$\frac{\mathrm{d}}{\mathrm{dx}} f[g(\mathrm{x})]$
Break the function into two functions:

$$
\mathrm{u}=g(\mathrm{x}) \quad \text { and } \quad \mathrm{y}=f(\mathrm{u})
$$

Solve:
$\frac{\mathrm{dy}}{\mathrm{dx}} f[g(\mathrm{x})]=\frac{\mathrm{dy}}{\mathrm{du}} f(\mathrm{u}) \frac{\mathrm{du}}{\mathrm{dx}} g(\mathrm{x})$

### 6.7 The antiderivative (Indefinite integral)

If:

$$
\frac{\mathrm{d}}{\mathrm{dx}} f(\mathrm{x})=g(\mathrm{x})
$$

Then:
$g(\mathrm{x})$ is the derivative of $f(\mathrm{x})$
$f(\mathrm{x})$ is the antiderivative of $g(\mathrm{x})$
$\int g(\mathrm{x}) \mathrm{dx}=f(\mathrm{x})+\mathrm{c}$
Notice something important here: taking the derivative of $f(x)$ may precisely give you $g(x)$, but taking the antiderivative of $g(x)$ does not necessarily give you $f(x)$ in its original form. Example:

$$
\begin{aligned}
& f(x)=3 x^{2}+5 \\
& \frac{d}{d x} f(x)=6 x \\
& \int 6 x d x=3 x^{2}+c
\end{aligned}
$$

Note that the constant $c$ is unknown! The original function $f(x)$ could have been $3 x^{2}+5$, $3 \mathrm{x}^{2}+10,3 \mathrm{x}^{2}+$ anything, and the derivative of $\mathrm{f}(\mathrm{x})$ would have still been 6 x . Determining the antiderivative of a function, then, is a bit less certain than determining the derivative of a function.

### 6.8 Common antiderivatives

$$
\begin{aligned}
& \int x^{n} d x=\frac{x^{n+1}}{n+1}+c \\
& \int \frac{1}{x} d x=(\ln |x|)+c
\end{aligned}
$$

Where,
$\mathrm{c}=\mathrm{a}$ constant

$$
\int \mathrm{a}^{\mathrm{x}} \mathrm{dx}=\frac{\mathrm{a}^{\mathrm{x}}}{\ln \mathrm{a}}+\mathrm{c}
$$

### 6.9 Antiderivatives of power functions of $e$

$$
\int \mathrm{e}^{\mathrm{x}} \mathrm{dx}=\mathrm{e}^{\mathrm{x}}+\mathrm{c}
$$

Note: this is a very unique and useful property of e. As in the case of derivatives, the antiderivative of such a function is that same function. In the case of the antiderivative, a constant term "c" is added to the end as well.

### 6.10 Rules for antiderivatives

### 6.10.1 Constant rule

$\int c f(x) d x=c \int f(x) d x$

### 6.10.2 Rule of sums

$$
\int[f(\mathrm{x})+g(\mathrm{x})] \mathrm{dx}=\left[\int f(\mathrm{x}) \mathrm{dx}\right]+\left[\int g(\mathrm{x}) \mathrm{dx}\right]
$$

### 6.10.3 Rule of differences

```
\int[f(x)-g(x)]dx = [\intf(x)dx ]-[\intg(x)dx ]
```


### 6.11 Definite integrals and the fundamental theorem of calculus

If:

$$
\int f(\mathrm{x}) \mathrm{dx}=g(\mathrm{x}) \quad \text { or } \quad \frac{\mathrm{d}}{\mathrm{dx}} g(\mathrm{x})=f(\mathrm{x})
$$

Then:
$\int_{\mathrm{a}}^{\mathrm{b}} f(\mathrm{x}) \mathrm{dx}=g(\mathrm{~b})-g(\mathrm{a})$

Where, a and b are constants

## If:

$$
\int f(\mathrm{x}) \mathrm{dx}=g(\mathrm{x}) \quad \text { and } \quad \mathrm{a}=0
$$

## Then:

$$
\int_{0}^{\mathrm{x}} f(\mathrm{x}) \mathrm{dx}=g(\mathrm{x})
$$

### 6.12 Differential equations

As opposed to normal equations where the solution is a number, a differential equation is one where the solution is actually a function, and which at least one derivative of that unknown function is part of the equation.

As with finding antiderivatives of a function, we are often left with a solution that encompasses more than one possibility (consider the many possible values of the constant "c" typically found in antiderivatives). The set of functions which answer any differential equation is called the "general solution" for that differential equation. Any one function out of that set is referred to as a "particular solution" for that differential equation. The variable of reference for differentiation and integration within the differential equation is known as the "independent variable."

## Chapter 7

## USING THE SPICE CIRCUIT SIMULATION PROGRAM

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### 7.1 Introduction

> "With Electronics Workbench, you can create circuit schematics that look just the same as those you're already familiar with on paper - plus you can flip the power switch so the schematic behaves like a real circuit. With other electronics simulators, you may have to type in SPICE node lists as text files - an abstract representation of a circuit beyond the capabilities of all but advanced electronics engineers."
(Electronics Workbench User's guide - version 4, page 7)
This introduction comes from the operating manual for a circuit simulation program called Electronics Workbench. Using a graphic interface, it allows the user to draw a circuit schematic and then have the computer analyze that circuit, displaying the results in graphic form. It is a very valuable analysis tool, but it has its shortcomings. For one, it and other graphic programs like it tend to be unreliable when analyzing complex circuits, as the translation from picture to computer code is not quite the exact science we would want it to be (yet). Secondly, due to its graphics requirements, it tends to need a significant amount of computational "horsepower" to run, and a computer operating system that supports graphics. Thirdly, these graphic programs can be costly.

However, underneath the graphics skin of Electronics Workbench lies a robust (and free!) program called SPICE, which analyzes a circuit based on a text-file description of the circuit's components and connections. What the user pays for with Electronics Workbench and other graphic circuit analysis programs is the convenient "point and click" interface, while SPICE does the actual mathematical analysis.

By itself, SPICE does not require a graphic interface and demands little in system resources. It is also very reliable. The makers of Electronic Workbench would like you to think that using SPICE in its native text mode is a task suited for rocket scientists, but I'm writing this to prove them wrong. SPICE is fairly easy to use for simple circuits, and its non-graphic interface actually lends itself toward the analysis of circuits that can be difficult to draw. I think it was the programming expert Donald Knuth who quipped, "What you see is all you get" when it comes to computer applications. Graphics may look more attractive, but abstracted interfaces (text) are actually more efficient.

This document is not intended to be an exhaustive tutorial on how to use SPICE. I'm merely trying to show the interested user how to apply it to the analysis of simple circuits, as an alternative to proprietary ( $\$ \$ \$$ ) and buggy programs. Once you learn the basics, there are other tutorials better suited to take you further. Using SPICE - a program originally intended to develop integrated
circuits - to analyze some of the really simple circuits showcased here may seem a bit like cutting butter with a chain saw, but it works!

All options and examples have been tested on SPICE version 2 g 6 on both MS-DOS and Linux operating systems. As far as I know, I'm not using features specific to version 2 g 6 , so these simple functions should work on most versions of SPICE.

### 7.2 History of SPICE

SPICE is a computer program designed to simulate analog electronic circuits. It original intent was for the development of integrated circuits, from which it derived its name: Simulation Program with Integrated Circuit Emphasis.

The origin of SPICE traces back to another circuit simulation program called CANCER. Developed by professor Ronald Rohrer of U.C. Berkeley along with some of his students in the late 1960's, CANCER continued to be improved through the early 1970's. When Rohrer left Berkeley, CANCER was re-written and re-named to SPICE, released as version 1 to the public domain in May of 1972. Version 2 of SPICE was released in 1975 (version 2 g 6 - the version used in this book - is a minor revision of this 1975 release). Instrumental in the decision to release SPICE as a public-domain computer program was professor Donald Pederson of Berkeley, who believed that all significant technical progress happens when information is freely shared. I for one thank him for his vision.

A major improvement came about in March of 1985 with version 3 of SPICE (also released under public domain). Written in the C language rather than FORTRAN, version 3 incorporated additional transistor types (the MESFET, for example), and switch elements. Version 3 also allowed the use of alphabetical node labels rather than only numbers. Instructions written for version 2 of SPICE should still run in version 3, though.

Despite the additional power of version 3, I have chosen to use version 2 g 6 throughout this book because it seems to be the easiest version to acquire and run on different computer systems.

### 7.3 Fundamentals of SPICE programming

Programming a circuit simulation with SPICE is much like programming in any other computer language: you must type the commands as text in a file, save that file to the computer's hard drive, and then process the contents of that file with a program (compiler or interpreter) that understands such commands.

In an interpreted computer language, the computer holds a special program called an interpreter that translates the program you wrote (the so-called source file) into the computer's own language, on the fly, as it's being executed:

Computer


In a compiled computer language, the program you wrote is translated all at once into the computer's own language by a special program called a compiler. After the program you've written has been "compiled," the resulting executable file needs no further translation to be understood directly by the computer. It can now be "run" on a computer whether or not compiler software has been installed on that computer:


SPICE is an interpreted language. In order for a computer to be able to understand the SPICE instructions you type, it must have the SPICE program (interpreter) installed:

## Computer



SPICE source files are commonly referred to as "netlists," although they are sometimes known as "decks" with each line in the file being called a "card." Cute, don't you think? Netlists are created by a person like yourself typing instructions line-by-line using a word processor or text editor. Text editors are much preferred over word processors for any type of computer programming, as they produce pure ASCII text with no special embedded codes for text highlighting (like italic or boldface fonts), which are uninterpretable by interpreter and compiler software.

As in general programming, the source file you create for SPICE must follow certain conventions of programming. It is a computer language in itself, albeit a simple one. Having programmed in BASIC and C/C++, and having some experience reading PASCAL and FORTRAN programs, it is my opinion that the language of SPICE is much simpler than any of these. It is about the same complexity as a markup language such as HTML, perhaps less so.

There is a cycle of steps to be followed in using SPICE to analyze a circuit. The cycle starts
when you first invoke the text editing program and make your first draft of the netlist. The next step is to run SPICE on that new netlist and see what the results are. If you are a novice user of SPICE, your first attempts at creating a good netlist will be fraught with small errors of syntax. Don't worry - as every computer programmer knows, proficiency comes with lots of practice. If your trial run produces error messages or results that are obviously incorrect, you need to re-invoke the text editing program and modify the netlist. After modifying the netlist, you need to run SPICE again and check the results. The sequence, then, looks something like this:

- Compose a new netlist with a text editing program. Save that netlist to a file with a name of your choice.
- Run SPICE on that netlist and observe the results.
- If the results contain errors, start up the text editing program again and modify the netlist.
- Run SPICE again and observe the new results.
- If there are still errors in the output of SPICE, re-edit the netlist again with the text editing program. Repeat this cycle of edit/run as many times as necessary until you are getting the desired results.
- Once you've "debugged" your netlist and are getting good results, run SPICE again, only this time redirecting the output to a new file instead of just observing it on the computer screen.
- Start up a text editing program or a word processor program and open the SPICE output file you just created. Modify that file to suit your formatting needs and either save those changes to disk and/or print them out on paper.

To "run" a SPICE "program," you need to type in a command at a terminal prompt interface, such as that found in MS-DOS, UNIX, or the MS-Windows DOS prompt option:

```
spice < example.cir
```

The word "spice" invokes the SPICE interpreting program (providing that the SPICE software has been installed on the computer!), the " $<$ " symbol redirects the contents of the source file to the SPICE interpreter, and example.cir is the name of the source file for this circuit example. The file extension ".cir" is not mandatory; I have seen ".inp" (for "input") and just plain ".txt" work well, too. It will even work when the netlist file has no extension. SPICE doesn't care what you name it, so long as it has a name compatible with the filesystem of your computer (for old MS-DOS machines, for example, the filename must be no more than 8 characters in length, with a 3 character extension, and no spaces or other non-alphanumerical characters).

When this command is typed in, SPICE will read the contents of the example.cir file, analyze the circuit specified by that file, and send a text report to the computer terminal's standard output (usually the screen, where you can see it scroll by). A typical SPICE output is several screens worth of information, so you might want to look it over with a slight modification of the command:
spice < example.cir | more

This alternative "pipes" the text output of SPICE to the "more" utility, which allows only one page to be displayed at a time. What this means (in English) is that the text output of SPICE is halted after one screen-full, and waits until the user presses a keyboard key to display the next screen-full of text. If you're just testing your example circuit file and want to check for any errors, this is a good way to do it.
spice < example.cir > example.txt
This second alternative (above) redirects the text output of SPICE to another file, called example.txt, where it can be viewed or printed. This option corresponds to the last step in the development cycle listed earlier. It is recommended by this author that you use this technique of "redirection" to a text file only after you've proven your example circuit netlist to work well, so that you don't waste time invoking a text editor just to see the output during the stages of "debugging."

Once you have a SPICE output stored in a .txt file, you can use a text editor or (better yet!) a word processor to edit the output, deleting any unnecessary banners and messages, even specifying alternative fonts to highlight the headings and/or data for a more polished appearance. Then, of course, you can print the output to paper if you so desire. Being that the direct SPICE output is plain ASCII text, such a file will be universally interpretable on any computer whether SPICE is installed on it or not. Also, the plain text format ensures that the file will be very small compared to the graphic screen-shot files generated by "point-and-click" simulators.

The netlist file format required by SPICE is quite simple. A netlist file is nothing more than a plain ASCII text file containing multiple lines of text, each line describing either a circuit component or special SPICE command. Circuit architecture is specified by assigning numbers to each component's connection points in each line, connections between components designated by common numbers. Examine the following example circuit diagram and its corresponding SPICE file. Please bear in mind that the circuit diagram exists only to make the simulation easier for human beings to understand. SPICE only understands netlists:


```
Example netlist
v1 1 0 dc 15
r1 1 0 2.2k
r2 1 2 3.3k
r3 2 0 150
.end
```

Each line of the source file shown above is explained here:

- v1 represents the battery (voltage source 1), positive terminal numbered 1, negative terminal numbered 0 , with a DC voltage output of 15 volts.
- r1 represents resistor $R_{1}$ in the diagram, connected between points 1 and 0 , with a value of $2.2 \mathrm{k} \Omega$.
- r2 represents resistor $R_{2}$ in the diagram, connected between points 1 and 2 , with a value of $3.3 \mathrm{k} \Omega$.
- r3 represents resistor $R_{3}$ in the diagram, connected between points 2 and 0 , with a value of $150 \mathrm{k} \Omega$.

Electrically common points (or "nodes") in a SPICE circuit description share common numbers, much in the same way that wires connecting common points in a large circuit typically share common wire labels.

To simulate this circuit, the user would type those six lines of text on a text editor and save them as a file with a unique name (such as example.cir). Once the netlist is composed and saved to a file, the user then processes that file with one of the command-line statements shown earlier (spice $<$ example.cir), and will receive this text output on their computer's screen:

```
1*******10/10/99 ******** spice 2g.6 3/15/83 ********07:32:42*****
Oexample netlist
0**** input listing temperature = 27.000 deg c
v1 1 0 dc 15
r1 1 0 2.2k
r2 1 2 3.3k
r3 2 0 150
.end
*****10/10/99 ********* spice 2g.6 3/15/83 ******07:32:42******
Oexample netlist
0**** small signal bias solution temperature = 27.000 deg c
node voltage node voltage
(1) 15.0000 ( 2) 0.6522
voltage source currents
name current
v1 -1.117E-02
total power dissipation 1.67E-01 watts
job concluded
0 total job time 0.02
1*******10/10/99 ********* spice 2g.6 3/15/83 ******07:32:42*****
0**** input listing temperature = 27.000 deg c
```

SPICE begins by printing the time, date, and version used at the top of the output. It then lists the input parameters (the lines of the source file), followed by a display of DC voltage readings from each node (reference number) to ground (always reference number 0). This is followed by a list of current readings through each voltage source (in this case there's only one, v1). Finally, the total power dissipation and computation time in seconds is printed.

All output values provided by SPICE are displayed in scientific notation.
The SPICE output listing shown above is a little verbose for most peoples' taste. For a final presentation, it might be nice to trim all the unnecessary text and leave only what matters. Here is a sample of that same output, redirected to a text file (spice < example.cir > example.txt), then trimmed down judiciously with a text editor for final presentation and printed:

```
example netlist
v1 1 0 dc 15
r1 1 0 2.2k
r2 1 2 3.3k
r3 2 0 150
.end
node voltage node voltage
( 1) 15.0000 ( 2) 0.6522
voltage source currents
name current
v1 -1.117E-02
total power dissipation 1.67E-01 watts
```

One of the very nice things about SPICE is that both input and output formats are plain-text, which is the most universal and easy-to-edit electronic format around. Practically any computer will be able to edit and display this format, even if the SPICE program itself is not resident on that computer. If the user desires, he or she is free to use the advanced capabilities of word processing programs to make the output look fancier. Comments can even be inserted between lines of the output for further clarity to the reader.

### 7.4 The command-line interface

If you've used DOS or UNIX operating systems before in a command-line shell environment, you may wonder why we have to use the " $<$ " symbol between the word "spice" and the name of the netlist file to be interpreted. Why not just enter the file name as the first argument to the command "spice" as we do when we invoke the text editor? The answer is that SPICE has the option of an interactive mode, whereby each line of the netlist can be interpreted as it is entered through the computer's Standard Input (stdin). If you simple type "spice" at the prompt and press [Enter], SPICE will begin to interpret anything you type in to it (live).

For most applications, it's nice to save your netlist work in a separate file and then let SPICE interpret that file when you're ready. This is the way I encourage SPICE to be used, and so this is the way it's presented in this lesson. In order to use SPICE this way in a command-line environment, we need to use the " $<$ " redirection symbol to direct the contents of your netlist file to Standard Input (stdin), which SPICE can then process.

### 7.5 Circuit components

Remember that this tutorial is not exhaustive by any means, and that all descriptions for elements in the SPICE language are documented here in condensed form. SPICE is a very capable piece of software with lots of options, and I'm only going to document a few of them.

All components in a SPICE source file are primarily identified by the first letter in each respective line. Characters following the identifying letter are used to distinguish one component of a certain type from another of the same type (r1, r2, r3, rload, rpullup, etc.), and need not follow any particular naming convention, so long as no more than eight characters are used in both the component identifying letter and the distinguishing name.

For example, suppose you were simulating a digital circuit with "pullup" and "pulldown" resistors. The name rpullup would be valid because it is seven characters long. The name rpulldown, however, is nine characters long. This may cause problems when SPICE interprets the netlist.

You can actually get away with component names in excess of eight total characters if there are no other similarly-named components in the source file. SPICE only pays attention to the first eight characters of the first field in each line, so rpulldown is actually interpreted as rpulldow with the " $n$ " at the end being ignored. Therefore, any other resistor having the first eight characters in its first field will be seen by SPICE as the same resistor, defined twice, which will cause an error (i.e. rpulldown1 and rpulldown2 would be interpreted as the same name, rpulldow).

It should also be noted that SPICE ignores character case, so r1 and R1 are interpreted by SPICE as one and the same.

SPICE allows the use of metric prefixes in specifying component values, which is a very handy feature. However, the prefix convention used by SPICE differs somewhat from standard metric symbols, primarily due to the fact that netlists are restricted to standard ASCII characters (ruling out Greek letters such as $\mu$ for the prefix "micro") and that SPICE is case-insensitive, so "m" (which is the standard symbol for "milli") and "M" (which is the standard symbol for "Mega") are interpreted identically. Here are a few examples of prefixes used in SPICE netlists:

```
r1 1 0 2t (Resistor R }\mp@subsup{\textrm{R}}{1}{},2\textrm{t}=2\mathrm{ Tera-ohms = 2 T}\Omega\mathrm{ )
r2 1 0 4g (Resistor R2, 4g=4 Giga-ohms = 4 G\Omega)
r3 1 0 47meg (Resistor R R , 47meg = 47 Mega-ohms = 47 M\Omega)
r41 0 3.3k (Resistor }\mp@subsup{\textrm{R}}{4}{},3.3\textrm{k}=3.3\mathrm{ kilo-ohms = 3.3 k }\Omega\mathrm{ )
r5 1 0 55m (Resistor R R , 55m = 55 milli-ohms = 55 m}\Omega\mathrm{ )
r6 1 0 10u (Resistor R}\mp@subsup{\textrm{R}}{6}{},10\textrm{u}=10\mathrm{ micro-ohms 10 }\mu\Omega\mathrm{ )
r7 1 0 30n (Resistor R }\mp@subsup{\textrm{R}}{7}{},30\textrm{n}=30\mathrm{ nano-ohms = 30 n }\Omega\mathrm{ )
r8 1 0 5p (Resistor R}\mp@subsup{\textrm{R}}{8}{},5\textrm{p}=5\mathrm{ pico-ohms = 5 p 
r9 1 0 250f (Resistor R}\mp@subsup{\textrm{R}}{9}{},250\textrm{f}=250\mathrm{ femto-ohms = 250 f }\Omega\mathrm{ )
```

Scientific notation is also allowed in specifying component values. For example:

```
r10 1 0 4.7e3 (Resistor R R }10,4.7\textrm{e}3=4.7\times1\mp@subsup{0}{}{3}\mathrm{ ohms = 4.7 kilo-ohms = 4.7 k }\Omega
r11 1 0 1e-12 (Resistor R R 
```

The unit (ohms, volts, farads, henrys, etc.) is automatically determined by the type of component being specified. SPICE "knows" that all of the above examples are "ohms" because they are all resistors (r1, r2, r3, . . .). If they were capacitors, the values would be interpreted as "farads," if inductors, then "henrys," etc.

### 7.5.1 Passive components

## CAPACITORS:

```
General form: c[name] [node1] [node2] [value] ic=[initial voltage]
Example 1: c1 12 33 10u
Example 2: c1 12 33 10u ic=3.5
```

Comments: The "initial condition" (ic=) variable is the capacitor's voltage in units of volts at the start of DC analysis. It is an optional value, with the starting voltage assumed to be zero if unspecified. Starting current values for capacitors are interpreted by SPICE only if the .tran analysis option is invoked (with the "uic" option).

## INDUCTORS:

```
General form: l[name] [node1] [node2] [value] ic=[initial current]
Example 1: l1 12 33 133m
Example 2: l1 12 33 133m ic=12.7m
```

Comments: The "initial condition" (ic=) variable is the inductor's current in units of amps at the start of DC analysis. It is an optional value, with the starting current assumed to be zero if unspecified. Starting current values for inductors are interpreted by SPICE only if the .tran analysis option is invoked.

## INDUCTOR COUPLING (transformers):

```
General form: k[name] l[name] l[name] [coupling factor]
```

Example 1: k1 l1 120.999

Comments: SPICE will only allow coupling factor values between 0 and 1 (non-inclusive), with 0 representing no coupling and 1 representing perfect coupling. The order of specifying coupled inductors ( 11,12 or 12,11 ) is irrelevant.

## RESISTORS:

$\begin{array}{ll}\text { General form: } & r \text { [name] [node1] [node2] [value] } \\ \text { Example: } & \text { rload } 23153.3 \mathrm{k}\end{array}$
Comments: In case you were wondering, there is no declaration of resistor power dissipation rating in SPICE. All components are assumed to be indestructible. If only real life were this forgiving!

### 7.5.2 Active components

All semiconductor components must have their electrical characteristics described in a line starting with the word ".model", which tells SPICE exactly how the device will behave. Whatever parameters are not explicitly defined in the .model card will default to values pre-programmed in SPICE. However, the .model card must be included, and at least specify the model name and device type (d, npn, pnp, njf, pjf, nmos, or pmos).

## DIODES:

```
General form: d[name] [anode] [cathode] [model]
Example: d1 1 2 mod1
```


## DIODE MODELS:

```
General form: .model [modelname] d [parmtr1=x] [parmtr2=x] . . .
Example: .model mod1 d
Example: .model mod2 d vj=0.65 rs=1.3
```

Parameter definitions:
is $=$ saturation current in amps
rs $=$ junction resistance in ohms
$\mathrm{n}=$ emission coefficient (unitless)
$\mathrm{tt}=$ transit time in seconds
cjo $=$ zero-bias junction capacitance in farads
$\mathrm{vj}=$ junction potential in volts
$\mathrm{m}=$ grading coefficient (unitless)
eg $=$ activation energy in electron-volts
xti $=$ saturation-current temperature exponent (unitless)
$\mathrm{kf}=$ flicker noise coefficient (unitless)
af $=$ flicker noise exponent (unitless)
$\mathrm{fc}=$ forward-bias depletion capacitance coefficient (unitless)
$\mathrm{bv}=$ reverse breakdown voltage in volts
ibv $=$ current at breakdown voltage in amps
Comments: The model name must begin with a letter, not a number. If you plan to specify a model for a 1N4003 rectifying diode, for instance, you cannot use " 1 n 4003 " for the model name. An alternative might be "m1n4003" instead.

TRANSISTORS (bipolar junction - BJT):

```
General form: q[name] [collector] [base] [emitter] [model]
Example: q1 2 3 0 mod1
    BJT TRANSISTOR MODELS:
General form: .model [modelname] [npn or pnp] [parmtr1=x] . . .
Example: .model mod1 pnp
Example: .model mod2 npn bf=75 is=1e-14
```

The model examples shown above are very nonspecific. To accurately model real-life transistors, more parameters are necessary. Take these two examples, for the popular 2N2222 and 2N2907 transistors (the " + ") characters represent line-continuation marks in SPICE, when you wish to break a single line (card) into two or more separate lines on your text editor:

```
Example: .model m2n2222 npn is=19f bf=150 vaf=100 ikf=.18
    ise=50p ne=2.5 br=7.5 var=6.4 ikr=12m
    isc=8.7p nc=1.2 rb=50 re=0.4 rc=0.4 cje=26p
    tf=0.5n cjc=11p tr=7n xtb=1.5 kf=0.032f af=1
Example: .model m2n2907 pnp is=1.1p bf=200 nf=1.2 vaf=50
    ikf=0.1 ise=13p ne=1.9 br=6 rc=0.6 cje=23p
    vje=0.85 mje=1.25 tf=0.5n cjc=19p vjc=0.5
    mjc=0.2 tr=34n xtb=1.5
```

Parameter definitions:
is $=$ transport saturation current in amps
$\mathrm{bf}=$ ideal maximum forward Beta (unitless)
$\mathrm{nf}=$ forward current emission coefficient (unitless)

```
vaf \(=\) forward Early voltage in volts
ikf \(=\) corner for forward Beta high-current rolloff in amps
ise \(=\) B-E leakage saturation current in amps
ne \(=\) B-E leakage emission coefficient (unitless)
\(\mathrm{br}=\) ideal maximum reverse Beta (unitless)
\(\mathrm{nr}=\) reverse current emission coefficient (unitless)
bar \(=\) reverse Early voltage in volts
ikrikr \(=\) corner for reverse Beta high-current rolloff in amps
iscisc \(=\) B-C leakage saturation current in amps
\(\mathrm{nc}=\mathrm{B}-\mathrm{C}\) leakage emission coefficient (unitless)
\(\mathrm{rb}=\) zero bias base resistance in ohms
irb \(=\) current for base resistance halfway value in amps
\(\mathrm{rbm}=\) minimum base resistance at high currents in ohms
\(\mathrm{re}=\) emitter resistance in ohms
\(\mathrm{rc}=\) collector resistance in ohms
cje \(=\) B-E zero-bias depletion capacitance in farads
vje \(=\) B-E built-in potential in volts
mje \(=\) B-E junction exponential factor (unitless)
\(\mathrm{tf}=\) ideal forward transit time (seconds)
\(\mathrm{xtf}=\) coefficient for bias dependence of transit time (unitless)
\(\mathrm{vtf}=\mathrm{B}-\mathrm{C}\) voltage dependence on transit time, in volts
itf \(=\) high-current parameter effect on transit time, in amps
ptf \(=\) excess phase at \(\mathrm{f}=1 /(\) transit time \()(2)(\mathrm{pi}) \mathrm{Hz}\), in degrees
\(\mathrm{cjc}=\mathrm{B}-\mathrm{C}\) zero-bias depletion capacitance in farads
\(\mathrm{vjc}=\mathrm{B}-\mathrm{C}\) built-in potential in volts
\(\mathrm{mjc}=\mathrm{B}-\mathrm{C}\) junction exponential factor (unitless)
\(\mathrm{xjcj}=\mathrm{B}-\mathrm{C}\) depletion capacitance fraction connected in base node (unitless)
\(\mathrm{tr}=\) ideal reverse transit time in seconds
\(\mathrm{cjs}=\) zero-bias collector-substrate capacitance in farads
\(\mathrm{vjs}=\) substrate junction built-in potential in volts
\(\mathrm{mjs}=\) substrate junction exponential factor (unitless)
\(\mathrm{xtb}=\) forward/reverse Beta temperature exponent
eg = energy gap for temperature effect on transport saturation current in electron-volts
\(\mathrm{xti}=\) temperature exponent for effect on transport saturation current (unitless)
\(\mathrm{kf}=\) flicker noise coefficient (unitless)
af \(=\) flicker noise exponent (unitless)
\(\mathrm{fc}=\) forward-bias depletion capacitance formula coefficient (unitless)
```

Comments: Just as with diodes, the model name given for a particular transistor type must begin with a letter, not a number. That's why the examples given above for the 2N2222 and 2N2907 types of BJTs are named "m2n2222" and "m2n2907" respectively.

As you can see, SPICE allows for very detailed specification of transistor properties. Many of the properties listed above are well beyond the scope and interest of the beginning electronics student, and aren't even useful apart from knowing the equations SPICE uses to model BJT transistors. For those interested in learning more about transistor modeling in SPICE, consult other books, such as Andrei Vladimirescu's The Spice Book (ISBN 0-471-60926-9).

TRANSISTORS (junction field-effect - JFET):

```
General form: j[name] [drain] [gate] [source] [model]
Example: j1 2 3 0 mod1
```

JFET TRANSISTOR MODELS:

```
General form: .model [modelname] [njf or pjf] [parmtr1=x] . . .
Example: .model mod1 pjf
Example: .model mod2 njf lambda=1e-5 pb=0.75
```

Parameter definitions:
vto $=$ threshold voltage in volts
beta $=$ transconductance parameter in amps/volts ${ }^{2}$
lambda $=$ channel length modulation parameter in units of $1 /$ volts
$\mathrm{rd}=$ drain resistance in ohms
$\mathrm{rs}=$ source resistance in ohms
cgs $=$ zero-bias G-S junction capacitance in farads
cgd $=$ zero-bias G-D junction capacitance in farads
$\mathrm{pb}=$ gate junction potential in volts
is $=$ gate junction saturation current in amps
$\mathrm{kf}=$ flicker noise coefficient (unitless)
af $=$ flicker noise exponent (unitless)
$\mathrm{fc}=$ forward-bias depletion capacitance coefficient (unitless)

TRANSISTORS (insulated-gate field-effect - IGFET or MOSFET):
General form: m[name] [drain] [gate] [source] [substrate] [model]
Example: m1 $2300 \bmod 1$
MOSFET TRANSISTOR MODELS:

```
General form: .model [modelname] [nmos or pmos] [parmtr1=x] . . .
Example: .model mod1 pmos
Example: .model mod2 nmos level=2 phi=0.65 rd=1.5
Example: .model mod3 nmos vto=-1 (depletion)
Example: .model mod4 nmos vto=1 (enhancement)
Example: .model mod5 pmos vto=1 (depletion)
Example: .model mod6 pmos vto=-1 (enhancement)
```

Comments: In order to distinguish between enhancement mode and depletion-mode (also known as depletion-enhancement mode) transistors, the model parameter "vto" (zero-bias threshold voltage) must be specified. Its default value is zero, but a positive value ( +1 volts, for example) on a P-channel transistor or a negative value ( -1 volts) on an N-channel transistor will specify that transistor to be a depletion (otherwise known as depletion-enhancement) mode device. Conversely, a negative value on a P-channel transistor or a positive value on an N -channel transistor will specify that transistor to be an enhancement mode device.

Remember that enhancement mode transistors are normally-off devices, and must be turned on by the application of gate voltage. Depletion-mode transistors are normally "on," but can be "pinched off" as well as enhanced to greater levels of drain current by applied gate voltage, hence the alternate designation of "depletion-enhancement" MOSFETs. The "vto" parameter specifies the threshold gate voltage for MOSFET conduction.

### 7.5.3 Sources

```
AC SINEWAVE VOLTAGE SOURCES (when using .ac card to specify frequency):
General form: v[name] [+node] [-node] ac [voltage] [phase] sin
Example 1: v1 1 0 ac 12 sin
Example 2: v1 1 0 ac 12 240 sin (12 V L 240')
```

Comments: This method of specifying AC voltage sources works well if you're using multiple sources at different phase angles from each other, but all at the same frequency. If you need to specify sources at different frequencies in the same circuit, you must use the next method!

AC SINEWAVE VOLTAGE SOURCES (when NOT using .ac card to specify frequency):
General form: v[name] [+node] [-node] sin([offset] [voltage] $+\quad$ [freq] [delay] [damping factor])
Example 1: v1 $10 \sin (0126000)$
Parameter definitions:
offset $=\mathrm{DC}$ bias voltage, offsetting the AC waveform by a specified voltage.
voltage $=$ peak, or crest, AC voltage value for the waveform.
freq $=$ frequency in Hertz.
delay $=$ time delay, or phase offset for the waveform, in seconds.
damping factor $=$ a figure used to create waveforms of decaying amplitude.
Comments: This method of specifying AC voltage sources works well if you're using multiple sources at different frequencies from each other. Representing phase shift is tricky, though, necessitating the use of the delay factor.

DC VOLTAGE SOURCES (when using .dc card to specify voltage):
General form: v[name] [+node] [-node] dc
Example 1: v1 10 dc
Comments: If you wish to have SPICE output voltages not in reference to node 0 , you must use the .dc analysis option, and to use this option you must specify at least one of your DC sources in this manner.

DC VOLTAGE SOURCES (when NOT using .dc card to specify voltage):

```
General form: v[name] [+node] [-node] dc [voltage]
```

Example 1: v1 10 dc 12

Comments: Nothing noteworthy here!

## PULSE VOLTAGE SOURCES

```
General form: v[name] [+node] [-node] pulse ([i] [p] [td] [tr]
+ [tf] [pw] [pd])
```

Parameter definitions:
i $=$ initial value
$p=$ pulse value
$\mathrm{td}=$ delay time (all time parameters in units of seconds)
$\mathrm{tr}=$ rise time
$\mathrm{tf}=$ fall time
$\mathrm{pw}=$ pulse width
pd $=$ period
Example 1: v1 10 pulse ( -3300010 m 20 m )
Comments: Example 1 is a perfect square wave oscillating between -3 and +3 volts, with zero rise and fall times, a 20 millisecond period, and a 50 percent duty cycle ( +3 volts for 10 ms , then -3 volts for 10 ms ).

AC SINEWAVE CURRENT SOURCES (when using .ac card to specify frequency):
General form: i [name] [+node] [-node] ac [current] [phase] sin
Example 1: i1 10 ac 3 sin (3 amps)
Example 2: i1 10 ac $1 \mathrm{~m} 240 \sin \left(1 \mathrm{~mA} L 240^{\circ}\right)$
Comments: The same comments apply here (and in the next example) as for AC voltage sources.

AC SINEWAVE CURRENT SOURCES (when NOT using .ac card to specify frequency):
General form: i[name] [+node] [-node] sin([offset]
$+\quad$ [current] [freq] 0 0)
Example 1: i1 $10 \sin (01.56000)$

DC CURRENT SOURCES (when using .dc card to specify current):
General form: i [name] [+node] [-node] dc
Example 1: i1 10 dc
DC CURRENT SOURCES (when NOT using .dc card to specify current):
General form: i [name] [+node] [-node] dc [current]
Example 1: i1 10 dc 12
Comments: Even though the books all say that the first node given for the DC current source is the positive node, that's not what I've found to be in practice. In actuality, a DC current source in SPICE pushes current in the same direction as a voltage source (battery) would with its negative node specified first.

## PULSE CURRENT SOURCES

```
General form: i [name] [+node] [-node] pulse ([i] [p] [td] [tr]
+ [tf] [pw] [pd])
    Parameter definitions:
    i = initial value
    p = pulse value
    td = delay time
    tr}= rise tim
    tf = fall time
    pw = pulse width
    pd = period
Example 1: i1 1 0 pulse (-3m 3m 0 0 0 17m 34m)
```

Comments: Example 1 is a perfect square wave oscillating between -3 mA and +3 mA , with zero rise and fall times, a 34 millisecond period, and a 50 percent duty cycle $(+3 \mathrm{~mA}$ for 17 ms , then -3 mA for 17 ms ).

VOLTAGE SOURCES (dependent):
General form: e[name] [out+node] [out-node] [in+node] [in-node]

+ [gain]

Example 1: e1 2012 999k
Comments: Dependent voltage sources are great to use for simulating operational amplifiers. Example 1 shows how such a source would be configured for use as a voltage follower, inverting input connected to output (node 2) for negative feedback, and the noninverting input coming in on node 1. The gain has been set to an arbitrarily high value of 999,000 . One word of caution, though: SPICE does not recognize the input of a dependent source as being a load, so a voltage source tied only to the input of an independent voltage source will be interpreted as "open." See op-amp circuit examples for more details on this.

## CURRENT SOURCES (dependent):

### 7.6 Analysis options

## AC ANALYSIS:

General form: .ac [curve] [points] [start] [final]
Example 1: .ac lin 110001000
Comments: The [curve] field can be "lin" (linear), "dec" (decade), or "oct" (octave), specifying the (non)linearity of the frequency sweep. ipoints; specifies how many points within the frequency sweep to perform analyses at (for decade sweep, the number of points per decade; for octave, the number of points per octave). The [start] and [final] fields specify the starting and ending frequencies of the sweep, respectively. One final note: the "start" value cannot be zero!

## DC ANALYSIS:

```
General form: .dc [source] [start] [final] [increment]
Example 1: .dc vin 1.5 15 0.5
```

Comments: The .dc card is necessary if you want to print or plot any voltage between two nonzero nodes. Otherwise, the default "small-signal" analysis only prints out the voltage between each nonzero node and node zero.

## TRANSIENT ANALYSIS:

```
General form: .tran [increment] [stop_time] [start_time]
```

+ [comp_interval]
Example 1: .tran 1m 50m uic
Example 2: .tran .5m 32m 0 .01m

Comments: Example 1 has an increment time of 1 millisecond and a stop time of 50 milliseconds (when only two parameters are specified, they are increment time and stop time, respectively). Example 2 has an increment time of 0.5 milliseconds, a stop time of 32 milliseconds, a start time of 0 milliseconds (no delay on start), and a computation interval of 0.01 milliseconds.

Default value for start time is zero. Transient analysis always beings at time zero, but storage of data only takes place between start time and stop time. Data output interval is increment time, or (stop time - start time) $/ 50$, which ever is smallest. However, the computing interval variable can be used to force a computational interval smaller than either. For large total interval counts, the itl5 variable in the . options card may be set to a higher number. The "uic" option tells SPICE to "use initial conditions."

## PLOT OUTPUT:

General form: .plot [type] [output1] [output2] . . . [output n]
Example 1: .plot dc $v(1,2)$ i(v2)
Example 2: .plot ac $v(3,4)$ vp $(3,4)$ i(v1) ip(v1)
Example 3: .plot tran $v(4,5)$ i(v2)
Comments: SPICE can't handle more than eight data point requests on a single . plot or .print card. If requesting more than eight data points, use multiple cards!

Also, here's a major caveat when using SPICE version 3: if you're performing AC analysis and you ask SPICE to plot an AC voltage as in example $\# 2$, the $\mathrm{v}(3,4)$ command will only output the real component of a rectangular-form complex number! SPICE version 2 outputs the polar magnitude of a complex number: a much more meaningful quantity if only a single quantity is asked for. To coerce SPICE3 to give you polar magnitude, you will have to re-write the . print or . plot argument as such: vm $(3,4)$.

## PRINT OUTPUT:

```
General form: .print [type] [output1] [output2] . . . [output n]
Example 1: .print dc v(1,2) i(v2)
Example 2: .print ac v(2,4) i(vinput) vp(2,3)
Example 3: .print tran v(4,5) i(v2)
```

Comments: SPICE can't handle more than eight data point requests on a single . plot or .print card. If requesting more than eight data points, use multiple cards!

FOURIER ANALYSIS:
General form: .four [freq] [output1] [output2] . . . [output n] Example 1: .four $60 \mathrm{v}(1,2)$

Comments: The .four card relies on the .tran card being present somewhere in the deck, with the proper time periods for analysis of adequate cycles. Also, SPICE may "crash" if a . plot analysis isn't done along with the .four analysis, even if all .tran parameters are technically correct. Finally, the .four analysis option only works when the frequency of the AC source is specified in that source's card line, and not in an .ac analysis option line.

It helps to include a computation interval variable in the . tran card for better analysis precision. A Fourier analysis of the voltage or current specified is performed up to the 9th harmonic, with the [freq] specification being the fundamental, or starting frequency of the analysis spectrum.

## MISCELLANEOUS:

```
General form: .options [option1] [option2]
Example 1: .options limpts=500
Example 2: .options itl5=0
Example 3: .options method=gear
```

```
Example 4: .options list
Example 5: .options nopage
Example 6: .options numdgt=6
```

Comments: There are lots of options that can be specified using this card. Perhaps the one most needed by beginning users of SPICE is the "limpts" setting. When running a simulation that requires more than 201 points to be printed or plotted, this calculation point limit must be increased or else SPICE will terminate analysis. The example given above (limpts=500) tells SPICE to allocate enough memory to handle at least 500 calculation points in whatever type of analysis is specified (DC, AC, or transient).

In example 2, we see an iteration variable (itl5) being set to a value of 0 . There are actually six different iteration variables available for user manipulation. They control the iteration cycle limits for solution of nonlinear equations. The variable itl5 sets the maximum number of iterations for a transient analysis. Similar to the limpts variable, itl5 usually needs to be set when a small computation interval has been specified on a .tran card. Setting itl5 to a value of 0 turns off the limit entirely, allowing the computer infinite iteration cycles (infinite time) to compute the analysis. Warning: this may result in long simulation times!

Example 3 with "method=gear" sets the numerical integration method used by SPICE. The default is "trapezoid" rather than "gear," trapezoid being a simple geometric approximation of area under a curve found by slicing up the curve into trapezoids to approximate the shape. The "gear" method is based on second-order or better polynomial equations and is named after C.W. Gear (Numerical Integration of Stiff Ordinary Equations, Report 221, Department of Computer Science, University of Illinois, Urbana). The Gear method of integration is more demanding of the computer (computationally "expensive") and will sometimes give slightly different results from the trapezoid method.

The "list" option shown in example 4 gives a verbose summary of all circuit components and their respective values in the final output.

By default, SPICE will insert ASCII page-break control codes in the output to separate different sections of the analysis. Specifying the "nopage" option (example 5) will prevent such pagination.

The "numdgt" option shown in example 6 specifies the number of significant digits output when using one of the ". print" data output options. SPICE defaults at a precision of 4 significant digits.

## WIDTH CONTROL:

```
General form: .width in=[columns] out=[columns]
Example 1: .width out=80
```

Comments: The .width card can be used to control the width of text output lines upon analysis. This is especially handy when plotting graphs with the .plot card. The default value is 120 , which can cause problems on 80 -character terminal displays unless set to 80 with this command.

### 7.7 Quirks

"Garbage in, garbage out."

## Anonymous

SPICE is a very reliable piece of software, but it does have its little quirks that take some getting used to. By "quirk" I mean a demand placed upon the user to write the source file in a particular
way in order for it to work without giving error messages. I do not mean any kind of fault with SPICE which would produce erroneous or misleading results: that would be more properly referred to as a "bug." Speaking of bugs, SPICE has a few of them as well.

Some (or all) of these quirks may be unique to SPICE version 2 g 6 , which is the only version I've used extensively. They may have been fixed in later versions.

### 7.7.1 A good beginning

SPICE demands that the source file begin with something other than the first "card" in the circuit description "deck." This first character in the source file can be a linefeed, title line, or a comment: there just has to be something there before the first component-specifying line of the file. If not, SPICE will refuse to do an analysis at all, claiming that there is a serious error (such as improper node connections) in the "deck."

### 7.7.2 A good ending

SPICE demands that the .end line at the end of the source file not be terminated with a linefeed or carriage return character. In other words, when you finish typing ". end" you should not hit the [Enter] key on your keyboard. The cursor on your text editor should stop immediately to the right of the "d" after the ". end" and go no further. Failure to heed this quirk will result in a "missing .end card" error message at the end of the analysis output. The actual circuit analysis is not affected by this error, so I normally ignore the message. However, if you're looking to receive a "perfect" output, you must pay heed to this idiosyncrasy.

### 7.7.3 Must have a node 0

You are given much freedom in numbering circuit nodes, but you must have a node 0 somewhere in your netlist in order for SPICE to work. Node 0 is the default node for circuit ground, and it is the point of reference for all voltages specified at single node locations.

When simple DC analysis is performed by SPICE, the output will contain a listing of voltages at all non-zero nodes in the circuit. The point of reference (ground) for all these voltage readings is node 0. For example:

```
node voltage node voltage
( 1) 15.0000 ( 2) 0.6522
```

In this analysis, there is a DC voltage of 15 volts between node 1 and ground (node 0 ), and a DC voltage of 0.6522 volts between node 2 and ground (node 0 ). In both these cases, the voltage polarity is negative at node 0 with reference to the other node (in other words, both nodes 1 and 2 are positive with respect to node 0 ).

### 7.7.4 Avoid open circuits

SPICE cannot handle open circuits of any kind. If your netlist specifies a circuit with an open voltage source, for example, SPICE will refuse to perform an analysis. A prime example of this type of error is found when "connecting" a voltage source to the input of a voltage-dependent source
(used to simulate an operational amplifier). SPICE needs to see a complete path for current, so I usually tie a high-value resistor (call it rbogus!) across the voltage source to act as a minimal load.

### 7.7.5 Avoid certain component loops

SPICE cannot handle certain uninterrupted loops of components in a circuit, namely voltage sources and inductors. The following loops will cause SPICE to abort analysis:

Parallel inductors

netlist
1124 10m
122450 m
1324 25m

Voltage source / inductor loop

netlist
v1 10 dc 12
1110 150m

## Series capacitors

$\mathrm{C}_{1} \stackrel{+}{=} 33 \mu \mathrm{~F}$

7

```
netlist
c1 5 6 33u
c2 6 7 47u
```

The reason SPICE can't handle these conditions stems from the way it performs DC analysis: by treating all inductors as shorts and all capacitors as opens. Since short-circuits ( $0 \Omega$ ) and open circuits (infinite resistance) either contain or generate mathematical infinitudes, a computer simply cannot deal with them, and so SPICE will discontinue analysis if any of these conditions occur.

In order to make these component configurations acceptable to SPICE, you must insert resistors of appropriate values into the appropriate places, eliminating the respective short-circuits and opencircuits. If a series resistor is required, choose a very low resistance value. Conversely, if a parallel resistor is required, choose a very high resistance value. For example:

To fix the parallel inductor problem, insert a very low-value resistor in series with each offending inductor.

fixed netlist
rbogus1 23 1e-12
rbogus2 25 1e-12
1134 10m
122450 m
135425 m

The extremely low-resistance resistors $\mathrm{R}_{\text {bogus } 1}$ and $\mathrm{R}_{\text {bogus } 2}$ (each one with a mere 1 pico-ohm of resistance) "break up" the direct parallel connections that existed between $\mathrm{L}_{1}, \mathrm{~L}_{2}$, and $\mathrm{L}_{3}$. It is important to choose very low resistances here so that circuit operation is not substantially impacted by the "fix."

To fix the voltage source / inductor loop, insert a very low-value resistor in series with the two components.


```
original netlist
v1 1 0 dc 12
l1 1 0 150m
```

fixed netlist
v1 10 dc 12
1120150 m
rbogus $121 e-12$

As in the previous example with parallel inductors, it is important to make the correction resistor $\left(\mathrm{R}_{\text {bogus }}\right)$ very low in resistance, so as to not substantially impact circuit operation.

To fix the series capacitor circuit, one of the capacitors must have a resistor shunting across it. SPICE requires a DC current path to each capacitor for analysis.

Original circuit
5

original netlist
c1 $5633 u$
c2 $6747 u$
fixed netlist
c1 56 33u
c2 $6747 u$
rbogus 679 e 12
"Fixed" circuit


The $\mathrm{R}_{\text {bogus }}$ value of 9 Tera-ohms provides a DC current path to $\mathrm{C}_{1}$ (and around $\mathrm{C}_{2}$ ) without substantially impacting the circuit's operation.

### 7.7.6 Current measurement

Although printing or plotting of voltage is quite easy in SPICE, the output of current values is a bit more difficult. Voltage measurements are specified by declaring the appropriate circuit nodes. For example, if we desire to know the voltage across a capacitor whose leads connect between nodes 4 and 7 , we might make out . print statement look like this:


```
c14 7 22u
.print ac v(4,7)
```

However, if we wanted to have SPICE measure the current through that capacitor, it wouldn't be quite so easy. Currents in SPICE must be specified in relation to a voltage source, not any arbitrary component. For example:


```
c147 22u
vinput 6 4 ac 1 sin
.print ac i(vinput)
```

This . print card instructs SPICE to print the current through voltage source $\mathrm{V}_{\text {input }}$, which happens to be the same as the current through our capacitor between nodes 4 and 7 . But what if there is no such voltage source in our circuit to reference for current measurement? One solution is to insert a shunt resistor into the circuit and measure voltage across it. In this case, I have chosen a shunt resistance value of $1 \Omega$ to produce 1 volt per amp of current through $\mathrm{C}_{1}$ :

c1 47 22u
rshunt 641
.print ac $\mathrm{v}(6,4)$

However, the insertion of an extra resistance into our circuit large enough to drop a meaningful voltage for the intended range of current might adversely affect things. A better solution for SPICE is this, although one would never seek such a current measurement solution in real life:

c14722u
vbogus 64 dc 0
.print ac i(vbogus)

Inserting a "bogus" DC voltage source of zero volts doesn't affect circuit operation at all, yet it provides a convenient place for SPICE to take a current measurement. Interestingly enough, it doesn't matter that $\mathrm{V}_{\text {bogus }}$ is a DC source when we're looking to measure AC current! The fact that SPICE will output an AC current reading is determined by the "ac" specification in the . print card and nothing more.

It should also be noted that the way SPICE assigns a polarity to current measurements is a bit odd. Take the following circuit as an example:


With 10 volts total voltage and $10 \mathrm{k} \Omega$ total resistance, you might expect SPICE to tell you there's going to be $1 \mathrm{~mA}(1 \mathrm{e}-03)$ of current through voltage source $\mathrm{V}_{1}$, but in actuality SPICE will output a figure of negative $1 \mathrm{~mA}(-1 \mathrm{e}-03)$ ! SPICE regards current out of the negative end of a DC voltage source (the normal direction) to be a negative value of current rather than a positive value of current. There are times I'll throw in a "bogus" voltage source in a DC circuit like this simply to get SPICE to output a positive current value:

example
v1 10
r1 125 k
r2 23 5k
vbogus 30 dc 0
.dc v1 10101
. print dc i(vbogus)
.end

Notice how $\mathrm{V}_{\text {bogus }}$ is positioned so that the circuit current will enter its positive side (node 3) and exit its negative side (node 0 ). This orientation will ensure a positive output figure for circuit current.

### 7.7.7 Fourier analysis

When performing a Fourier (frequency-domain) analysis on a waveform, I have found it necessary to either print or plot the waveform using the .print or .plot cards, respectively. If you don't print or plot it, SPICE will pause for a moment during analysis and then abort the job after outputting the "initial transient solution."

Also, when analyzing a square wave produced by the "pulse" source function, you must give the waveform some finite rise and fall time, or else the Fourier analysis results will be incorrect. For some reason, a perfect square wave with zero rise/fall time produces significant levels of even harmonics according to SPICE's Fourier analysis option, which is not true for real square waves.

### 7.8 Example circuits and netlists

The following circuits are pre-tested netlists for SPICE 2g6, complete with short descriptions when necessary. Feel free to "copy" and "paste" any of the netlists to your own SPICE source file for analysis and/or modification. My goal here is twofold: to give practical examples of SPICE netlist design to further understanding of SPICE netlist syntax, and to show how simple and compact SPICE netlists can be in analyzing simple circuits.

All output listings for these examples have been "trimmed" of extraneous information, giving you the most succinct presentation of the SPICE output as possible. I do this primarily to save space on this document. Typical SPICE outputs contain lots of headers and summary information not necessarily germane to the task at hand. So don't be surprised when you run a simulation on your own and find that the output doesn't exactly look like what I have shown here!

### 7.8.1 Multiple-source DC resistor network, part 1



Without a . dc card and a .print or .plot card, the output for this netlist will only display voltages for nodes 1,2 , and 3 (with reference to node 0 , of course).

```
Netlist:
Multiple dc sources
v1 1 0 dc 24
v2 3 0 dc 15
r1 1 2 10k
r2 2 3 8.1k
r3 2 0 4.7k
```

```
.end
```


## Output:

| node | voltage | node | voltage | node | voltage |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\left(\begin{array}{cc}1) & 24.0000\end{array} \quad(2)\right.$ | 9.7470 | $(3)$ | 15.0000 |  |  |

### 7.8.2 Multiple-source DC resistor network, part 2



By adding a .dc analysis card and specifying source $\mathrm{V}_{1}$ from 24 volts to 24 volts in 1 step (in other words, 24 volts steady), we can use the .print card analysis to print out voltages between any two points we desire. Oddly enough, when the .dc analysis option is invoked, the default voltage printouts for each node (to ground) disappears, so we end up having to explicitly specify them in the . print card to see them at all.

## Netlist:

```
Multiple dc sources
v1 1 0
v2 3 0 15
r1 1 2 10k
r2 2 3 8.1k
r3 2 0 4.7k
.dc v1 24 24 1
.print dc v(1) v(2) v(3) v(1,2) v(2,3)
.end
```


## Output:

| $v 1$ | $v(1)$ | $v(2)$ | $v(3)$ | $v(1,2)$ | $v(2,3)$ |
| :--- | :--- | :--- | :--- | :--- | :---: |
| $2.400 E+01$ | $2.400 E+01$ | $9.747 E+00$ | $1.500 E+01$ | $1.425 E+01$ | $-5.253 E+00$ |

### 7.8.3 RC time-constant circuit



For DC analysis, the initial conditions of any reactive component ( C or L ) must be specified (voltage for capacitors, current for inductors). This is provided by the last data field of each capacitor card (ic=0). To perform a DC analysis, the .tran ("transient") analysis option must be specified, with the first data field specifying time increment in seconds, the second specifying total analysis timespan in seconds, and the "uic" telling it to "use initial conditions" when analyzing.

```
    Netlist:
RC time delay circuit
v1 1 0 dc 10
c1 1 2 47u ic=0
c2 1 2 22u ic=0
r1 2 0 3.3k
.tran . 05 1 uic
.print tran v(1,2)
.end
```


## Output:

| time | $v(1,2)$ |
| :--- | :--- |
| $0.000 \mathrm{E}+00$ | $7.701 \mathrm{E}-06$ |
| $5.000 \mathrm{E}-02$ | $1.967 \mathrm{E}+00$ |
| $1.000 \mathrm{E}-01$ | $3.551 \mathrm{E}+00$ |
| $1.500 \mathrm{E}-01$ | $4.824 \mathrm{E}+00$ |
| $2.000 \mathrm{E}-01$ | $5.844 \mathrm{E}+00$ |
| $2.500 \mathrm{E}-01$ | $6.664 \mathrm{E}+00$ |
| $3.000 \mathrm{E}-01$ | $7.322 \mathrm{E}+00$ |
| $3.500 \mathrm{E}-01$ | $7.851 \mathrm{E}+00$ |
| $4.000 \mathrm{E}-01$ | $8.274 \mathrm{E}+00$ |
| $4.500 \mathrm{E}-01$ | $8.615 \mathrm{E}+00$ |
| $5.000 \mathrm{E}-01$ | $8.888 \mathrm{E}+00$ |
| $5.500 \mathrm{E}-01$ | $9.107 \mathrm{E}+00$ |
| $6.000 \mathrm{E}-01$ | $9.283 \mathrm{E}+00$ |
| $6.500 \mathrm{E}-01$ | $9.425 \mathrm{E}+00$ |
| $7.000 \mathrm{E}-01$ | $9.538 \mathrm{E}+00$ |
| $7.500 \mathrm{E}-01$ | $9.629 \mathrm{E}+00$ |
| $8.000 \mathrm{E}-01$ | $9.702 \mathrm{E}+00$ |


| $8.500 \mathrm{E}-01$ | $9.761 \mathrm{E}+00$ |
| :--- | :--- |
| $9.000 \mathrm{E}-01$ | $9.808 \mathrm{E}+00$ |
| $9.500 \mathrm{E}-01$ | $9.846 \mathrm{E}+00$ |
| $1.000 \mathrm{E}+00$ | $9.877 \mathrm{E}+00$ |

### 7.8.4 Plotting and analyzing a simple AC sinewave voltage



This exercise does show the proper setup for plotting instantaneous values of a sine-wave voltage source with the .plot function (as a transient analysis). Not surprisingly, the Fourier analysis in this deck also requires the .tran (transient) analysis option to be specified over a suitable time range. The time range in this particular deck allows for a Fourier analysis with rather poor accuracy. The more cycles of the fundamental frequency that the transient analysis is performed over, the more precise the Fourier analysis will be. This is not a quirk of SPICE, but rather a basic principle of waveforms.

## Netlist:

```
v1 1 0 sin(0 15 60 0 0)
rload 1 0 10k
* change tran card to the following for better Fourier precision
* .tran 1m 30m .01m and include .options card:
* .options itl5=30000
.tran 1m 30m
.plot tran v(1)
.four 60 v(1)
.end
```

Output:

| time | $\mathrm{v}(1) \quad-2.000 \mathrm{E}+01$ | $-1.000 \mathrm{E}+01$ | $0.000 \mathrm{E}+00$ | $1.000 \mathrm{E}+01$ |
| :---: | :---: | :---: | :---: | :---: |
| $0.000 \mathrm{E}+00$ | $0.000 \mathrm{E}+00$. | . | * | . |
| $1.000 \mathrm{E}-03$ | $5.487 \mathrm{E}+00$ | . | * | . |
| $2.000 \mathrm{E}-03$ | $1.025 \mathrm{E}+01$ | . | . | * |
| 3.000E-03 | $1.350 \mathrm{E}+01$ | . | . | . * |
| 4.000E-03 | $1.488 \mathrm{E}+01$ | . | . | . * |
| $5.000 \mathrm{E}-03$ | $1.425 \mathrm{E}+01$ | . | . | . * |
| $6.000 \mathrm{E}-03$ | $1.150 \mathrm{E}+01$ | . | . | * |
| $7.000 \mathrm{E}-03$ | $7.184 \mathrm{E}+00$ | . | * | . |
| $8.000 \mathrm{E}-03$ | $1.879 \mathrm{E}+00$ | . | * | . |
| $9.000 \mathrm{E}-03$ | $-3.714 \mathrm{E}+00$ | * | . | - |




### 7.8.5 Simple AC resistor-capacitor circuit



The .ac card specifies the points of ac analysis from 60 Hz to 60 Hz , at a single point. This card, of course, is a bit more useful for multi-frequency analysis, where a range of frequencies can be analyzed in steps. The .print card outputs the AC voltage between nodes 1 and 2 , and the AC voltage between node 2 and ground.

## Netlist:

Demo of a simple AC circuit
v1 10 ac 12 sin
r1 1230
c1 $20100 u$
.ac lin 16060
.print ac $v(1,2) \mathrm{v}(2)$
.end

## Output:

| freq | $v(1,2)$ | $v(2)$ |
| :--- | :--- | :--- |
| $6.000 \mathrm{E}+01$ | $8.990 \mathrm{E}+00$ | $7.949 \mathrm{E}+00$ |

### 7.8.6 Low-pass filter



This low-pass filter blocks AC and passes DC to the $\mathrm{R}_{\text {load }}$ resistor. Typical of a filter used to suppress ripple from a rectifier circuit, it actually has a resonant frequency, technically making it a band-pass filter. However, it works well anyway to pass DC and block the high-frequency harmonics generated by the AC-to-DC rectification process. Its performance is measured with an AC source sweeping from 500 Hz to 15 kHz . If desired, the .print card can be substituted or supplemented with a .plot card to show AC voltage at node 4 graphically.

## Netlist:

Lowpass filter
v1 21 ac 24 sin
v2 10 dc 24
rload 401 k
1123100 m
1234250 m
c1 $30100 u$
.ac lin 30500 15k
.print ac v(4)
.plot ac v(4)
.end

| freq | v (4) |
| :--- | :--- |
| $5.000 \mathrm{E}+02$ | $1.935 \mathrm{E}-01$ |
| $1.000 \mathrm{E}+03$ | $3.275 \mathrm{E}-02$ |
| $1.500 \mathrm{E}+03$ | $1.057 \mathrm{E}-02$ |
| $2.000 \mathrm{E}+03$ | $4.614 \mathrm{E}-03$ |
| $2.500 \mathrm{E}+03$ | $2.402 \mathrm{E}-03$ |
| $3.000 \mathrm{E}+03$ | $1.403 \mathrm{E}-03$ |
| $3.500 \mathrm{E}+03$ | $8.884 \mathrm{E}-04$ |
| $4.000 \mathrm{E}+03$ | $5.973 \mathrm{E}-04$ |
| $4.500 \mathrm{E}+03$ | $4.206 \mathrm{E}-04$ |
| $5.000 \mathrm{E}+03$ | $3.072 \mathrm{E}-04$ |
| $5.500 \mathrm{E}+03$ | $2.311 \mathrm{E}-04$ |
| $6.000 \mathrm{E}+03$ | $1.782 \mathrm{E}-04$ |
| $6.500 \mathrm{E}+03$ | $1.403 \mathrm{E}-04$ |
| $7.000 \mathrm{E}+03$ | $1.124 \mathrm{E}-04$ |
| $7.500 \mathrm{E}+03$ | $9.141 \mathrm{E}-05$ |
| $8.000 \mathrm{E}+03$ | $7.536 \mathrm{E}-05$ |
| $8.500 \mathrm{E}+03$ | $6.285 \mathrm{E}-05$ |
| $9.000 \mathrm{E}+03$ | $5.296 \mathrm{E}-05$ |
| $9.500 \mathrm{E}+03$ | $4.504 \mathrm{E}-05$ |
| $1.000 \mathrm{E}+04$ | $3.863 \mathrm{E}-05$ |
| $1.050 \mathrm{E}+04$ | $3.337 \mathrm{E}-05$ |
| $1.100 \mathrm{E}+04$ | $2.903 \mathrm{E}-05$ |
| $1.150 \mathrm{E}+04$ | $2.541 \mathrm{E}-05$ |
| $1.200 \mathrm{E}+04$ | $2.237 \mathrm{E}-05$ |
| $1.250 \mathrm{E}+04$ | $1.979 \mathrm{E}-05$ |


| $1.300 \mathrm{E}+04$ | $1.760 \mathrm{E}-05$ |
| :--- | :--- |
| $1.350 \mathrm{E}+04$ | $1.571 \mathrm{E}-05$ |
| $1.400 \mathrm{E}+04$ | $1.409 \mathrm{E}-05$ |
| $1.450 \mathrm{E}+04$ | $1.268 \mathrm{E}-05$ |
| $1.500 \mathrm{E}+04$ | $1.146 \mathrm{E}-05$ |



### 7.8.7 Multiple-source AC network



One of the idiosyncrasies of SPICE is its inability to handle any loop in a circuit exclusively composed of series voltage sources and inductors. Therefore, the "loop" of $\mathrm{V}_{1}-\mathrm{L}_{1}-\mathrm{L}_{2}-\mathrm{V}_{2}-\mathrm{V}_{1}$ is unacceptable. To get around this, I had to insert a low-resistance resistor somewhere in that loop to break it up. Thus, we have $\mathrm{R}_{\text {bogus }}$ between 3 and 4 (with 1 pico-ohm of resistance), and $\mathrm{V}_{2}$ between 4 and 0 . The circuit above is the original design, while the circuit below has $\mathrm{R}_{\text {bogus }}$ inserted to avoid the SPICE error.


## Netlist:

Multiple ac source
v1 10 ac 550 sin
v2 40 ac 4325 sin
1112450 m
c1 20330 u
1223 150m

```
rbogus 3 4 1e-12
.ac lin 1 30 30
.print ac v(2)
.end
```


## Output:

freq $\quad v(2)$
$3.000 \mathrm{E}+01 \quad 1.413 \mathrm{E}+02$

### 7.8.8 AC phase shift demonstration



The currents through each leg are indicated by the voltage drops across each respective shunt resistor ( $1 \mathrm{amp}=1$ volt through $1 \Omega$ ), output by the $\mathrm{v}(1,2)$ and $\mathrm{v}(1,3)$ terms of the .print card. The phase of the currents through each leg are indicated by the phase of the voltage drops across each respective shunt resistor, output by the $v p(1,2)$ and $v p(1,3)$ terms in the .print card.

## Netlist:

phase shift
v1 10 ac 4 sin
rshunt1 121
rshunt2 131
11201
r1 $306.3 k$
.ac lin 110001000
.print ac $v(1,2) \mathrm{v}(1,3) \mathrm{vp}(1,2) \mathrm{vp}(1,3)$
.end

## Output:

| freq | $v(1,2)$ | $v(1,3)$ | $v p(1,2)$ | $v p(1,3)$ |
| :--- | :--- | :--- | :---: | :--- |
| $1.000 \mathrm{E}+03$ | $6.366 \mathrm{E}-04$ | $6.349 \mathrm{E}-04$ | $-9.000 \mathrm{E}+01$ | $0.000 \mathrm{E}+00$ |

### 7.8.9 Transformer circuit



SPICE understands transformers as a set of mutually coupled inductors. Thus, to simulate a transformer in SPICE, you must specify the primary and secondary windings as separate inductors, then instruct SPICE to link them together with a "k" card specifying the coupling constant. For ideal transformer simulation, the coupling constant would be unity (1). However, SPICE can't handle this value, so we use something like 0.999 as the coupling factor.

Note that all winding inductor pairs must be coupled with their own k cards in order for the simulation to work properly. For a two-winding transformer, a single k card will suffice. For a three-winding transformer, three k cards must be specified (to $\operatorname{link} \mathrm{L}_{1}$ with $\mathrm{L}_{2}, \mathrm{~L}_{2}$ with $\mathrm{L}_{3}$, and $\mathrm{L}_{1}$ with $\mathrm{L}_{3}$ ).

The $\mathrm{L}_{1} / \mathrm{L}_{2}$ inductance ratio of 100:1 provides a $10: 1$ step-down voltage transformation ratio. With 120 volts in we should see 12 volts out of the $L_{2}$ winding. The $L_{1} / L_{3}$ inductance ratio of 100:25 (4:1) provides a $2: 1$ step-down voltage transformation ratio, which should give us 60 volts out of the $\mathrm{L}_{3}$ winding with 120 volts in.

## Netlist:

```
transformer
```

v1 10 ac 120 sin
rbogus0 $161 \mathrm{e}-3$
1160100
12241
133525
k1 11120.999
k2 12130.999
k3 11130.999
r1 241000
r2 351000
rbogus1 501 e 10
rbogus2 40 1e10
.ac lin 16060
. print ac $v(1,0) \mathrm{v}(2,0) \mathrm{v}(3,0)$
.end

## Output:

| freq | $v(1)$ | $v(2)$ | $v(3)$ |
| :--- | :--- | :--- | :--- |
| $6.000 \mathrm{E}+01$ | $1.200 \mathrm{E}+02$ | $1.199 \mathrm{E}+01$ | $5.993 \mathrm{E}+01$ |

In this example, $\mathrm{R}_{\text {bogus } 0}$ is a very low-value resistor, serving to break up the source/inductor loop of $\mathrm{V}_{1} / \mathrm{L}_{1} . \mathrm{R}_{\text {bogus } 1}$ and $\mathrm{R}_{\text {bogus } 2}$ are very high-value resistors necessary to provide DC paths to ground on each of the isolated circuits. Note as well that one side of the primary circuit is directly grounded. Without these ground references, SPICE will produce errors!

### 7.8.10 Full-wave bridge rectifier



Diodes, like all semiconductor components in SPICE, must be modeled so that SPICE knows all the nitty-gritty details of how they're supposed to work. Fortunately, SPICE comes with a few generic models, and the diode is the most basic. Notice the .model card which simply specifies "d" as the generic diode model for mod1. Again, since we're plotting the waveforms here, we need to specify all parameters of the AC source in a single card and print/plot all values using the .tran option.

## Netlist:

fullwave bridge rectifier
v1 $10 \sin (0156000)$
rload $1010 k$
d1 $12 \bmod 1$
d2 $02 \bmod 1$
d3 $31 \bmod 1$
d4 $30 \bmod 1$
.model mod1 d
.tran . 5 m 25m
. plot tran $v(1,0) \mathrm{v}(2,3)$
.end

## Output:

legend:
*: v(1)
$+: v(2,3)$
time $v(1)$
(*)--------- -2.000E+01 $-1.000 \mathrm{E}+01 \quad 0.000 \mathrm{E}+00 \quad 1.000 \mathrm{E}+01 \quad 2.000 \mathrm{E}+01$


```
2.200E-02 1.344E+01 . . . . \(+\quad+\)
\(2.250 \mathrm{E}-021.195 \mathrm{E}+01\).
\(2.300 \mathrm{E}-02 \quad 1.016 \mathrm{E}+01\).
\(2.350 \mathrm{E}-02 \quad 7.917 \mathrm{E}+00\).
\(2.400 \mathrm{E}-02 \quad 5.460 \mathrm{E}+00\).
\(2.450 \mathrm{E}-02\) 2.809E+00 . . \(+\quad\). \(\quad\).
\(2.500 \mathrm{E}-02\)-8.297E-04 . \(+\quad\) * .
```


### 7.8.11 Common-base BJT transistor amplifier



This analysis sweeps the input voltage (Vin) from 0 to 5 volts in 0.1 volt increments, then prints out the voltage between the collector and emitter leads of the transistor $\mathrm{v}(2,3)$. The transistor (Q1) is an NPN with a forward Beta of 50 .

## Netlist:

```
Common-base BJT amplifier
vsupply 1 0 dc 24
vin 0 4 dc
rc 1 2 800
re 3 4 100
q1 2 0 3 mod1
.model mod1 npn bf=50
.dc vin 0 5 0.1
.print dc v(2,3)
.plot dc v(2,3)
.end
```


## Output:

| vin | $v(2,3)$ |
| :--- | :--- |
| $0.000 \mathrm{E}+00$ | $2.400 \mathrm{E}+01$ |
| $1.000 \mathrm{E}-01$ | $2.410 \mathrm{E}+01$ |
| $2.000 \mathrm{E}-01$ | $2.420 \mathrm{E}+01$ |
| $3.000 \mathrm{E}-01$ | $2.430 \mathrm{E}+01$ |
| $4.000 \mathrm{E}-01$ | $2.440 \mathrm{E}+01$ |
| $5.000 \mathrm{E}-01$ | $2.450 \mathrm{E}+01$ |


| $6.000 \mathrm{E}-01$ | $2.460 \mathrm{E}+01$ |
| :--- | :--- |
| $7.000 \mathrm{E}-01$ | $2.466 \mathrm{E}+01$ |
| $8.000 \mathrm{E}-01$ | $2.439 \mathrm{E}+01$ |
| $9.000 \mathrm{E}-01$ | $2.383 \mathrm{E}+01$ |
| $1.000 \mathrm{E}+00$ | $2.317 \mathrm{E}+01$ |
| $1.100 \mathrm{E}+00$ | $2.246 \mathrm{E}+01$ |
| $1.200 \mathrm{E}+00$ | $2.174 \mathrm{E}+01$ |
| $1.300 \mathrm{E}+00$ | $2.101 \mathrm{E}+01$ |
| $1.400 \mathrm{E}+00$ | $2.026 \mathrm{E}+01$ |
| $1.500 \mathrm{E}+00$ | $1.951 \mathrm{E}+01$ |
| $1.600 \mathrm{E}+00$ | $1.876 \mathrm{E}+01$ |
| $1.700 \mathrm{E}+00$ | $1.800 \mathrm{E}+01$ |
| $1.800 \mathrm{E}+00$ | $1.724 \mathrm{E}+01$ |
| $1.900 \mathrm{E}+00$ | $1.648 \mathrm{E}+01$ |
| $2.000 \mathrm{E}+00$ | $1.572 \mathrm{E}+01$ |
| $2.100 \mathrm{E}+00$ | $1.495 \mathrm{E}+01$ |
| $2.200 \mathrm{E}+00$ | $1.418 \mathrm{E}+01$ |
| $2.300 \mathrm{E}+00$ | $1.342 \mathrm{E}+01$ |
| $2.400 \mathrm{E}+00$ | $1.265 \mathrm{E}+01$ |
| $2.500 \mathrm{E}+00$ | $1.188 \mathrm{E}+01$ |
| $2.600 \mathrm{E}+00$ | $1.110 \mathrm{E}+01$ |
| $2.700 \mathrm{E}+00$ | $1.033 \mathrm{E}+01$ |
| $2.800 \mathrm{E}+00$ | $9.560 \mathrm{E}+00$ |
| $2.900 \mathrm{E}+00$ | $8.787 \mathrm{E}+00$ |
| $3.000 \mathrm{E}+00$ | $8.014 \mathrm{E}+00$ |
| $3.100 \mathrm{E}+00$ | $7.240 \mathrm{E}+00$ |
| $3.200 \mathrm{E}+00$ | $6.465 \mathrm{E}+00$ |
| $3.300 \mathrm{E}+00$ | $5.691 \mathrm{E}+00$ |
| $3.400 \mathrm{E}+00$ | $4.915 \mathrm{E}+00$ |
| $3.500 \mathrm{E}+00$ | $4.140 \mathrm{E}+00$ |
| $3.600 \mathrm{E}+00$ | $3.364 \mathrm{E}+00$ |
| $3.700 \mathrm{E}+00$ | $2.588 \mathrm{E}+00$ |
| $3.800 \mathrm{E}+00$ | $1.811 \mathrm{E}+00$ |
| $3.900 \mathrm{E}+00$ | $1.034 \mathrm{E}+00$ |
| $4.000 \mathrm{E}+00$ | $2.587 \mathrm{E}-01$ |
| $4.100 \mathrm{E}+00$ | $9.744 \mathrm{E}-02$ |
| $4.200 \mathrm{E}+00$ | $7.815 \mathrm{E}-02$ |
| $4.300 \mathrm{E}+00$ | $6.806 \mathrm{E}-02$ |
| $4.400 \mathrm{E}+00$ | $6.141 \mathrm{E}-02$ |
| $4.500 \mathrm{E}+00$ | $5.657 \mathrm{E}-02$ |
| $4.600 \mathrm{E}+00$ | $5.281 \mathrm{E}-02$ |
| $4.700 \mathrm{E}+00$ | $4.981 \mathrm{E}-02$ |
| $4.800 \mathrm{E}+00$ | $4.734 \mathrm{E}-02$ |
| $4.900 \mathrm{E}+00$ | $4.525 \mathrm{E}-02$ |
| $5.000 \mathrm{E}+00$ | $4.346 \mathrm{E}-02$ |



| $4.400 \mathrm{E}+00$ | 6.141E-02 * | . . | . |
| :---: | :---: | :---: | :---: |
| $4.500 \mathrm{E}+00$ | 5.657E-02 * | . . |  |
| $4.600 \mathrm{E}+00$ | 5.281E-02 * | . . |  |
| $4.700 \mathrm{E}+00$ | 4.981E-02 * | . . |  |
| $4.800 \mathrm{E}+00$ | 4.734E-02 * | - . |  |
| $4.900 \mathrm{E}+00$ | 4.525E-02 * | . . | . |
| $5.000 \mathrm{E}+00$ | 4.346E-02 * | - . |  |

### 7.8.12 Common-source JFET amplifier with self-bias



Netlist:
common source jfet amplifier
vin $10 \sin (016000)$
vdd 30 dc 20
rdrain $3210 k$
rsource 40 1k
j1 $214 \bmod 1$
.model mod1 njf
.tran 1 m 30 m
.plot tran $v(2,0) \mathrm{v}(1,0)$
.end
Output:
legend:
*: v(2)
$+: \mathrm{v}(1)$
time $v(2)$
$\begin{array}{llllll}(*)--------- & 1.400 \mathrm{E}+01 & 1.600 \mathrm{E}+01 & 1.800 \mathrm{E}+01 & 2.000 \mathrm{E}+01 & 2.200 \mathrm{E}+01\end{array}$
(+)----------1.000E+00 -5.000E-01 $0.000 \mathrm{E}+00 \quad 5.000 \mathrm{E}-01 \quad 1.000 \mathrm{E}+00$

-     -         -             -                 -                     -                         -                             -                                 -                                     -                                         -                                             -                                                 -                                                     -                                                         -                                                             -                                                                 -                                                                     -                                                                         -                                                                             -                                                                                 -                                                                                     -                                                                                         -                                                                                             -                                                                                                 -                                                                                                     -                                                                                                         -                                                                                                             - 



### 7.8.13 Inverting op-amp circuit



To simulate an ideal operational amplifier in SPICE, we use a voltage-dependent voltage source as a differential amplifier with extremely high gain. The "e" card sets up the dependent voltage source with four nodes, 3 and 0 for voltage output, and 1 and 0 for voltage input. No power supply is needed for the dependent voltage source, unlike a real operational amplifier. The voltage gain is set at 999,000 in this case. The input voltage source $\left(\mathrm{V}_{1}\right)$ sweeps from 0 to 3.5 volts in 0.05 volt steps.

## Netlist:

Inverting opamp
v1 20 dc
e $3001999 k$
r1 31 3.29k
r2 12 1.18k
.dc v1 03.50 .05
.print dc v(3,0)
.end

## Output:

| $v 1$ | $v(3)$ |
| :--- | ---: |
| $0.000 \mathrm{E}+00$ | $0.000 \mathrm{E}+00$ |
| $5.000 \mathrm{E}-02$ | $-1.394 \mathrm{E}-01$ |
| $1.000 \mathrm{E}-01$ | $-2.788 \mathrm{E}-01$ |
| $1.500 \mathrm{E}-01$ | $-4.182 \mathrm{E}-01$ |
| $2.000 \mathrm{E}-01$ | $-5.576 \mathrm{E}-01$ |
| $2.500 \mathrm{E}-01$ | $-6.970 \mathrm{E}-01$ |
| $3.000 \mathrm{E}-01$ | $-8.364 \mathrm{E}-01$ |
| $3.500 \mathrm{E}-01$ | $-9.758 \mathrm{E}-01$ |
| $4.000 \mathrm{E}-01$ | $-1.115 \mathrm{E}+00$ |
| $4.500 \mathrm{E}-01$ | $-1.255 \mathrm{E}+00$ |
| $5.000 \mathrm{E}-01$ | $-1.394 \mathrm{E}+00$ |
| $5.500 \mathrm{E}-01$ | $-1.533 \mathrm{E}+00$ |
| $6.000 \mathrm{E}-01$ | $-1.673 \mathrm{E}+00$ |
| $6.500 \mathrm{E}-01$ | $-1.812 \mathrm{E}+00$ |
| $7.000 \mathrm{E}-01$ | $-1.952 \mathrm{E}+00$ |
| $7.500 \mathrm{E}-01$ | $-2.091 \mathrm{E}+00$ |
| $8.000 \mathrm{E}-01$ | $-2.231 \mathrm{E}+00$ |
| $8.500 \mathrm{E}-01$ | $-2.370 \mathrm{E}+00$ |
| $9.000 \mathrm{E}-01$ | $-2.509 \mathrm{E}+00$ |
| $9.500 \mathrm{E}-01$ | $-2.649 \mathrm{E}+00$ |
| $1.000 \mathrm{E}+00$ | $-2.788 \mathrm{E}+00$ |
| $1.050 \mathrm{E}+00$ | $-2.928 \mathrm{E}+00$ |
| $1.100 \mathrm{E}+00$ | $-3.067 \mathrm{E}+00$ |
| $1.150 \mathrm{E}+00$ | $-3.206 \mathrm{E}+00$ |
| $1.200 \mathrm{E}+00$ | $-3.346 \mathrm{E}+00$ |
| $1.250 \mathrm{E}+00$ | $-3.485 \mathrm{E}+00$ |
| $1.300 \mathrm{E}+00$ | $-3.625 \mathrm{E}+00$ |


| $1.350 \mathrm{E}+00$ | $-3.764 \mathrm{E}+00$ |
| :--- | :--- |
| $1.400 \mathrm{E}+00$ | $-3.903 \mathrm{E}+00$ |
| $1.450 \mathrm{E}+00$ | $-4.043 \mathrm{E}+00$ |
| $1.500 \mathrm{E}+00$ | $-4.182 \mathrm{E}+00$ |
| $1.550 \mathrm{E}+00$ | $-4.322 \mathrm{E}+00$ |
| $1.600 \mathrm{E}+00$ | $-4.461 \mathrm{E}+00$ |
| $1.650 \mathrm{E}+00$ | $-4.600 \mathrm{E}+00$ |
| $1.700 \mathrm{E}+00$ | $-4.740 \mathrm{E}+00$ |
| $1.750 \mathrm{E}+00$ | $-4.879 \mathrm{E}+00$ |
| $1.800 \mathrm{E}+00$ | $-5.019 \mathrm{E}+00$ |
| $1.850 \mathrm{E}+00$ | $-5.158 \mathrm{E}+00$ |
| $1.900 \mathrm{E}+00$ | $-5.297 \mathrm{E}+00$ |
| $1.950 \mathrm{E}+00$ | $-5.437 \mathrm{E}+00$ |
| $2.000 \mathrm{E}+00$ | $-5.576 \mathrm{E}+00$ |
| $2.050 \mathrm{E}+00$ | $-5.716 \mathrm{E}+00$ |
| $2.100 \mathrm{E}+00$ | $-5.855 \mathrm{E}+00$ |
| $2.150 \mathrm{E}+00$ | $-5.994 \mathrm{E}+00$ |
| $2.200 \mathrm{E}+00$ | $-6.134 \mathrm{E}+00$ |
| $2.250 \mathrm{E}+00$ | $-6.273 \mathrm{E}+00$ |
| $2.300 \mathrm{E}+00$ | $-6.413 \mathrm{E}+00$ |
| $2.350 \mathrm{E}+00$ | $-6.552 \mathrm{E}+00$ |
| $2.400 \mathrm{E}+00$ | $-6.692 \mathrm{E}+00$ |
| $2.450 \mathrm{E}+00$ | $-6.831 \mathrm{E}+00$ |
| $2.500 \mathrm{E}+00$ | $-6.970 \mathrm{E}+00$ |
| $2.550 \mathrm{E}+00$ | $-7.110 \mathrm{E}+00$ |
| $2.600 \mathrm{E}+00$ | $-7.249 \mathrm{E}+00$ |
| $2.650 \mathrm{E}+00$ | $-7.389 \mathrm{E}+00$ |
| $2.700 \mathrm{E}+00$ | $-7.528 \mathrm{E}+00$ |
| $2.750 \mathrm{E}+00$ | $-7.667 \mathrm{E}+00$ |
| $2.800 \mathrm{E}+00$ | $-7.807 \mathrm{E}+00$ |
| $2.850 \mathrm{E}+00$ | $-7.946 \mathrm{E}+00$ |
| $2.900 \mathrm{E}+00$ | $-8.086 \mathrm{E}+00$ |
| $2.950 \mathrm{E}+00$ | $-8.225 \mathrm{E}+00$ |
| $3.000 \mathrm{E}+00$ | $-8.364 \mathrm{E}+00$ |
| $3.050 \mathrm{E}+00$ | $-8.504 \mathrm{E}+00$ |
| $3.100 \mathrm{E}+00$ | $-8.643 \mathrm{E}+00$ |
| $3.150 \mathrm{E}+00$ | $-8.783 \mathrm{E}+00$ |
| $3.200 \mathrm{E}+00$ | $-8.922 \mathrm{E}+00$ |
| $3.250 \mathrm{E}+00$ | $-9.061 \mathrm{E}+00$ |
| $3.300 \mathrm{E}+00$ | $-9.201 \mathrm{E}+00$ |
| $3.350 \mathrm{E}+00$ | $-9.340 \mathrm{E}+00$ |
| $3.400 \mathrm{E}+00$ | $-9.480 \mathrm{E}+00$ |
| $3.450 \mathrm{E}+00$ | $-9.619 \mathrm{E}+00$ |
| 3.500 | $-9.758 \mathrm{E}+00$ |

### 7.8.14 Noninverting op-amp circuit



Another example of a SPICE quirk: since the dependent voltage source "e" isn't considered a load to voltage source $\mathrm{V}_{1}$, SPICE interprets $\mathrm{V}_{1}$ to be open-circuited and will refuse to analyze it. The fix is to connect $\mathrm{R}_{\text {bogus }}$ in parallel with $\mathrm{V}_{1}$ to act as a DC load. Being directly connected across $\mathrm{V}_{1}$, the resistance of $\mathrm{R}_{\text {bogus }}$ is not crucial to the operation of the circuit, so $10 \mathrm{k} \Omega$ will work fine. I decided not to sweep the $V_{1}$ input voltage at all in this circuit for the sake of keeping the netlist and output listing simple.

## Netlist:

```
noninverting opamp
v1 2 0 dc 5
rbogus 2 0 10k
e 3 0 2 1 999k
r1 3 1 20k
r2 1 0 10k
.end
```


## Output:

| node | voltage | node | voltage | node | voltage |
| :---: | :--- | :---: | :--- | :---: | :---: |
| $\left(\begin{array}{c}1)\end{array}\right.$ | 5.0000 | $(2)$ | 5.0000 | $(3)$ | 15.0000 |

### 7.8.15 Instrumentation amplifier



Note the very high-resistance $\mathrm{R}_{\text {bogus } 1}$ and $\mathrm{R}_{\text {bogus } 2}$ resistors in the netlist (not shown in schematic for brevity) across each input voltage source, to keep SPICE from thinking $\mathrm{V}_{1}$ and $\mathrm{V}_{2}$ were opencircuited, just like the other op-amp circuit examples.

## Netlist:

Instrumentation amplifier
v1 10
rbogus1 109 e 12
v2 40 dc 5
rbogus2 40 9e12
e1 3012 999k
e2 6045 999k
e3 9087 999k
rload 9010 k
r1 23 10k
rgain 25 10k
r2 56 10k
r3 37 10k
r4 79 10k
r5 68 10k
r6 80 10k
.dc v1 0101
. print dc v(9) v(3,6)
.end
Output:
v1

$$
\mathrm{v}(9) \quad \mathrm{v}(3,6)
$$

| $0.000 \mathrm{E}+00$ | $1.500 \mathrm{E}+01$ | $-1.500 \mathrm{E}+01$ |
| ---: | ---: | ---: |
| $1.000 \mathrm{E}+00$ | $1.200 \mathrm{E}+01$ | $-1.200 \mathrm{E}+01$ |
| $2.000 \mathrm{E}+00$ | $9.000 \mathrm{E}+00$ | $-9.000 \mathrm{E}+00$ |
| $3.000 \mathrm{E}+00$ | $6.000 \mathrm{E}+00$ | $-6.000 \mathrm{E}+00$ |
| $4.000 \mathrm{E}+00$ | $3.000 \mathrm{E}+00$ | $-3.000 \mathrm{E}+00$ |
| $5.000 \mathrm{E}+00$ | $9.955 \mathrm{E}-11$ | $-9.956 \mathrm{E}-11$ |
| $6.000 \mathrm{E}+00$ | $-3.000 \mathrm{E}+00$ | $3.000 \mathrm{E}+00$ |
| $7.000 \mathrm{E}+00$ | $-6.000 \mathrm{E}+00$ | $6.000 \mathrm{E}+00$ |
| $8.000 \mathrm{E}+00$ | $-9.000 \mathrm{E}+00$ | $9.000 \mathrm{E}+00$ |
| $9.000 \mathrm{E}+00$ | $-1.200 \mathrm{E}+01$ | $1.200 \mathrm{E}+01$ |
| $1.000 \mathrm{E}+01$ | $-1.500 \mathrm{E}+01$ | $1.500 \mathrm{E}+01$ |

### 7.8.16 Op-amp integrator with sinewave input



Netlist:
Integrator with sinewave input
vin $10 \sin (0156000)$
r1 12 10k
c1 23 150u ic=0
e $3002999 k$
.tran 1 m 30 m uic
.plot tran $v(1,0) \mathrm{v}(3,0)$
.end

## Output:

legend:
*: v(1)
$+: \mathrm{v}(3)$
time $\quad v(1)$
(*)-------- -2.000E+01 $-1.000 \mathrm{E}+01 \quad 0.000 \mathrm{E}+00 \quad 1.000 \mathrm{E}+01$

7.8.17 Op-amp integrator with squarewave input


Netlist:
Integrator with squarewave input
vin 10 pulse ( -1100010 m 20 m )
r1 12 1k
c1 23 150u ic=0
e $3002999 k$
.tran 1 m 50 m uic
. plot tran $\mathrm{v}(1,0) \mathrm{v}(3,0)$
.end
Output:
legend:
*: v(1)
$+: \mathrm{v}(3)$
time $\mathrm{v}(1)$
$\begin{array}{llllll}(*)--------1.000 \mathrm{E}+00 & -5.000 \mathrm{E}-01 & 0.000 \mathrm{E}+00 & 5.000 \mathrm{E}-01 & 1.000 \mathrm{E}+00 \\ (+)-------1.000 \mathrm{E}-01 & -5.000 \mathrm{E}-02 & 0.000 \mathrm{E}+00 & 5.000 \mathrm{E}-02 & 1.000 \mathrm{E}-01\end{array}$



## Chapter 8

## TROUBLESHOOTING THEORY AND PRACTICE

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## 8.1

Perhaps the most valuable but difficult-to-learn skill any technical person could have is the ability to troubleshoot a system. For those unfamiliar with the term, troubleshooting means the act of pinpointing and correcting problems in any kind of system. For an auto mechanic, this means determining and fixing problems in cars based on the car's behavior. For a doctor, this means correctly diagnosing a patient's malady and prescribing a cure. For a business expert, this means identifying the source(s) of inefficiency in a corporation and recommending corrective measures.

Troubleshooters must be able to determine the cause or causes of a problem simply by examining its effects. Rarely does the source of a problem directly present itself for all to see. Cause/effect relationships are often complex, even for seemingly simple systems, and often the proficient troubleshooter is regarded by others as something of a miracle-worker for their ability to quickly discern the root cause of a problem. While some people are gifted with a natural talent for troubleshooting, it is a skill that can be learned like any other.

Sometimes the system to be analyzed is in so bad a state of affairs that there is no hope of ever getting it working again. When investigators sift through the wreckage of a crashed airplane, or when a doctor performs an autopsy, they must do their best to determine the cause of massive failure after the fact. Fortunately, the task of the troubleshooter is usually not this grim. Typically, a misbehaving system is still functioning to some degree and may be stimulated and adjusted by the troubleshooter as part of the diagnostic procedure. In this sense, troubleshooting is a lot like scientific method: determining cause/effect relationships by means of live experimentation.

Like science, troubleshooting is a mixture of standard procedure and personal creativity. There are certain procedures employed as tools to discern cause(s) from effects, but they are impotent if not coupled with a creative and inquisitive mind. In the course of troubleshooting, the troubleshooter may have to invent their own specific technique - adapted to the particular system they're working on - and/or modify tools to perform a special task. Creativity is necessary in examining a problem from different perspectives: learning to ask different questions when the "standard" questions don't lead to fruitful answers.

If there is one personality trait I've seen positively associated with excellent troubleshooting more than any other, it's technical curiosity. People fascinated by learning how things work, and who aren't discouraged by a challenging problem, tend to be better at troubleshooting than others. Richard Feynman, the late physicist who taught at Caltech for many years, illustrates to me the ultimate troubleshooting personality. Reading any of his (auto)biographical books is both educating and entertaining, and I recommend them to anyone seeking to develop their own scientific reasoning/troubleshooting skills.

### 8.2 Questions to ask before proceeding

- Has the system ever worked before? If yes, has anything happened to it since then that could cause the problem?
- Has this system proven itself to be prone to certain types of failure?
- How urgent is the need for repair?
- What are the safety concerns, before I start troubleshooting?
- What are the process quality concerns, before I start troubleshooting (what can I do without causing interruptions in production)?

These preliminary questions are not trivial. Indeed, they are essential to expedient and safe troubleshooting. They are especially important when the system to be trouble-shot is large, dangerous, and/or expensive.

Sometimes the troubleshooter will be required to work on a system that is still in full operation (perhaps the ultimate example of this is a doctor diagnosing a live patient). Once the cause or causes are determined to a high degree of certainty, there is the step of corrective action. Correcting a system fault without significantly interrupting the operation of the system can be very challenging, and it deserves thorough planning.

When there is high risk involved in taking corrective action, such as is the case with performing surgery on a patient or making repairs to an operating process in a chemical plant, it is essential for the worker(s) to plan ahead for possible trouble. One question to ask before proceeding with repairs is, "how and at what point(s) can I abort the repairs if something goes wrong?" In risky situations, it is vital to have planned "escape routes" in your corrective action, just in case things do not go as planned. A surgeon operating on a patient knows if there are any "points of no return" in such a procedure, and stops to re-check the patient before proceeding past those points. He or she also knows how to "back out" of a surgical procedure at those points if needed.

### 8.3 General troubleshooting tips

When first approaching a failed or otherwise misbehaving system, the new troubleshooter often doesn't know where to begin. The following strategies are not exhaustive by any means, but provide the troubleshooter with a simple checklist of questions to ask in order to start isolating the problem.

As tips, these troubleshooting suggestions are not comprehensive procedures: they serve as starting points only for the troubleshooting process. An essential part of expedient troubleshooting is probability assessment, and these tips help the troubleshooter determine which possible points of failure are more or less likely than others. Final isolation of the system failure is usually determined through more specific techniques (outlined in the next section - Specific Troubleshooting Techniques).

### 8.3.1 Prior occurrence

If this device or process has been historically known to fail in a certain particular way, and the conditions leading to this common failure have not changed, check for this "way" first. A corollary to this troubleshooting tip is the directive to keep detailed records of failure. Ideally, a computerbased failure $\log$ is optimal, so that failures may be referenced by and correlated to a number of factors such as time, date, and environmental conditions.

Example: The car's engine is overheating. The last two times this happened, the cause was low coolant level in the radiator.

What to do: Check the coolant level first. Of course, past history by no means guarantees the present symptoms are caused by the same problem, but since this is more likely, it makes sense to check this first.

If, however, the cause of routine failure in a system has been corrected (i.e. the leak causing low coolant level in the past has been repaired), then this may not be a probable cause of trouble this time.

### 8.3.2 Recent alterations

If a system has been having problems immediately after some kind of maintenance or other change, the problems might be linked to those changes.

Example: The mechanic recently tuned my car's engine, and now I hear a rattling noise that I didn't hear before I took the car in for repair.

What to do: Check for something that may have been left loose by the mechanic after his or her tune-up work.

### 8.3.3 Function vs. non-function

If a system isn't producing the desired end result, look for what it is doing correctly; in other words, identify where the problem is not, and focus your efforts elsewhere. Whatever components or subsystems necessary for the properly working parts to function are probably okay. The degree of fault can often tell you what part of it is to blame.

Example: The radio works fine on the AM band, but not on the FM band.
What to do: Eliminate from the list of possible causes, anything in the radio necessary for the AM band's function. Whatever the source of the problem is, it is specific to the FM band and not to the AM band. This eliminates the audio amplifier, speakers, fuse, power supply, and almost all external wiring. Being able to eliminate sections of the system as possible failures reduces the scope of the problem and makes the rest of the troubleshooting procedure more efficient.

### 8.3.4 Hypothesize

Based on your knowledge of how a system works, think of various kinds of failures that would cause this problem (or these phenomena) to occur, and check for those failures (starting with the most likely based on circumstances, history, or knowledge of component weaknesses).

Example: The car's engine is overheating.
What to do: Consider possible causes for overheating, based on what you know of engine operation. Either the engine is generating too much heat, or not getting rid of the heat well enough (most likely the latter). Brainstorm some possible causes: a loose fan belt, clogged radiator, bad water pump, low coolant level, etc. Investigate each one of those possibilities before investigating alternatives.

### 8.4 Specific troubleshooting techniques

After applying some of the general troubleshooting tips to narrow the scope of a problem's location, there are techniques useful in further isolating it. Here are a few:

### 8.4.1 Swap identical components

In a system with identical or parallel subsystems, swap components between those subsystems and see whether or not the problem moves with the swapped component. If it does, you've just swapped the faulty component; if it doesn't, keep searching!

This is a powerful troubleshooting method, because it gives you both a positive and a negative indication of the swapped component's fault: when the bad part is exchanged between identical systems, the formerly broken subsystem will start working again and the formerly good subsystem will fail.

I was once able to troubleshoot an elusive problem with an automotive engine ignition system using this method: I happened to have a friend with an automobile sharing the exact same model of ignition system. We swapped parts between the engines (distributor, spark plug wires, ignition coil - one at a time) until the problem moved to the other vehicle. The problem happened to be a "weak" ignition coil, and it only manifested itself under heavy load (a condition that could not be simulated in my garage). Normally, this type of problem could only be pinpointed using an ignition system analyzer (or oscilloscope) and a dynamometer to simulate loaded driving conditions. This technique, however, confirmed the source of the problem with $100 \%$ accuracy, using no diagnostic equipment whatsoever.

Occasionally you may swap a component and find that the problem still exists, but has changed in some way. This tells you that the components you just swapped are somehow different (different calibration, different function), and nothing more. However, don't dismiss this information just because it doesn't lead you straight to the problem - look for other changes in the system as a whole as a result of the swap, and try to figure out what these changes tell you about the source of the problem.

An important caveat to this technique is the possibility of causing further damage. Suppose a component has failed because of another, less conspicuous failure in the system. Swapping the failed component with a good component will cause the good component to fail as well. For example, suppose that a circuit develops a short, which "blows" the protective fuse for that circuit. The blown fuse is not evident by inspection, and you don't have a meter to electrically test the fuse, so you decide to swap the suspect fuse with one of the same rating from a working circuit. As a result of this, the good fuse that you move to the shorted circuit blows as well, leaving you with two blown fuses and two non-working circuits. At least you know for certain that the original fuse was blown, because the circuit it was moved to stopped working after the swap, but this knowledge was gained only through the loss of a good fuse and the additional "down time" of the second circuit.

Another example to illustrate this caveat is the ignition system problem previously mentioned. Suppose that the "weak" ignition coil had caused the engine to backfire, damaging the muffler. If swapping ignition system components with another vehicle causes the problem to move to the other vehicle, damage may be done to the other vehicle's muffler as well. As a general rule, the technique of swapping identical components should be used only when there is minimal chance of causing additional damage. It is an excellent technique for isolating non-destructive problems.

Example 1: You're working on a CNC machine tool with $X, Y$, and $Z$-axis drives. The $Y$ axis is not working, but the $X$ and $Z$ axes are working. All three axes share identical components (feedback encoders, servo motor drives, servo motors).

What to do: Exchange these identical components, one at a time, Y axis and either one of the working axes (X or Z), and see after each swap whether or not the problem has moved with the swap.

Example 2: A stereo system produces no sound on the left speaker, but the right speaker works just fine.

What to do: Try swapping respective components between the two channels and see if the problem changes sides, from left to right. When it does, you've found the defective component. For instance, you could swap the speakers between channels: if the problem moves to the other side (i.e. the same speaker that was dead before is still dead, now that it's connected to the right channel cable) then you know that speaker is bad. If the problem stays on the same side (i.e. the speaker formerly silent is now producing sound after having been moved to the other side of the room and connected to the other cable), then you know the speakers are fine, and the problem must lie somewhere else (perhaps in the cable connecting the silent speaker to the amplifier, or in the amplifier itself).

If the speakers have been verified as good, then you could check the cables using the same method. Swap the cables so that each one now connects to the other channel of the amplifier and to the other speaker. Again, if the problem changes sides (i.e. now the right speaker is now "dead" and the left speaker now produces sound), then the cable now connected to the right speaker must be defective. If neither swap (the speakers nor the cables) causes the problem to change sides from left to right, then the problem must lie within the amplifier (i.e. the left channel output must be "dead").

### 8.4.2 Remove parallel components

If a system is composed of several parallel or redundant components which can be removed without crippling the whole system, start removing these components (one at a time) and see if things start to work again.

Example 1: A "star" topology communications network between several computers has failed. None of the computers are able to communicate with each other.

What to do: Try unplugging the computers, one at a time from the network, and see if the network starts working again after one of them is unplugged. If it does, then that last unplugged computer may be the one at fault (it may have been "jamming" the network by constantly outputting data or noise).

Example 2: A household fuse keeps blowing (or the breaker keeps tripping open) after a short amount of time.

What to do: Unplug appliances from that circuit until the fuse or breaker quits interrupting the circuit. If you can eliminate the problem by unplugging a single appliance, then that appliance might be defective. If you find that unplugging almost any appliance solves the problem, then the circuit may simply be overloaded by too many appliances, neither of them defective.

### 8.4.3 Divide system into sections and test those sections

In a system with multiple sections or stages, carefully measure the variables going in and out of each stage until you find a stage where things don't look right.

Example 1: A radio is not working (producing no sound at the speaker))
What to do: Divide the circuitry into stages: tuning stage, mixing stages, amplifier stage, all the way through to the speaker(s). Measure signals at test points between these stages and tell whether or not a stage is working properly.

Example 2: An analog summer circuit is not functioning properly.

## Analog summer circuit



What to do: I would test the passive averager network (the three resistors at the lower-left corner of the schematic) to see that the proper (averaged) voltage was seen at the noninverting input of the op-amp. I would then measure the voltage at the inverting input to see if it was the same as at the noninverting input (or, alternatively, measure the voltage difference between the two inputs of the op-amp, as it should be zero). Continue testing sections of the circuit (or just test points within the circuit) to see if you measure the expected voltages and currents.

### 8.4.4 Simplify and rebuild

Closely related to the strategy of dividing a system into sections, this is actually a design and fabrication technique useful for new circuits, machines, or systems. It's always easier begin the design and construction process in little steps, leading to larger and larger steps, rather than to build the whole thing at once and try to troubleshoot it as a whole.

Suppose that someone were building a custom automobile. He or she would be foolish to bolt all the parts together without checking and testing components and subsystems as they went along, expecting everything to work perfectly after it's all assembled. Ideally, the builder would check the proper operation of components along the way through the construction process: start and tune the engine before it's connected to the drivetrain, check for wiring problems before all the cover panels are put in place, check the brake system in the driveway before taking it out on the road, etc.

Countless times I've witnessed students build a complex experimental circuit and have trouble getting it to work because they didn't stop to check things along the way: test all resistors before
plugging them into place, make sure the power supply is regulating voltage adequately before trying to power anything with it, etc. It is human nature to rush to completion of a project, thinking that such checks are a waste of valuable time. However, more time will be wasted in troubleshooting a malfunctioning circuit than would be spent checking the operation of subsystems throughout the process of construction.

Take the example of the analog summer circuit in the previous section for example: what if it wasn't working properly? How would you simplify it and test it in stages? Well, you could reconnect the op-amp as a basic comparator and see if it's responsive to differential input voltages, and/or connect it as a voltage follower (buffer) and see if it outputs the same analog voltage as what is input. If it doesn't perform these simple functions, it will never perform its function in the summer circuit! By stripping away the complexity of the summer circuit, paring it down to an (almost) bare op-amp, you can test that component's functionality and then build from there (add resistor feedback and check for voltage amplification, then add input resistors and check for voltage summing), checking for expected results along the way.

### 8.4.5 Trap a signal

Set up instrumentation (such as a datalogger, chart recorder, or multimeter set on "record" mode) to monitor a signal over a period of time. This is especially helpful when tracking down intermittent problems, which have a way of showing up the moment you've turned your back and walked away.

This may be essential for proving what happens first in a fast-acting system. Many fast systems (especially shutdown "trip" systems) have a "first out" monitoring capability to provide this kind of data.

Example \#1: A turbine control system shuts automatically in response to an abnormal condition. By the time a technician arrives at the scene to survey the turbine's condition, however, everything is in a "down" state and it's impossible to tell what signal or condition was responsible for the initial shutdown, as all operating parameters are now "abnormal."

What to do: One technician I knew used a videocamera to record the turbine control panel, so he could see what happened (by indications on the gauges) first in an automatic-shutdown event. Simply by looking at the panel after the fact, there was no way to tell which signal shut the turbine down, but the videotape playback would show what happened in sequence, down to a frame-by-frame time resolution.

Example \#2: An alarm system is falsely triggering, and you suspect it may be due to a specific wire connection going bad. Unfortunately, the problem never manifests itself while you're watching $i t!$

What to do: Many modern digital multimeters are equipped with "record" settings, whereby they can monitor a voltage, current, or resistance over time and note whether that measurement deviates substantially from a regular value. This is an invaluable tool for use in "intermittent" electronic system failures.

### 8.5 Likely failures in proven systems

The following problems are arranged in order from most likely to least likely, top to bottom. This order has been determined largely from personal experience troubleshooting electrical and electronic problems in automotive, industry, and home applications. This order also assumes a circuit or system that has been proven to function as designed and has failed after substantial operation time. Problems experienced in newly assembled circuits and systems do not necessarily exhibit the same probabilities of occurrence.

### 8.5.1 Operator error

A frequent cause of system failure is error on the part of those human beings operating it. This cause of trouble is placed at the top of the list, but of course the actual likelihood depends largely on the particular individuals responsible for operation. When operator error is the cause of a failure, it is unlikely that it will be admitted prior to investigation. I do not mean to suggest that operators are incompetent and irresponsible - quite the contrary: these people are often your best teachers for learning system function and obtaining a history of failure - but the reality of human error cannot be overlooked. A positive attitude coupled with good interpersonal skills on the part of the troubleshooter goes a long way in troubleshooting when human error is the root cause of failure.

### 8.5.2 Bad wire connections

As incredible as this may sound to the new student of electronics, a high percentage of electrical and electronic system problems are caused by a very simple source of trouble: poor (i.e. open or shorted) wire connections. This is especially true when the environment is hostile, including such factors as high vibration and/or a corrosive atmosphere. Connection points found in any variety of plug-and-socket connector, terminal strip, or splice are at the greatest risk for failure. The category of "connections" also includes mechanical switch contacts, which can be thought of as a high-cycle connector. Improper wire termination lugs (such as a compression-style connector crimped on the end of a solid wire - a definite faux pas) can cause high-resistance connections after a period of trouble-free service.

It should be noted that connections in low-voltage systems tend to be far more troublesome than connections in high-voltage systems. The main reason for this is the effect of arcing across a discontinuity (circuit break) in higher-voltage systems tends to blast away insulating layers of dirt and corrosion, and may even weld the two ends together if sustained long enough. Low-voltage systems tend not to generate such vigorous arcing across the gap of a circuit break, and also tend to be more sensitive to additional resistance in the circuit. Mechanical switch contacts used in lowvoltage systems benefit from having the recommended minimum wetting current conducted through them to promote a healthy amount of arcing upon opening, even if this level of current is not necessary for the operation of other circuit components.

Although open failures tend to more common than shorted failures, "shorts" still constitute a substantial percentage of wiring failure modes. Many shorts are caused by degradation of wire insulation. This, again, is especially true when the environment is hostile, including such factors as high vibration, high heat, high humidity, or high voltage. It is rare to find a mechanical switch contact that is failed shorted, except in the case of high-current contacts where contact "welding"
may occur in overcurrent conditions. Shorts may also be caused by conductive buildup across terminal strip sections or the backs of printed circuit boards.

A common case of shorted wiring is the ground fault, where a conductor accidently makes contact with either earth or chassis ground. This may change the voltage(s) present between other conductors in the circuit and ground, thereby causing bizarre system malfunctions and/or personnel hazard.

### 8.5.3 Power supply problems

These generally consist of tripped overcurrent protection devices or damage due to overheating. Although power supply circuitry is usually less complex than the circuitry being powered, and therefore should figure to be less prone to failure on that basis alone, it generally handles more power than any other portion of the system and therefore must deal with greater voltages and/or currents. Also, because of its relative design simplicity, a system's power supply may not receive the engineering attention it deserves, most of the engineering focus devoted to more glamorous parts of the system.

### 8.5.4 Active components

Active components (amplification devices) tend to fail with greater regularity than passive (nonamplifying) devices, due to their greater complexity and tendency to amplify overvoltage/overcurrent conditions. Semiconductor devices are notoriously prone to failure due to electrical transient (voltage/current surge) overloading and thermal (heat) overloading. Electron tube devices are far more resistant to both of these failure modes, but are generally more prone to mechanical failures due to their fragile construction.

### 8.5.5 Passive components

Non-amplifying components are the most rugged of all, their relative simplicity granting them a statistical advantage over active devices. The following list gives an approximate relation of failure probabilities (again, top being the most likely and bottom being the least likely):

- Capacitors (shorted), especially electrolytic capacitors. The paste electrolyte tends to lose moisture with age, leading to failure. Thin dielectric layers may be punctured by overvoltage transients.
- Diodes open (rectifying diodes) or shorted (Zener diodes).
- Inductor and transformer windings open or shorted to conductive core. Failures related to overheating (insulation breakdown) are easily detected by smell.
- Resistors open, almost never shorted. Usually this is due to overcurrent heating, although it is less frequently caused by overvoltage transient (arc-over) or physical damage (vibration or impact). Resistors may also change resistance value if overheated!


### 8.6 Likely failures in unproven systems

"All men are liable to error;"
John Locke

Whereas the last section deals with component failures in systems that have been successfully operating for some time, this section concentrates on the problems plaguing brand-new systems. In this case, failure modes are generally not of the aging kind, but are related to mistakes in design and assembly caused by human beings.

### 8.6.1 Wiring problems

In this case, bad connections are usually due to assembly error, such as connection to the wrong point or poor connector fabrication. Shorted failures are also seen, but usually involve misconnections (conductors inadvertently attached to grounding points) or wires pinched under box covers.

Another wiring-related problem seen in new systems is that of electrostatic or electromagnetic interference between different circuits by way of close wiring proximity. This kind of problem is easily created by routing sets of wires too close to each other (especially routing signal cables close to power conductors), and tends to be very difficult to identify and locate with test equipment.

### 8.6.2 Power supply problems

Blown fuses and tripped circuit breakers are likely sources of trouble, especially if the project in question is an addition to an already-functioning system. Loads may be larger than expected, resulting in overloading and subsequent failure of power supplies.

### 8.6.3 Defective components

In the case of a newly-assembled system, component fault probabilities are not as predictable as in the case of an operating system that fails with age. Any type of component - active or passive - may be found defective or of imprecise value "out of the box" with roughly equal probability, barring any specific sensitivities in shipping (i.e fragile vacuum tubes or electrostatically sensitive semiconductor components). Moreover, these types of failures are not always as easy to identify by sight or smell as an age- or transient-induced failure.

### 8.6.4 Improper system configuration

Increasingly seen in large systems using microprocessor-based components, "programming" issues can still plague non-microprocessor systems in the form of incorrect time-delay relay settings, limit switch calibrations, and drum switch sequences. Complex components having configuration "jumpers" or switches to control behavior may not be "programmed" properly.

Components may be used in a new system outside of their tolerable ranges. Resistors, for example, with too low of power ratings, of too great of tolerance, may have been installed. Sensors, instruments, and controlling mechanisms may be uncalibrated, or calibrated to the wrong ranges.

### 8.6.5 Design error

Perhaps the most difficult to pinpoint and the slowest to be recognized (especially by the chief designer) is the problem of design error, where the system fails to function simply because it cannot function as designed. This may be as trivial as the designer specifying the wrong components in a system, or as fundamental as a system not working due to the designer's improper knowledge of physics.

I once saw a turbine control system installed that used a low-pressure switch on the lubrication oil tubing to shut down the turbine if oil pressure dropped to an insufficient level. The oil pressure for lubrication was supplied by an oil pump turned by the turbine. When installed, the turbine refused to start. Why? Because when it was stopped, the oil pump was not turning, thus there was no oil pressure to lubricate the turbine. The low-oil-pressure switch detected this condition and the control system maintained the turbine in shutdown mode, preventing it from starting. This is a classic example of a design flaw, and it could only be corrected by a change in the system logic.

While most design flaws manifest themselves early in the operational life of the system, some remain hidden until just the right conditions exist to trigger the fault. These types of flaws are the most difficult to uncover, as the troubleshooter usually overlooks the possibility of design error due to the fact that the system is assumed to be "proven." The example of the turbine lubrication system was a design flaw impossible to ignore on start-up. An example of a "hidden" design flaw might be a faulty emergency coolant system for a machine, designed to remain inactive until certain abnormal conditions are reached - conditions which might never be experienced in the life of the system.

### 8.7 Potential pitfalls

Fallacious reasoning and poor interpersonal relations account for more failed or belabored troubleshooting efforts than any other impediments. With this in mind, the aspiring troubleshooter needs to be familiar with a few common troubleshooting mistakes.

Trusting that a brand-new component will always be good. While it is generally true that a new component will be in good condition, it is not always true. It is also possible that a component has been mis-labeled and may have the wrong value (usually this mis-labeling is a mistake made at the point of distribution or warehousing and not at the manufacturer, but again, not always!).

Not periodically checking your test equipment. This is especially true with batterypowered meters, as weak batteries may give spurious readings. When using meters to safety-check for dangerous voltage, remember to test the meter on a known source of voltage both before and after checking the circuit to be serviced, to make sure the meter is in proper operating condition.

Assuming there is only one failure to account for the problem. Single-failure system problems are ideal for troubleshooting, but sometimes failures come in multiple numbers. In some instances, the failure of one component may lead to a system condition that damages other components. Sometimes a component in marginal condition goes undetected for a long time, then when another component fails the system suffers from problems with both components.

Mistaking coincidence for causality. Just because two events occurred at nearly the same time does not necessarily mean one event caused the other! They may be both consequences of a common cause, or they may be totally unrelated! If possible, try to duplicate the same condition suspected to be the cause and see if the event suspected to be the coincidence happens again. If not, then there is either no causal relationship as assumed. This may mean there is no causal relationship between the two events whatsoever, or that there is a causal relationship, but just not the one you expected.

Self-induced blindness. After a long effort at troubleshooting a difficult problem, you may become tired and begin to overlook crucial clues to the problem. Take a break and let someone else look at it for a while. You will be amazed at what a difference this can make. On the other hand, it is generally a bad idea to solicit help at the start of the troubleshooting process. Effective troubleshooting involves complex, multi-level thinking, which is not easily communicated with others. More often than not, "team troubleshooting" takes more time and causes more frustration than doing it yourself. An exception to this rule is when the knowledge of the troubleshooters is complementary: for example, a technician who knows electronics but not machine operation, teamed with an operator who knows machine function but not electronics.

Failing to question the troubleshooting work of others on the same job. This may sound rather cynical and misanthropic, but it is sound scientific practice. Because it is easy to overlook important details, troubleshooting data received from another troubleshooter should be personally verified before proceeding. This is a common situation when troubleshooters "change shifts" and a technician takes over for another technician who is leaving before the job is done. It is important to exchange information, but do not assume the prior technician checked everything they said they did, or checked it perfectly. I've been hindered in my troubleshooting efforts on many occasions by failing to verify what someone else told me they checked.

Being pressured to "hurry up." When an important system fails, there will be pressure from other people to fix the problem as quickly as possible. As they say in business, "time is money." Having been on the receiving end of this pressure many times, I can understand the need for expedience. However, in many cases there is a higher priority: caution. If the system in question harbors great danger to life and limb, the pressure to "hurry up" may result in injury or death. At the very least, hasty repairs may result in further damage when the system is restarted. Most failures can be recovered or at least temporarily repaired in short time if approached intelligently. Improper "fixes" resulting in haste often lead to damage that cannot be recovered in short time, if ever. If the potential for greater harm is present, the troubleshooter needs to politely address the pressure received from others, and maintain their perspective in the midst of chaos. Interpersonal skills are just as important in this realm as technical ability!

Finger-pointing. It is all too easy to blame a problem on someone else, for reasons of ignorance, pride, laziness, or some other unfortunate facet of human nature. When the responsibility for system maintenance is divided into departments or work crews, troubleshooting efforts are often hindered by blame cast between groups. "It's a mechanical problem . . . it's an electrical problem . . . it's an instrument problem . . ." ad infinitum, ad nauseum, is all too common in the workplace. I have found that a positive attitude does more to quench the fires of blame than anything else.

On one particular job, I was summoned to fix a problem in a hydraulic system assumed to be related to the electronic metering and controls. My troubleshooting isolated the source of trouble to a faulty control valve, which was the domain of the millwright (mechanical) crew. I knew that the millwright on shift was a contentious person, so I expected trouble if I simply passed the problem on to his department. Instead, I politely explained to him and his supervisor the nature of the problem as well as a brief synopsis of my reasoning, then proceeded to help him replace the faulty valve, even though it wasn't "my" responsibility to do so. As a result, the problem was fixed very quickly, and I gained the respect of the millwright.

### 8.8 Contributors

Contributors to this chapter are listed in chronological order of their contributions, from most recent to first. See Appendix 2 (Contributor List) for dates and contact information.

Alejandro Gamero Divasto (January 2002): contributed troubleshooting tips regarding potential hazards of swapping two similar components, avoiding pressure placed on the troubleshooter, perils of "team" troubleshooting, wisdom of recording system history, operator error as a cause of failure, and the perils of finger-pointing.

## Chapter 9

## CIRCUIT SCHEMATIC SYMBOLS

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### 9.1 Wires and connections



Older electrical schematics showed connecting wires crossing, while non-connecting wires "jumped" over each other with little half-circle marks. Newer electrical schematics show connecting wires joining with a dot, while non-connecting wires cross with no dot. However, some people still use the older convention of connecting wires crossing with no dot, which may create confusion.

For this reason, I opt to use a hybrid convention, with connecting wires unambiguously connected by a dot, and non-connecting wires unambiguously "jumping" over one another with a half-circle mark. While this may be frowned upon by some, it leaves no room for interpretational error: in each case, the intent is clear and unmistakable:

## Convention used in this book



### 9.2 Power sources

DC voltage


AC voltage
$\%$
Variable
DC voltage


AC current


### 9.3 Resistors



Rheostat



Photoresistor


### 9.4 Capacitors

$$
\begin{gathered}
\text { Non-polarized } \\
=1
\end{gathered}
$$



### 9.5 Inductors

| Fixed-value |  | Iron core |
| :---: | :---: | :---: |
| $\xi \quad\}$ |  | $\hat{3} \\|$ \# |
| Variable | Variac | Tapped |
| 多 | $\underset{\sim}{3}$ | $-2$ |

### 9.6 Mutual inductors



Synchro

9.7 Switches, hand actuated


### 9.8 Switches, process actuated

## Normally open shown on top; normally closed on bottom



It is very important to keep in mind that the "normal" contact status of a process-actuated switch refers to its status when the process is absent and/or inactive, not "normal" in the sense of process conditions as expected during routine operation. For instance, a normally-closed low-flow detection switch installed on a coolant pipe will be maintained in the actuated state (open) when there is regular coolant flow through the pipe. If the coolant flow stops, the flow switch will go to its "normal" (unactuated) status of closed.

A limit switch is one actuated by contact with a moving machine part. An electronic limit switch senses mechanical motion, but does so using light, magnetic fields, or other non-contact means.

### 9.9 Switches, electrically actuated (relays)

Relay components, "ladder logic" notation style


Relays, electronic schematic notation style


### 9.10 Connectors



Plug \& Jack connected
Receptacle

(female) | Household |
| :---: |
| power |
| connectors |



### 9.11 Diodes

| Generic | Schottky | Shockley | Constant current |
| :---: | :---: | :---: | :---: |
| ${ }_{\mathrm{A}} \rightarrow$ ¢ | $\mathrm{A}_{\rightarrow} \mathrm{f}{ }_{\mathrm{k}}$ | ${ }_{\text {A }} \mathrm{N}^{\text {k }}$ | ${ }_{\text {}} \rightarrow \mathrm{I}{ }_{\text {k }}$ |



### 9.12 Transistors, bipolar



Dual-emitter NPN Dual-emitter PNP




### 9.13 Transistors, junction field-effect (JFET)



### 9.14 Transistors, insulated-gate field-effect (IGFET or MOSFET)


9.15 Transistors, hybrid

IGBT (NPN)


IGBT (PNP)

. . . with case


IGBT (N-channel)
IGBT (P-channel)

$$
{ }_{E}^{\frac{Q^{G}}{J T T}}
$$

${ }_{E}^{L_{E}^{G}} T_{1}$

$$
\begin{aligned}
& \mathrm{E}=\text { Emitter } \\
& \mathrm{G}=\text { Gate } \\
& \mathrm{C}=\text { Collector }
\end{aligned}
$$

### 9.16 Thyristors



### 9.17 Integrated circuits




### 9.18 Electron tubes



Phototube


Thyratron


> Cathode Ray Tube


$$
\begin{array}{|lc|}
\hline \mathrm{P}=\text { Plate } & \mathrm{S}=\text { Screen } \\
\mathrm{G}=\text { Grid } & \mathrm{A}=\text { Anode } \\
\mathrm{C}=\text { Cathode } & \mathrm{H}=\text { Heater } \\
\mathrm{I}=\text { Ignitor } & \text { Sup }=\text { Suppressor } \\
\hline
\end{array}
$$

## Chapter 10

## PERIODIC TABLE OF THE ELEMENTS

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```

| Hydrogen <br> Hy <br> 1.00794 <br> $1 \mathrm{~s}^{1}$ |  | Periodic Table of the Elements |  |  |  |  |  |  |  |  |  | Metalloids |  |  | Nonmetals |  | He <br> 4.00260 <br> $4 \mathrm{Hel}^{2}$${ }^{2}$ | $\underset{\oplus}{\oplus}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{array}{\|l\|} \hline \mathrm{Li} \\ \text { Lithium } \\ 6.941 \\ 2 \mathrm{~s}^{1} \\ \hline \end{array}$ | Ber <br> Beryllium <br> 9.012182 <br> $2 s^{2}$ |  |  |  | K19 <br> Potassium <br> $39.0983-$ <br> $4 s^{1}$ | - Atomic mass (averaged according to occurence on earth) <br> Metals |  |  |  |  |  | BBoron <br>  <br> 10.81 <br> $2 p^{1}$${ }^{5} 1$ | C Carbon <br> 12.011 <br> $2 p^{2}$ | N <br> Nitrogen <br> 14.0067 <br> $2 p^{3}$ | OOxygen <br> 15.9994 <br> $2 p^{4}$ | Fruorine <br> Fl <br> 18.9984 <br> $2 p^{5}$ | $\mathrm{Ne} \quad 10$ <br> Neon <br> 20.179 <br> $2 p^{6}$ | $\underset{0}{1}$ |
| Na $\quad 11$ <br> Sodium <br> 22.989768 <br> $3 s^{1}$ | Mg 12 <br> Magnesium  <br> 24.3050  <br> $3 \mathrm{~s}^{2}$  |  |  | lectron <br> figuration |  |  |  |  |  |  |  | Al $\quad 13$ <br> Aluminum <br> 26.9815 <br> $3 p^{1}$ | $\begin{array}{\|cr\|} \hline \text { Si } & 14 \\ \text { Silicon } \\ 28.0855 \\ 3 \mathrm{p}^{2} & \\ \hline \end{array}$ | Pr $\quad 15$ <br> Phosphorus <br> 30.9738 <br> $3 p^{3}$ | $\begin{array}{\|l\|} \hline S^{\text {Sulfur }} \\ 32.06 \\ 3 p^{4} \end{array}$ | Cl $\quad 17$ <br> Chlorine <br> 35.453 <br> $3 p^{5}$ | Ar $\quad 18$ Argon 39.948 $3 p^{6}$ | (1) |
|  | Ca 20 Calcium 40.078 $4 s^{2}$ | Sc <br> Scandium <br> 44.955910 <br> $3 d^{1} 4 \mathrm{~s}^{2}$ | Ti 22 <br> Titanium <br> 47.88 <br> $3 d^{2} 4 s^{2}$ | $\begin{aligned} & \hline V \quad 23 \\ & \text { Vanadium } \\ & 50.9415 \\ & 3 d^{3} 4 \mathrm{~s}^{2} \end{aligned}$ | Cr $\quad 24$ <br> Chromium <br> 51.9961 <br> $3 d^{5} 4 \mathrm{~s}^{1}$ | Mn $\quad 25$ <br> Manganese <br> 54.93805 <br> $3 d^{5} 4 \mathrm{~s}^{2}$ | $\left\{\begin{array}{l} \mathrm{Fe} \quad 26 \\ \quad \text { Iron } \\ 55.847 \\ 3 d^{6} 4 \mathrm{~s}^{2} \end{array}\right.$ | Co 27 <br> Cobalt <br> 58.93320 <br> $3 \mathrm{~d}^{7} 4 \mathrm{~s}^{2}$ | $\mathrm{Ni} \quad 28$ <br> Nickel <br> 58.69 <br> $3 \mathrm{~d}^{8} 4 \mathrm{~s}^{2}$ | Cu $\quad 29$ <br> Copper <br> 63.546 <br> $3 \mathrm{~d}^{10} 4 \mathrm{~s}^{1}$ | $\begin{aligned} & \mathrm{Zn} \quad 30 \\ & \begin{array}{l} \text { Zinc } \\ 65.39 \\ 3 d^{10} 4 \mathrm{~s}^{2} \end{array} \\ & \hline \end{aligned}$ | Ga $\quad 31$ <br> Gallium <br> 69.723 <br> $4 p^{1}$ | Ger $\quad 32$ Germanium 72.61 $4 \mathrm{p}^{2}$ | As 33 <br> Arsenic <br> 74.92159 <br> $4 \mathrm{p}^{3}$ | Se $\quad 34$ Selenium 78.96 $4 p^{4}$ | $\mathrm{Br} \quad 35$ <br> Bromine <br> 79.904 <br> $4 \mathrm{p}^{5}$ | $\mathrm{Kr} \quad 36$ <br> Krypton <br> 83.80 <br> $4 p^{6}$ | $\underset{\sim}{\underset{\sim}{2}}$ |
| Rb <br> Rubidium <br> 85 <br> 85.4678 <br> $5 s^{1}$ | $\mathrm{Sr} \quad 38$ <br> Strontium <br> 87.62 <br> $5 \mathrm{~s}^{2}$ | $\begin{array}{\|lr} \hline \mathrm{Y}^{\text {YHtrium }} \\ 88.90585 \\ 4 d^{1} 5 \mathrm{~s}^{2} \\ \hline \end{array}$ | Zr $\quad 40$ <br> Zirconium <br> 91.224 <br> $4 d^{2} 5 s^{2}$ | Nb $\quad 41$ Niobium 92.90638 $4 d^{4} 5 s^{1}$ | Mo $\quad 42$ <br> Molybdenum <br> 95.94 <br> $4 d^{5} 5 s^{1}$ | Tc $\quad 43$ <br> Technetium <br> (98) <br> $4 d^{5} 5 s^{2}$ | Ru $\quad 44$ <br> Ruthenium <br> 101.07 <br> $4 d^{7} 5 s^{1}$ | Rh 45 <br> Rhodium <br> 102.90550 <br> $4 \mathrm{~d}^{8} 5 \mathrm{~s}^{1}$ | $\begin{array}{\|lr\|} \hline \text { Pd } \quad 46 \\ \text { Palladium } \\ 106.42 \\ 4 d^{10} 5 s^{\circ} \\ \hline \end{array}$ | $\mathrm{Ag} \quad 47$ Silver 107.8682 $4 d^{10} 5 s^{1}$ | Cd $\quad 48$ Cadmium 112.411 $4 d^{10} 5 s^{2}$ | $\begin{array}{\|lr} \hline \text { In } & 49 \\ \text { Indium } \\ 114.82 \\ 5 p^{1} \\ \hline \end{array}$ | $\begin{array}{\|l\|} \hline \text { Sn } 50 \\ \operatorname{Tin}^{118.710} \\ 5 p^{2} \\ \hline \end{array}$ | Sb $\quad 51$ <br> Antimony <br> 121.75 <br> $5 p^{3}$ | $\begin{array}{\|lr\|} \hline \text { Te } & 52 \\ \text { Tellurium } \\ 127.60 \\ 5 p^{4} & \\ \hline \end{array}$ | $\begin{array}{\|l\|} \hline \text { I } \quad 53 \\ \text { lodine } \\ 126.905 \\ 5 p^{5} \\ \hline \end{array}$ | Xe $\quad 54$ $\quad$ Xenon 131.30 $5 p^{6}$ | OV |
| Cs $\quad 55$ <br> Cesium <br> 132.90543 <br> $6 s^{1}$ | Ba <br> Barium <br> 137.327 <br> $6 \mathrm{~s}^{2}$ | 57-71Lanthanide <br> series | Hf 72 Hafnium 178.49 $5 d^{2} 6 s^{2}$ | Ta $\quad 73$ Tantalum 180.9479 $5 d^{3} 6 \mathrm{~s}^{2}$ | W $\quad 74$ <br> Tungsten <br> 183.85 <br> $5 d^{4} 6 s^{2}$ | Re $\quad 75$ <br> Rhenium <br> 186.207 <br> $5 d^{5} 6 s^{2}$ | Os $\quad 76$ <br> Osmium <br> 190.2 <br> $5 d^{6} 6 s^{2}$ | Ir $\quad 77$ <br> Iridium <br> 192.22 <br> $5 d^{7} 6 \mathrm{~s}^{2}$ | $\begin{array}{\|l\|} \hline \mathrm{Pt} \quad 78 \\ \text { Platinum } \\ 195.08 \\ 5 \mathrm{~d}^{9} 6 \mathrm{~s}^{1} \\ \hline \end{array}$ | Au 79 Gold 196.96654 $5 d^{10} 6 s^{1}$ | $\mathrm{Hg} \quad 80$ Mercury 200.59 $5 \mathrm{~d}^{10} 6 \mathrm{~s}^{2}$ | TI 81 <br> Thallium  <br> 204.3833  <br> $6 p^{1}$  | $\mathrm{Pb} \quad 82$ <br> Lead <br> 207.2 <br> $6 \mathrm{p}^{2}$ | $\mathrm{Bi} \quad 83$ <br> Bismuth <br> 208.98037 <br> $6 p^{3}$ | Po 84 Polonium $(209)$ $6 p^{4}$ | At 85 Astatine $(210)$ $6 p^{5}$ | Rn $\quad 86$ Radon $(222)$ $6 p^{6}$ | $\underset{\sum_{i}^{\infty}}{\substack{\infty}}$ |
| $\mathrm{Fr} r \mid$ <br> Francium <br> (223) <br> $7 \mathrm{~s}^{1}$ | Ra <br> Radium <br> $(226)$ <br> $7 \mathrm{~s}^{2}$ | 89-103 Actinide series | Unq 104 Unniquadium $(261)$ $6 d^{2} 7 \mathrm{~s}^{2}$ | Unp 105 <br> Unnilpentium <br> $(262)$ <br> $6 d^{3} 7 s^{2}$ | Unh 106 <br> Unnilhexium <br> $(263)$ <br> $6 d^{4} 7 \mathrm{~s}^{2}$ | Uns $\quad 107$ Unnisseptium (262) | 108 | 109 |  |  |  |  |  |  |  |  |  |  |


| Lanthanideseries | 57 | Ce | Pr | Nd 60 |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Lanthanum | Cerium | Prasedymium | Neodymium | Promethium | Samarium | Europium | Gadolinium | Terbium | Dysprosium | Holmium | Erbium | Thulium | Yterbium | Lutetiu |
|  | 138.905 | 140.115 | 140.90765 | 144.2 |  | 150.36 | 51.965 | 157.25 | 158.92534 | 162.50 | 164.9303 | 67.26 | 168.934 | . | 174.96 |
|  | $5 d^{1} 6 s^{2}$ | $4 f^{1} 5 d^{1} 6 s^{2}$ | $4 f^{3} 6 s^{2}$ | $4 \mathrm{f}^{4} 6 \mathrm{~s}^{2}$ | $\mathrm{s}^{2}$ | $4 f^{6} 6 \mathrm{~s}^{2}$ | $4 f^{7} 6 s^{2}$ | $4 \mathrm{f}^{7} 5 \mathrm{~d}^{1} 6 \mathrm{~s}^{2}$ | $4 f^{9} 6 \mathrm{~s}^{2}$ | $4 f^{10} 6 s^{2}$ | $4 f^{11} 6 s^{2}$ | $4 f^{12} 6 s^{2}$ | $4 f^{13} 6 s^{2}$ | $4 \mathrm{f}^{14} 6 \mathrm{~s}^{2}$ | $4 f^{14} 5 d^{1} 6 s^{2}$ |

Actinide
series

| Ac 89 | Th 90 | Pa 91 | 92 | Np 93 | Pu 94 | Am 95 | Cm 96 | Bk 97 | Cf 98 | Es 99 | Fm 100 | Md 101 | No 102 | Lr 103 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Actinium } \\ & (227) \end{aligned}$ | $\begin{aligned} & \text { Thorium } \\ & 232.0381 \end{aligned}$ | $\begin{aligned} & \text { Protactinium } \\ & 231.03588 \end{aligned}$ | $\begin{aligned} & \text { Uranium } \\ & 238.0289 \end{aligned}$ | $\begin{aligned} & \text { Neptunium } \\ & (237) \end{aligned}$ | $\begin{gathered} \text { Plutonium } \\ (244) \end{gathered}$ | $\underset{(243)}{\text { Americium }}$ | $\begin{gathered} \text { Curium } \\ (247) \end{gathered}$ | $\begin{array}{c\|} \text { Berkelium } \\ (247) \end{array}$ | $\begin{aligned} & \text { Californium } \\ & (251) \end{aligned}$ | $\begin{aligned} & \text { Einsteinium } \\ & (252) \end{aligned}$ | $\begin{aligned} & \text { Fermium } \\ & (257) \end{aligned}$ | $\begin{array}{\|c\|} \hline \text { Mendelevium } \\ (258) \end{array}$ | $\begin{aligned} & \text { Nobelium } \\ & (259) \end{aligned}$ | Lawrencium (260) |
| $6 d^{1} 7 \mathrm{~s}^{2}$ | $6 d^{2} 7 s^{2}$ | $5 f^{2} 6 d^{1} 7 \mathrm{~s}^{2}$ | $5 f^{3} 6 d^{1} 7 \mathrm{~s}^{2}$ | $5 f^{4} 6 d^{1} 7 s^{2}$ | $5 f^{6} 6 d^{0} 7 s^{2}$ | $5 f^{7} 6 d^{0} 7 \mathrm{~s}^{2}$ | $5 f^{7} 6 d^{1} 7 \mathrm{~s}^{2}$ | $5 f^{9} 6 d^{0} 7 \mathrm{~s}^{2}$ | $5 f^{10} 6 d^{0} 7 s^{2}$ | $5 f^{11} 6 d^{0} 7 s^{2}$ | $5 f^{12} 6 d^{0} 7 s^{2}$ | $5 f^{13} 6 d^{0} 7 s^{2}$ | $6 d^{0} 7 s^{2}$ | $6 d^{1} 7 \mathrm{~s}^{2}$ |

### 10.2 Table (portrait view)



### 10.3 Data

Atomic masses shown in parentheses indicate the most stable isotope (longest half-life) known.
Electron configuration data was taken from Douglas C. Giancoli's Physics, 3rd edition. Average atomic masses were taken from Kenneth W. Whitten's, Kenneth D. Gailey's, and Raymond E. Davis' General Chemistry, 3rd edition. In the latter book, the masses were specified as 1985 IUPAC values.

## Appendix A-1

## CONTRIBUTOR LIST

## A-1.1 How to contribute to this book

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## A-1.2 Credits

All entries arranged in alphabetical order of surname. Major contributions are listed by individual name with some detail on the nature of the contribution(s), date, contact info, etc. Minor contributions (typo corrections, etc.) are listed by name only for reasons of brevity. Please understand that when I classify a contribution as "minor," it is in no way inferior to the effort or value of a "major" contribution, just smaller in the sense of less text changed. Any and all contributions are gratefully accepted. I am indebted to all those who have given freely of their own knowledge, time, and resources to make this a better book!

## A-1.2.1 Dennis Crunkilton

- Date(s) of contribution(s):October 2005 to present
- Nature of contribution:Ch 1, added permitivity, capacitor and inductor formulas, wire table; 10/2005.
- Nature of contribution: Ch 1, expanded dielectric table, 10232.eps, copied data from Volume 1, Chapter 13; 10/2005.
- Nature of contribution: Mini table of contents, all chapters except appedicies; html, latex, ps, pdf; See Devel/tutorial.html; 01/2006.
- Contact at: dcrunkilton(at)att(dot)net


## A-1.2.2 Alejandro Gamero Divasto

- Date(s) of contribution(s): January 2002
- Nature of contribution: Suggestions related to troubleshooting: caveat regarding swapping two similar components as a troubleshooting tool; avoiding pressure placed on the troubleshooter; perils of "team" troubleshooting; wisdom of recording system history; operator error as a cause of failure; and the perils of finger-pointing.


## A-1.2.3 Tony R. Kuphaldt

- Date(s) of contribution(s): 1996 to present
- Nature of contribution: Original author.
- Contact at: liec0@lycos.com


## A-1.2.4 Your name here

- Date(s) of contribution(s): Month and year of contribution
- Nature of contribution: Insert text here, describing how you contributed to the book.
- Contact at: my_email@provider.net


## A-1.2.5 Typo corrections and other "minor" contributions

- The students of Bellingham Technical College's Instrumentation program.
- Bernard Sheehan (January 2005), Typographical error correction in "Right triangle trigonometry" section Chapter 5: TRIGONOMETRY REFERENCE (two formulas for tan x the second one reads $\tan \mathrm{x}=\cos \mathrm{x} / \sin \mathrm{x}$ it should be $\cot \mathrm{x}=\cos \mathrm{x} / \sin \mathrm{x}-$ changes to 01001.eps previously made)
- Chirvasuta Constantin (April 2003) Identified error in quadratic equation formula.
- Jeff DeFreitas (March 2006)Improve appearance: replace "/" and "/" Chapters: A1, A2.
- Gerald Gardner (January 2003) Suggested adding Imperial gallons conversion to table.
- Harvey Lew (??? 2003) Typo correction in Trig chapter: "tangent" should have been "cotangent".
- Don Stalkowski (June 2002) Technical help with PostScript-to-PDF file format conversion.
- Joseph Teichman (June 2002) Suggestion and technical help regarding use of PNG images instead of JPEG.


## Appendix A-2

## ABOUT THIS BOOK

## A-2.1 Purpose

They say that necessity is the mother of invention. At least in the case of this book, that adage is true. As an industrial electronics instructor, I was forced to use a sub-standard textbook during my first year of teaching. My students were daily frustrated with the many typographical errors and obscure explanations in this book, having spent much time at home struggling to comprehend the material within. Worse yet were the many incorrect answers in the back of the book to selected problems. Adding insult to injury was the $\$ 100+$ price.

Contacting the publisher proved to be an exercise in futility. Even though the particular text I was using had been in print and in popular use for a couple of years, they claimed my complaint was the first they'd ever heard. My request to review the draft for the next edition of their book was met with disinterest on their part, and I resolved to find an alternative text.

Finding a suitable alternative was more difficult than I had imagined. Sure, there were plenty of texts in print, but the really good books seemed a bit too heavy on the math and the less intimidating books omitted a lot of information I felt was important. Some of the best books were out of print, and those that were still being printed were quite expensive.

It was out of frustration that I compiled Lessons in Electric Circuits from notes and ideas I had been collecting for years. My primary goal was to put readable, high-quality information into the hands of my students, but a secondary goal was to make the book as affordable as possible. Over the years, I had experienced the benefit of receiving free instruction and encouragement in my pursuit of learning electronics from many people, including several teachers of mine in elementary and high school. Their selfless assistance played a key role in my own studies, paving the way for a rewarding career and fascinating hobby. If only I could extend the gift of their help by giving to other people what they gave to me . . .

So, I decided to make the book freely available. More than that, I decided to make it "open," following the same development model used in the making of free software (most notably the various UNIX utilities released by the Free Software Foundation, and the Linux operating system, whose fame is growing even as I write). The goal was to copyright the text - so as to protect my authorship

- but expressly allow anyone to distribute and/or modify the text to suit their own needs with a minimum of legal encumbrance. This willful and formal revoking of standard distribution limitations under copyright is whimsically termed copyleft. Anyone can "copyleft" their creative work simply by appending a notice to that effect on their work, but several Licenses already exist, covering the fine legal points in great detail.

The first such License I applied to my work was the GPL - General Public License - of the Free Software Foundation (GNU). The GPL, however, is intended to copyleft works of computer software, and although its introductory language is broad enough to cover works of text, its wording is not as clear as it could be for that application. When other, less specific copyleft Licenses began appearing within the free software community, I chose one of them (the Design Science License, or $\mathrm{DSL})$ as the official notice for my project.

In "copylefting" this text, I guaranteed that no instructor would be limited by a text insufficient for their needs, as I had been with error-ridden textbooks from major publishers. I'm sure this book in its initial form will not satisfy everyone, but anyone has the freedom to change it, leveraging my efforts to suit variant and individual requirements. For the beginning student of electronics, learn what you can from this book, editing it as you feel necessary if you come across a useful piece of information. Then, if you pass it on to someone else, you will be giving them something better than what you received. For the instructor or electronics professional, feel free to use this as a reference manual, adding or editing to your heart's content. The only "catch" is this: if you plan to distribute your modified version of this text, you must give credit where credit is due (to me, the original author, and anyone else whose modifications are contained in your version), and you must ensure that whoever you give the text to is aware of their freedom to similarly share and edit the text. The next chapter covers this process in more detail.

It must be mentioned that although I strive to maintain technical accuracy in all of this book's content, the subject matter is broad and harbors many potential dangers. Electricity maims and kills without provocation, and deserves the utmost respect. I strongly encourage experimentation on the part of the reader, but only with circuits powered by small batteries where there is no risk of electric shock, fire, explosion, etc. High-power electric circuits should be left to the care of trained professionals! The Design Science License clearly states that neither I nor any contributors to this book bear any liability for what is done with its contents.

## A-2.2 The use of SPICE

One of the best ways to learn how things work is to follow the inductive approach: to observe specific instances of things working and derive general conclusions from those observations. In science education, labwork is the traditionally accepted venue for this type of learning, although in many cases labs are designed by educators to reinforce principles previously learned through lecture or textbook reading, rather than to allow the student to learn on their own through a truly exploratory process.

Having taught myself most of the electronics that I know, I appreciate the sense of frustration students may have in teaching themselves from books. Although electronic components are typically inexpensive, not everyone has the means or opportunity to set up a laboratory in their own homes, and when things go wrong there's no one to ask for help. Most textbooks seem to approach the task of education from a deductive perspective: tell the student how things are supposed to work, then apply those principles to specific instances that the student may or may not be able to explore by
themselves. The inductive approach, as useful as it is, is hard to find in the pages of a book.
However, textbooks don't have to be this way. I discovered this when I started to learn a computer program called SPICE. It is a text-based piece of software intended to model circuits and provide analyses of voltage, current, frequency, etc. Although nothing is quite as good as building real circuits to gain knowledge in electronics, computer simulation is an excellent alternative. In learning how to use this powerful tool, I made a discovery: SPICE could be used within a textbook to present circuit simulations to allow students to "observe" the phenomena for themselves. This way, the readers could learn the concepts inductively (by interpreting SPICE's output) as well as deductively (by interpreting my explanations). Furthermore, in seeing SPICE used over and over again, they should be able to understand how to use it themselves, providing a perfectly safe means of experimentation on their own computers with circuit simulations of their own design.

Another advantage to including computer analyses in a textbook is the empirical verification it adds to the concepts presented. Without demonstrations, the reader is left to take the author's statements on faith, trusting that what has been written is indeed accurate. The problem with faith, of course, is that it is only as good as the authority in which it is placed and the accuracy of interpretation through which it is understood. Authors, like all human beings, are liable to err and/or communicate poorly. With demonstrations, however, the reader can immediately see for themselves that what the author describes is indeed true. Demonstrations also serve to clarify the meaning of the text with concrete examples.

SPICE is introduced early in volume I (DC) of this book series, and hopefully in a gentle enough way that it doesn't create confusion. For those wishing to learn more, a chapter in this volume (volume V ) contains an overview of SPICE with many example circuits. There may be more flashy (graphic) circuit simulation programs in existence, but SPICE is free, a virtue complementing the charitable philosophy of this book very nicely.

## A-2.3 Acknowledgements

First, I wish to thank my wife, whose patience during those many and long evenings (and weekends!) of typing has been extraordinary.

I also wish to thank those whose open-source software development efforts have made this endeavor all the more affordable and pleasurable. The following is a list of various free computer software used to make this book, and the respective programmers:

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- Vim text editor - Bram Moolenaar and others.
- Xcircuit drafting program - Tim Edwards.
- SPICE circuit simulation program - too many contributors to mention.
- TEX text processing system - Donald Knuth and others.
- Texinfo document formatting system - Free Software Foundation.
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Thanks to Michael Stutz for drafting his Design Science License, and to Richard Stallman for pioneering the concept of copyleft.

Last but certainly not least, many thanks to my parents and those teachers of mine who saw in me a desire to learn about electricity, and who kindled that flame into a passion for discovery and intellectual adventure. I honor you by helping others as you have helped me.

Tony Kuphaldt, July 2001
"A candle loses nothing of its light when lighting another"
Kahlil Gibran

## Appendix A-3

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## A-3.2.2 Alejandro Gamero Divasto

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## Appendix A-4

## DESIGN SCIENCE LICENSE

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