

# Glossary of Symbols

## GENERAL MATHEMATICAL SYMBOLS

		Page
$\cup$	union	
$\cap$	intersection	
$\subseteq$	subset	
$\subset$	proper subset	
$\setminus$	set-theoretic difference	
$\Delta$	symmetric difference	
$[x]$	greatest integer $\leq x$	
$\{x\}$	least integer $\geq x$	
$\ f\ $	support of $f$	215
$\mathbf{R} \upharpoonright S$	restriction of $\mathbf{R}$ to $S$	215
$\mathbf{R}'$	transpose of $\mathbf{R}$	

## GRAPH-THEORETIC SYMBOLS

$A$	arc set	171
$\mathbf{A}$	adjacency matrix of a graph	7
$\mathbf{A}$	adjacency matrix of a digraph	173
$b(f)$	boundary of $f$	140
$\mathcal{B}$	bond space	213
$c(G)$	closure of $G$	56
$\text{cap } K$	capacity of cut $K$	194
$\mathcal{C}$	cycle space	212
$d_G(v)$	degree of vertex $v$ in $G$	10
$d_G(f)$	degree of face $f$ in $G$	140
$d_D^-(v)$	indegree of $v$ in $D$	172
$d_D^+(v)$	outdegree of $v$ in $D$	172
$d_G(u, v)$	distance between $u$ and $v$ in $G$	14
$D$	directed graph	171
$D(G)$	associated digraph of $G$	179
$\text{ext } J$	exterior of $J$	135
$\text{Ext } J$	closure of $\text{ext } J$	135
$E$	edge set	1
$f^-(S)$	flow into $S$	191
$f^+(S)$	flow out of $S$	191
$F$	face set	139
$F(B, \tilde{H})$	set of faces of $\tilde{H}$ in which $B$ is drawable	164

		Page
$G$	graph	1
$G[S]$	subgraph of $G$ induced by $S$	9
$\text{int } J$	interior of $J$	135
$\text{Int } J$	closure of $\text{int } J$	135
$K_n$	complete graph	4
$K_{m,n}$	complete bipartite graph	5
$\mathbf{M}$	incidence matrix of a graph	7
$\mathbf{M}$	incidence matrix of a digraph	214
$N$	network	191
$N_G(S)$	neighbour set of $S$ in $G$	72
$N_D^-(v)$	in-neighbour set of $v$ in $D$	175
$N_D^+(v)$	out-neighbour set of $v$ in $D$	175
$r(k, l)$	Ramsey number	103
$r(k_1, k_2, \dots, k_m)$	Ramsey number	108
$r_n$	$r(3, 3, \dots, 3)$	108
$\text{val } f$	value of flow $f$	192
$V$	vertex set	1
$V(B, H)$	set of vertices of attachment of $B$ to $H$	146
$\alpha$	independence number	101
$\alpha'$	edge independence number	102
$\beta$	covering number	101
$\beta'$	edge covering number	102
$\delta$	minimum degree	10
$\delta^-$	minimum indegree	172
$\delta^+$	minimum outdegree	172
$\Delta$	maximum degree	10
$\Delta^-$	maximum indegree	172
$\Delta^+$	maximum outdegree	172
$\varepsilon$	number of edges	3
$\kappa$	connectivity	42
$\kappa'$	edge connectivity	42
$\nu$	number of vertices	3
$o$	number of odd components	76
$\pi_k$	chromatic polynomial	125
$\tau$	number of spanning trees	32
$\phi$	number of faces	139
$\chi$	chromatic number	117
$\chi'$	edge chromatic number	91
$\chi^*$	face chromatic number	158
$\omega$	number of components	13
$\bar{D}$	converse of $D$	173
$\hat{D}$	condensation of $D$	173

		<i>Page</i>
$G^c$	complement of $G$	6
$G^*$	dual of $G$	140
$\tilde{G}$	planar embedding of $G$	135
$W^{-1}$	reverse of walk $W$	12
$G \cdot e$	contraction of $e$	32
$G - e$	deletion of $e$	9
$G + e$	addition of $e$	9
$G - v$	deletion of $v$	9
$G + E'$	addition of $E'$	9
$G - S$	deletion of $S$	9
$G \cong H$	isomorphism	4
$H \subseteq G$	subgraph	8
$H \subset G$	proper subgraph	8
$G \cup H$	union	9
$G \cap H$	intersection	10
$G + H$	disjoint union	10
$G \times H$	product	96
$G \vee H$	join	58
$\bar{H}(G)$	complement of $H$ in $G$	29
$[S, T]$	set of edges between $S$ and $T$	29
$(S, T)$	set of arcs from $S$ to $T$	176
$WW'$	concatenation of walks	12